

At-wavelength metrology with grating based shearing interferometer at DLS

Hongchang Wang¹, Kawal Sawhney¹, Sébastien Berujon^{1, 2},
Eric Ziegler², Christian David³, Timm Weitkamp⁴

¹Diamond Light Source,

²European Synchrotron Radiation Facility,

³ Paul Scherrer Institut

⁴Synchrotron Soleil

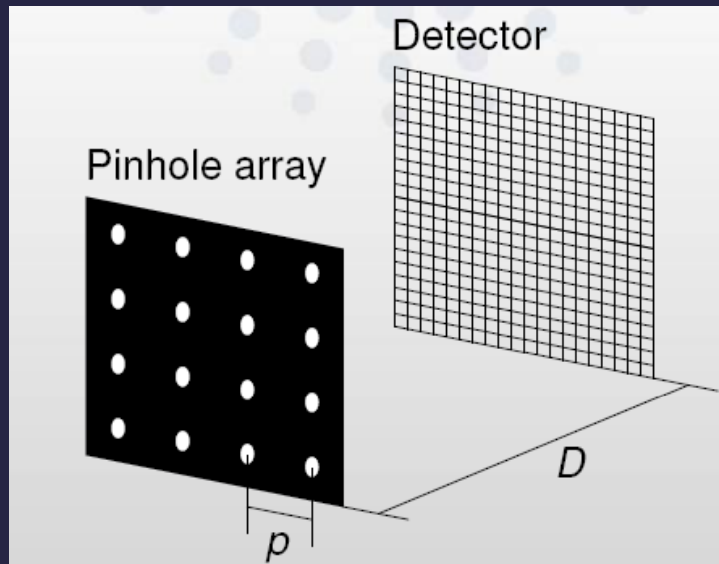


Outline

- **Introduction**
- **Rotating shearing interferometer**
- **Characterisation of Parabolic refractive lens**
- **Characterisation of X-ray mirror**
- **Summary and Outlook**

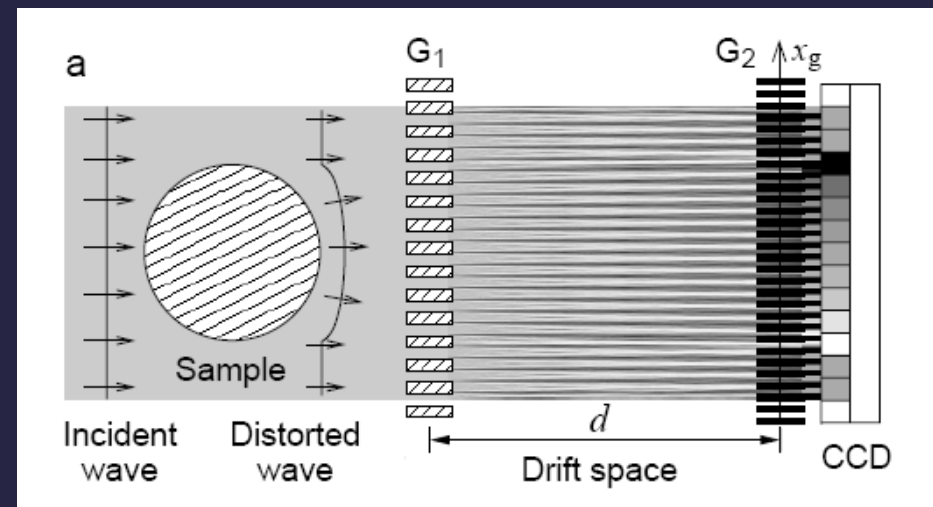
At-wavelength Metrology

Hartmann sensor



- ☹️ Low photon efficiency
- ☹️ Restricted to near field
- ☺️ Two dimensional information

Grating shearing interferometer

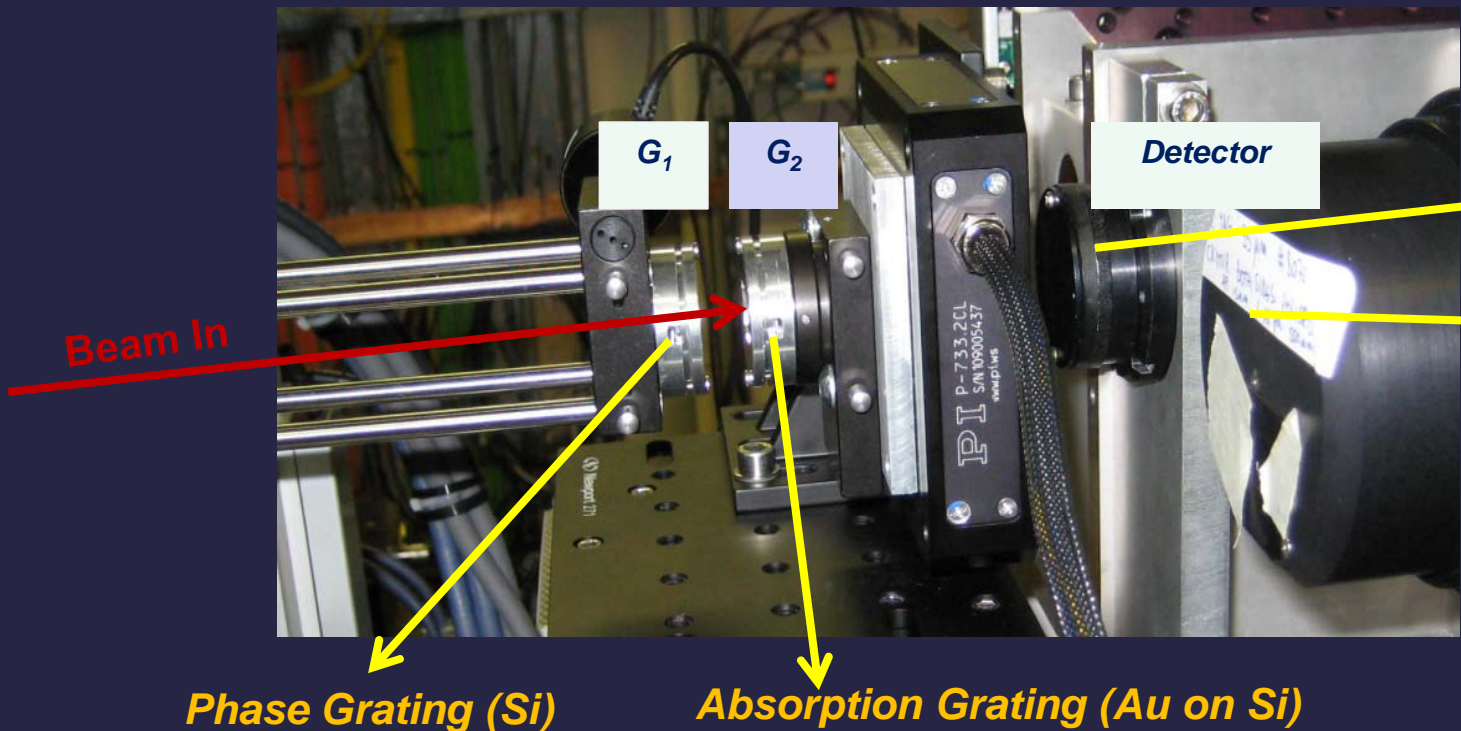


- ☺️ High photon efficiency
 - ☺️ High sensitivity
 - ☺️ Gives information about coherence function
- Two modes of operation:
(1) phase stepping (2) More Fringe analysis

J. Hartmann, Z. Instrumentenkd. **20** (1900) 47–58

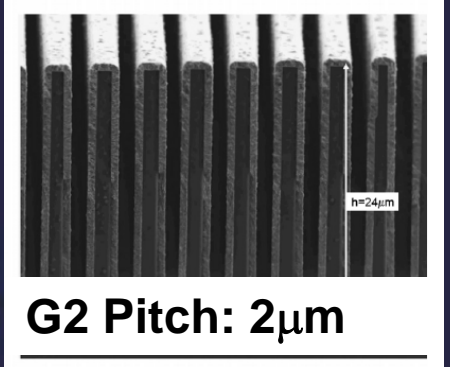
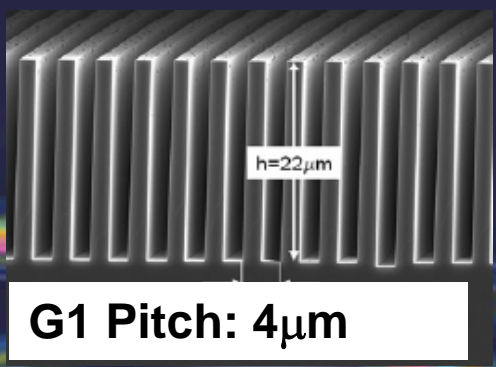
T. Weitkamp, et al, Opt. Express, 13, 6296 (2005)
T. Weitkamp, et al., Appl. Phys. Lett. 86, 054101 (2005)
T. Weitkamp, et al., SPIE. 5533, 140 (2004)

Grating setup at DLS B16



Detector:
MFDI: 6.4 μ m/pix

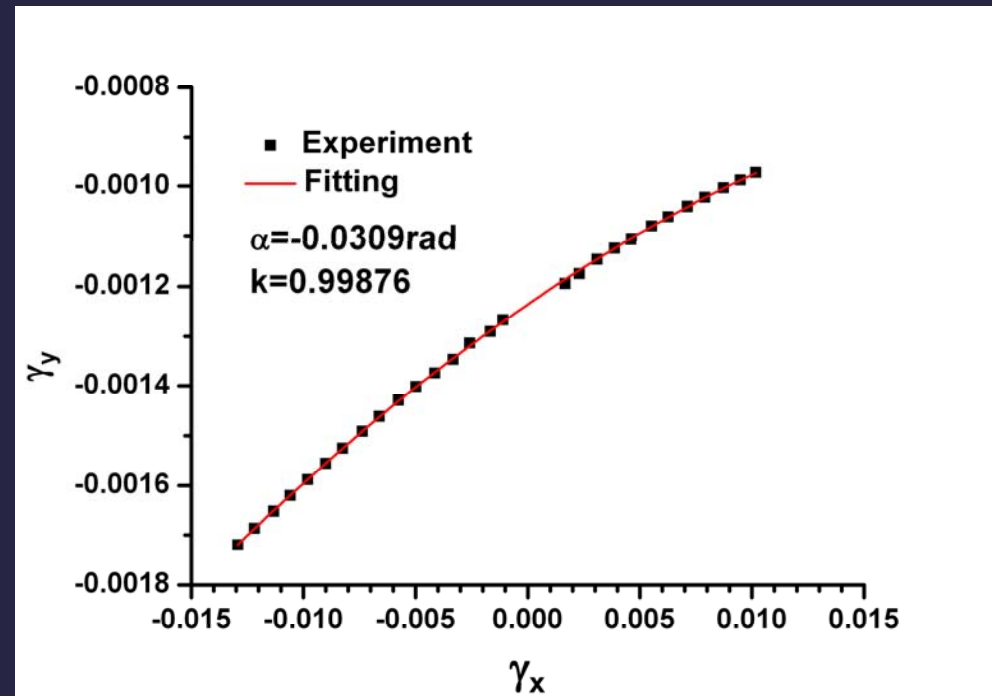
PCO 4000
4X: 0.9 μ m/pix
10X: 0.36 μ m/pix
20X: 0.18 μ m/pix



Grating Image Courtesy of C. David, Microelectronic Engineering, 84, 2007



Rotating shearing interferometer



$\alpha \rightarrow$ G2 misalign angle
 $k \rightarrow$ Wavefront Radius of Curvature

Experiment at DLS B16: Hongchang Wang and Kawal Sawhney



Radius of Curvature for Flat field Wavefront

d0 G1 Pitch

$$d_0 = 4 \mu\text{m}?$$

d2 G2 Pitch

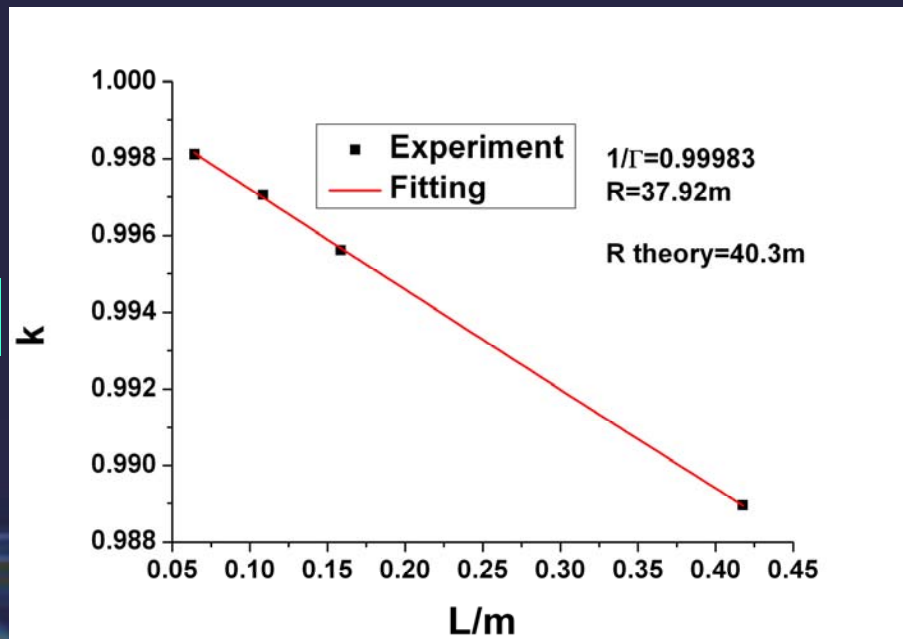
$$d_2 = 2 \mu\text{m}?$$

$$d_0 / 2 = \Gamma d_2$$

R: Radius of Curvature

$$\frac{R}{R+L} = \Gamma k$$

Order	L/m	α/rad	k	R/m ($\Gamma=1$)
3rd	0.0643	-0.0351	0.9981	33.96
5th	0.1085	-0.0352	0.9971	36.67
7th	0.1585	-0.0352	0.9956	36.03
19th	0.4175	-0.0354	0.9889	37.20

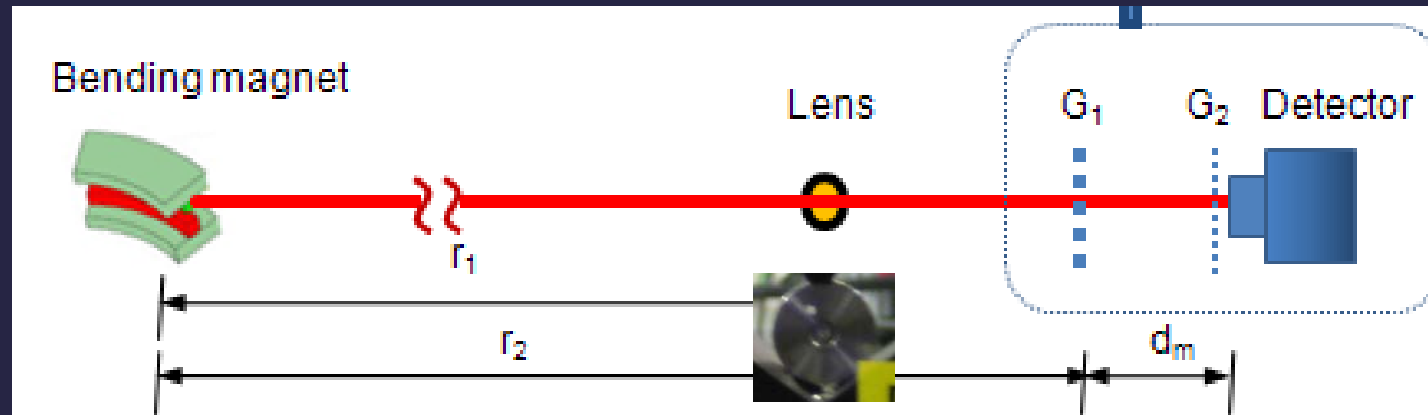


$$R_{\text{exp}} = 37.9\text{m}$$

$$R_{\text{theory}} = 40.3\text{m}$$

diamond

Characterization of Parabolic refractive lens

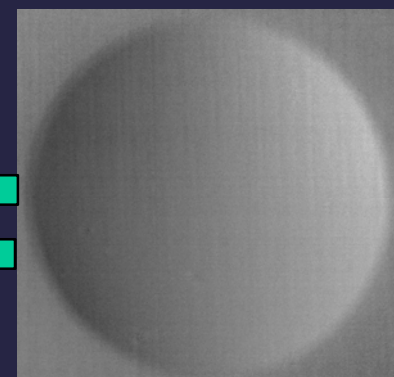
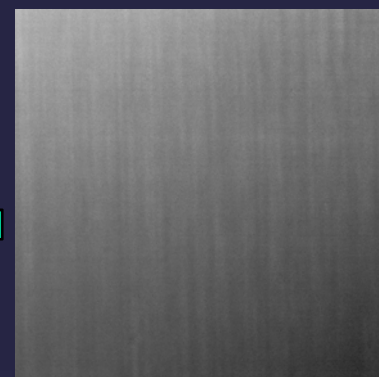
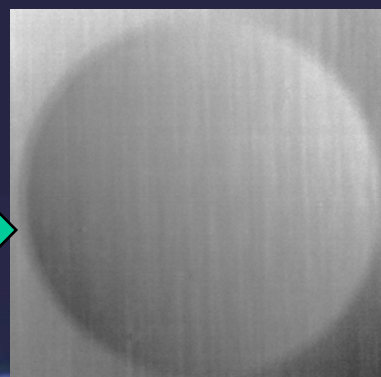
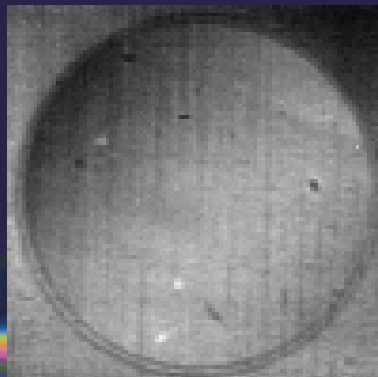


Phase stepping

Without Flat Field correction

Flat Field

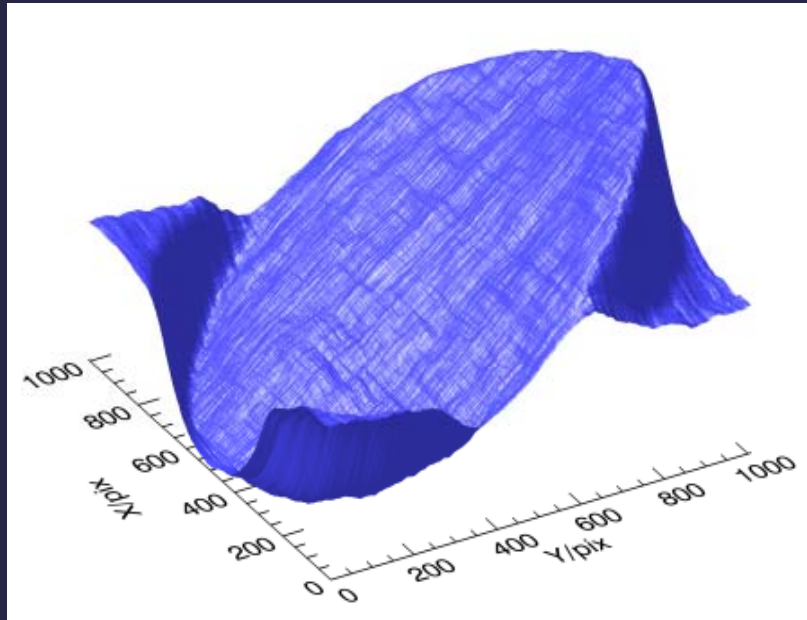
With Flat Field correction



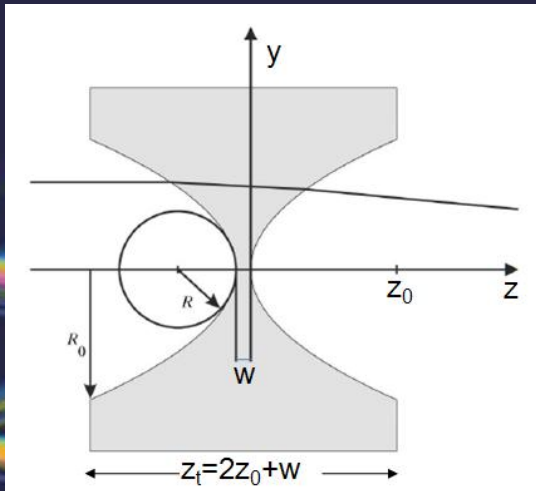
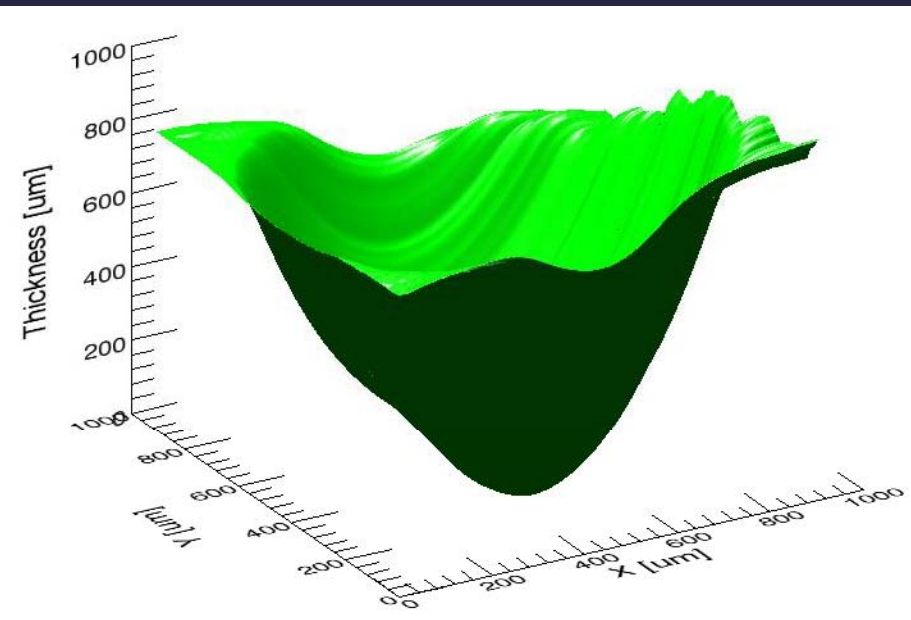
Experiment at DLS B16: Hongchang Wang and Kawal Sawhney, 2010

Characterisation of Parabolic refractive lens

Phase Gradient distribution



Relative thickness distribution



$$\alpha_x = \frac{r_2}{r_1} \frac{d_2}{2\pi d_m} \phi_x$$

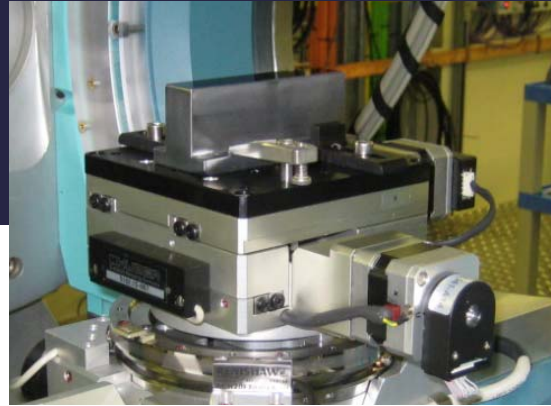
$$\Phi_{lens} = \int_0^{L_x} \frac{r_2}{r_1} \frac{d_2}{\lambda d_m} \phi_x dx$$

$$\Delta\Phi = \frac{2\pi}{\lambda} \times h \times \delta$$

	$R_0/\mu\text{m}$	$R/\mu\text{m}$	f/m	$2z_0/\mu\text{m}$	$\Delta\Phi_{\text{max}}/\text{rad}$
Theory	400	200	64.5	800	93.2
Test	450	250	80.8	810	94.5

Plane mirror characterization

Plane Mirror:
100mm (L) *10mm (W)
Slope Error: $0.2\mu\text{rad}$



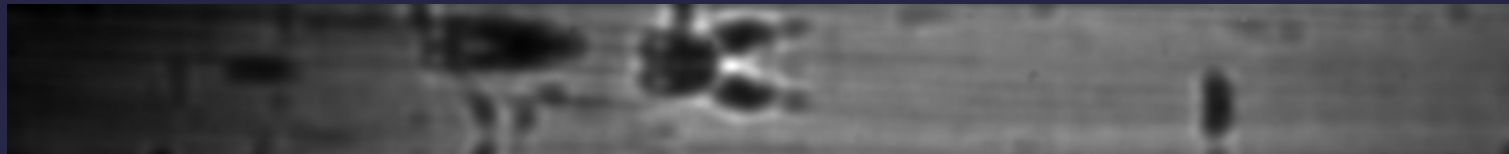
B16 Bending magnet



Mirror

G₁ G₂ Detector

Phase Stepping



Moiré Fringe

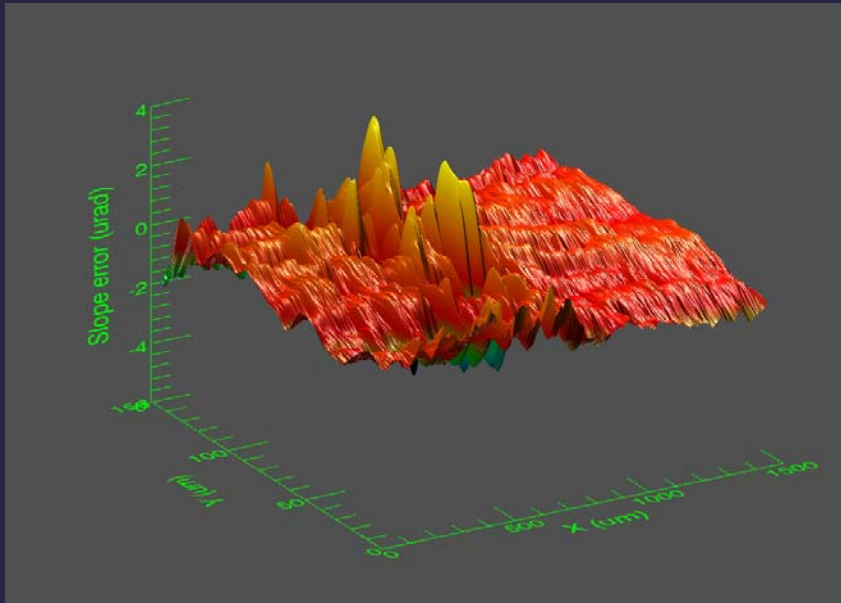
Mirror Length

Mirror Width



Data Processing

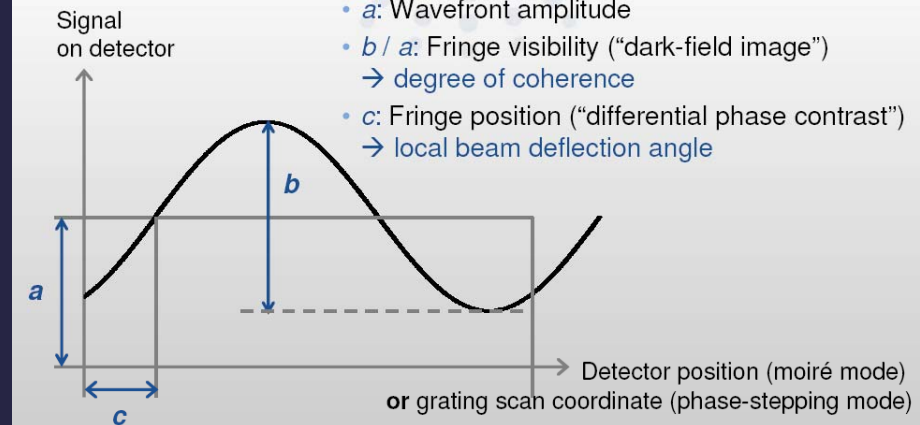
Phase Stepping



Signals extracted

Three types of information

- a : Wavefront amplitude
- b/a : Fringe visibility ("dark-field image")
→ degree of coherence
- c : Fringe position ("differential phase contrast")
→ local beam deflection angle



$$y = a_0 + b_0 \cos\left(\frac{2\pi}{d} x + \phi\right)$$

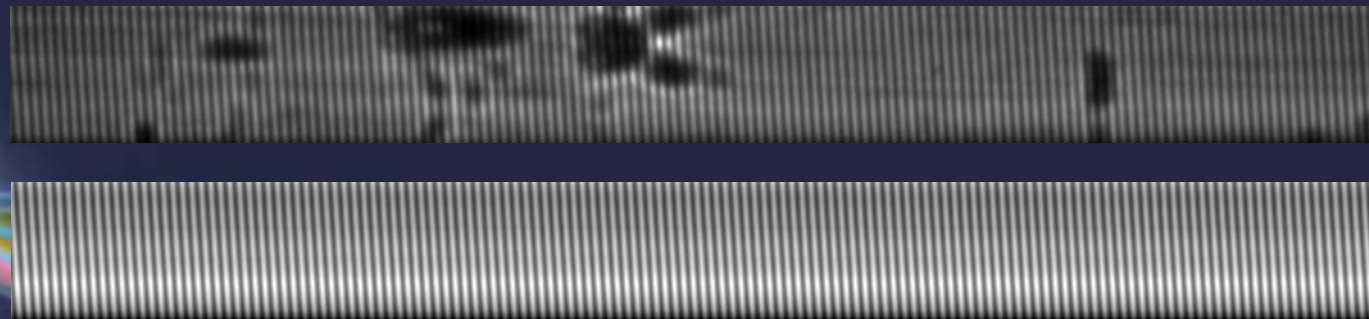
$$\delta = \frac{\alpha}{2} = \frac{d_2 \phi}{4\pi L}$$

Moiré Fringe

FFT

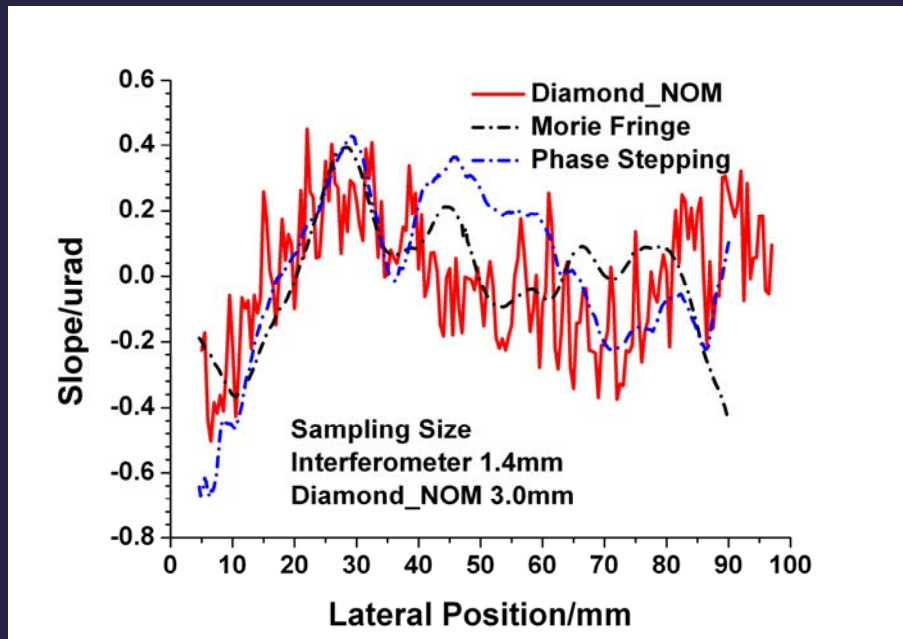
Mirror Length

Mirror Width

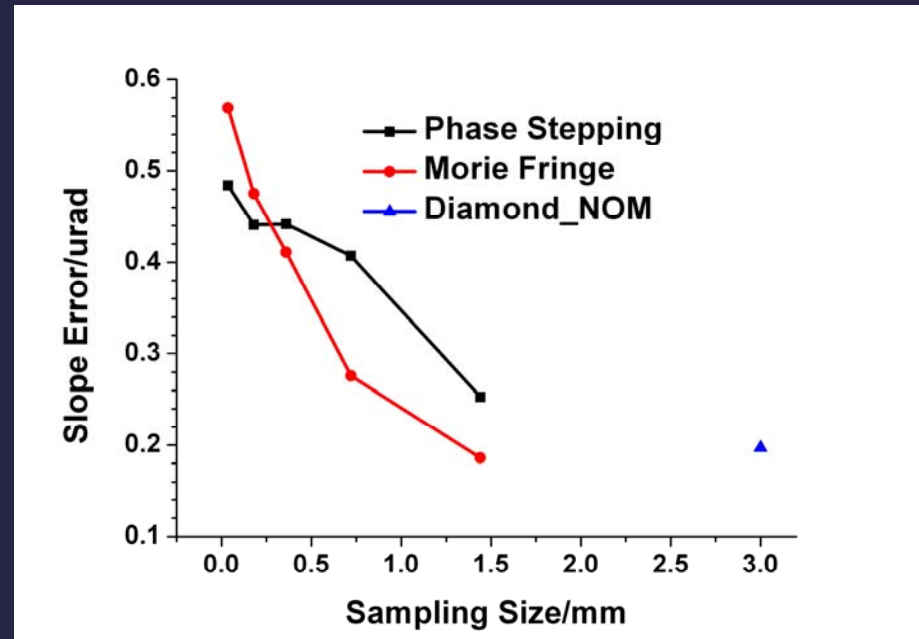


Plane mirror characterisation

Slope comparison



Slope Error vs. Sampling Size



Diamond_NOM test data from Simon Alcock

-1mm

0mm

1mm

Mirror Length

Mirror Width



H. Wang, et al. Paper is in preparation (2011)

Phase Stepping vs. Moiré Fringe Analysis

	Phase Stepping	Moiré Fringe Analysis
No. of Image	>3 [10 in our test]	1
FFT	Intensity vs. G2 position	Fringe position
Grating Divergence Match	Desirable	Not required
Resolution	One pixel	One fringe
Advantage	2D high resolution	Fast
Disadvantage	Time-consuming	One dimension

Summary and Outlook

- **Shearing interferometer has been developed at DLS B16**
- **Parabolic lens has been studied with phase stepping method**
- **Plane mirror was measured with shearing interferometer**
- **At-wavelength metrology in near future (Curved mirrors, Zone Plate, Multilayer Laue Lens (MLL)...)**
- **High resolution tests with 2D grating?**

Acknowledgements

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Thanks for your attention