

Single-nanometer focusing of hard X-rays using adaptive optical system



Current status of X-ray mirror development for coming coherent-X-ray

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Acknowledgement

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Background and today's contents

3rd generation SR facilities widely contribute to many S&T fields.
4th generation facility (XFEL) has already been here.

Highly brilliant X-ray is not particular, now.



How should mirror optic contribute to coherent X-ray optical system?

Current research targets

1. Focusing down to sub-10nm (including brief introduction of sub-50nm focusing)
2. Full-field, achromatic and high-resolution imaging of incoherent X-rays
3. Focused and full coherent X-ray illumination for diffraction microscopy

Required accuracy for nano-focusing under D-limited condition

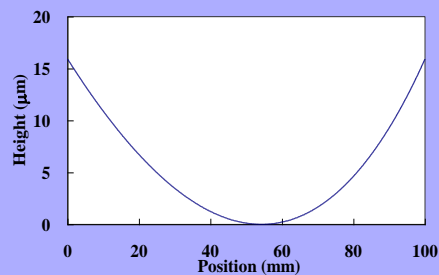
Kirkpatrick-Baez mirrors

Elliptical mirror $\times 2$

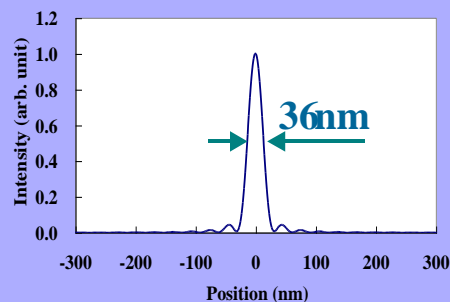
Diffraction-limited focusing

Waves are in constructive interference state.

$$\text{Phase error} = \frac{2d \sin \theta}{\lambda} \text{ wave}$$



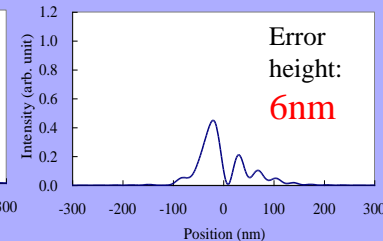
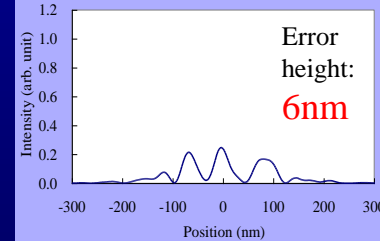
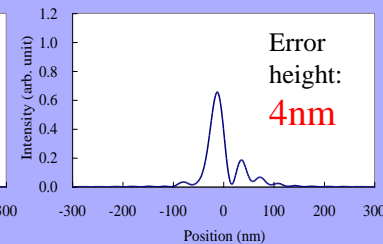
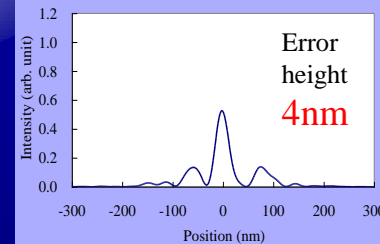
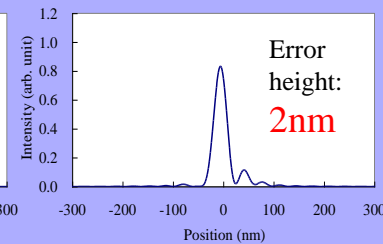
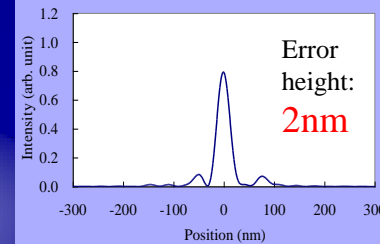
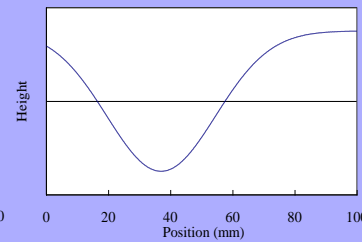
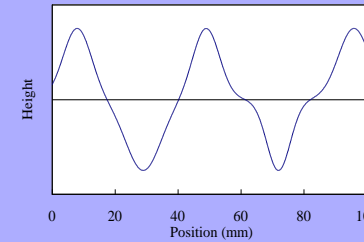
Designed profile (ellipse)



Beam profile

40mm < L_s < 50mm

100mm < L_s



© Plasma CVM (chemical vaporization machining)

→ Rough figuring (Rapid figuring with 10nm (P-V) level accuracy)

K. Yamamura et al., Rev. Sci. Instrum. 71 (2000), 4627

© EEM (elastic emission machining)

→ Final figuring and smoothing (Fine figuring with atomically smoothing)

K. Yamauchi et al., Rev. Sci. Instrum. 73 (2002), 4028

© MSI (microstitching interferometry)

→ Figure tester with spatial resolution close to 0.01mm

K. Yamauchi et al., Rev. Sci. Instrum. 74 (2003), 2894

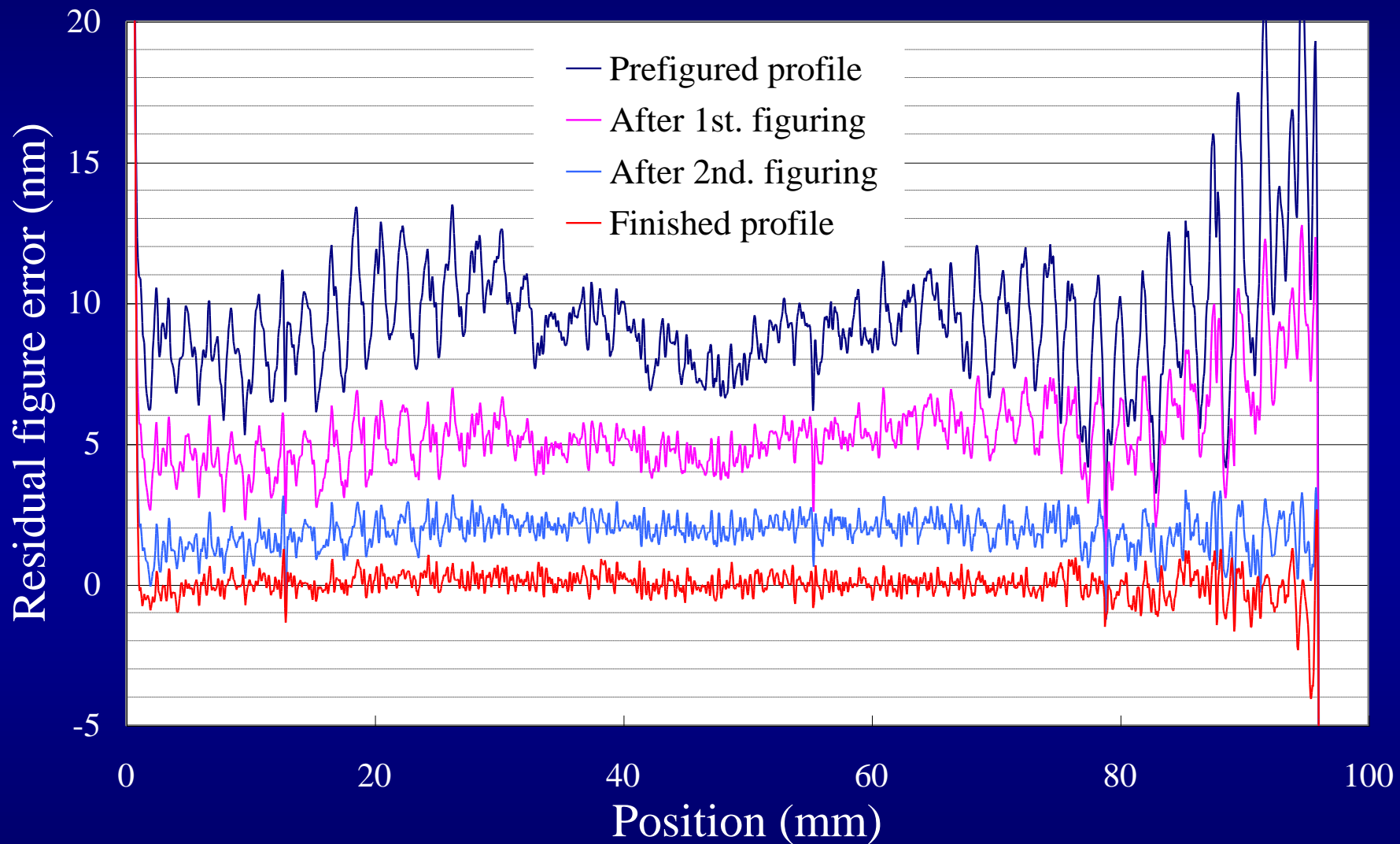
© RADSI (relative-angle determinable stitching interferometry)

→ Figure tester for steeply curved ellipse of large NA mirror

H. Mimura et al., Rev. Sci. Instrum. 76 (2005), 045102

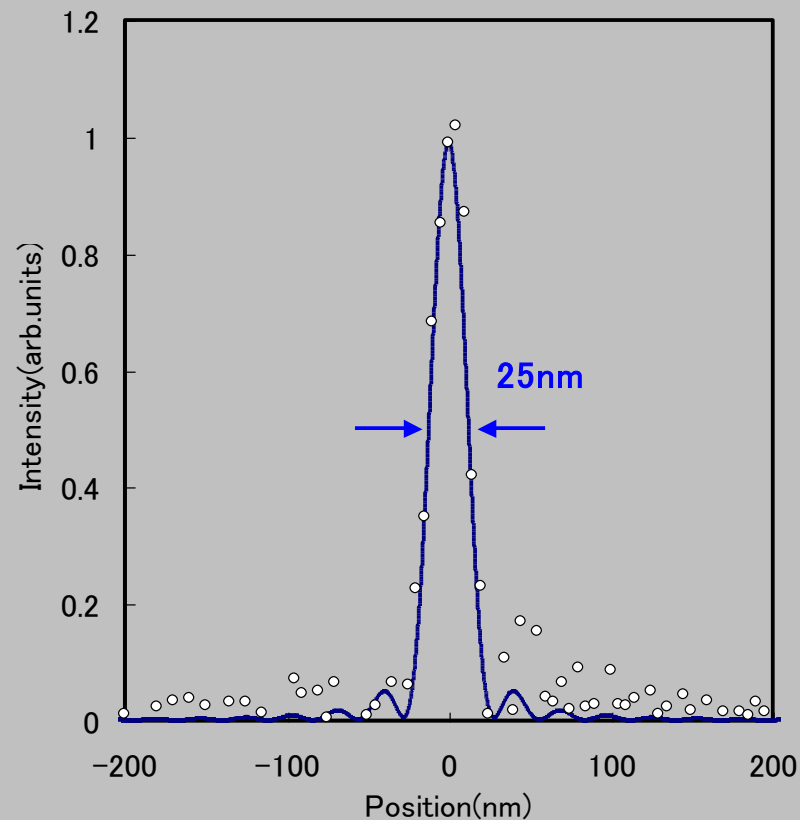
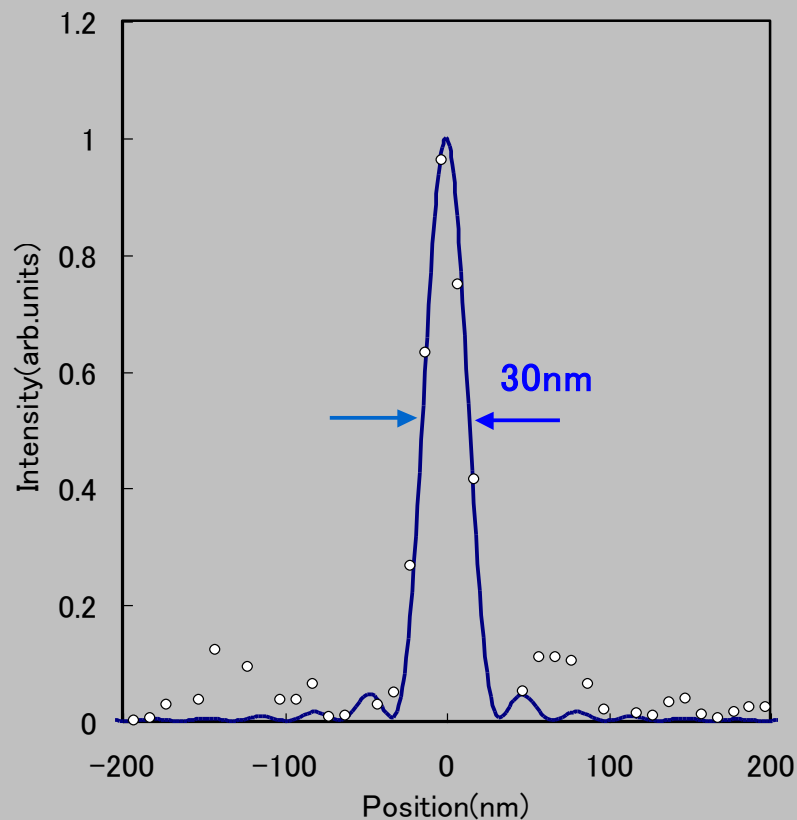
JTEC URL <http://www.j-tec.co.jp>

Typical deterministic figuring properties using EEM



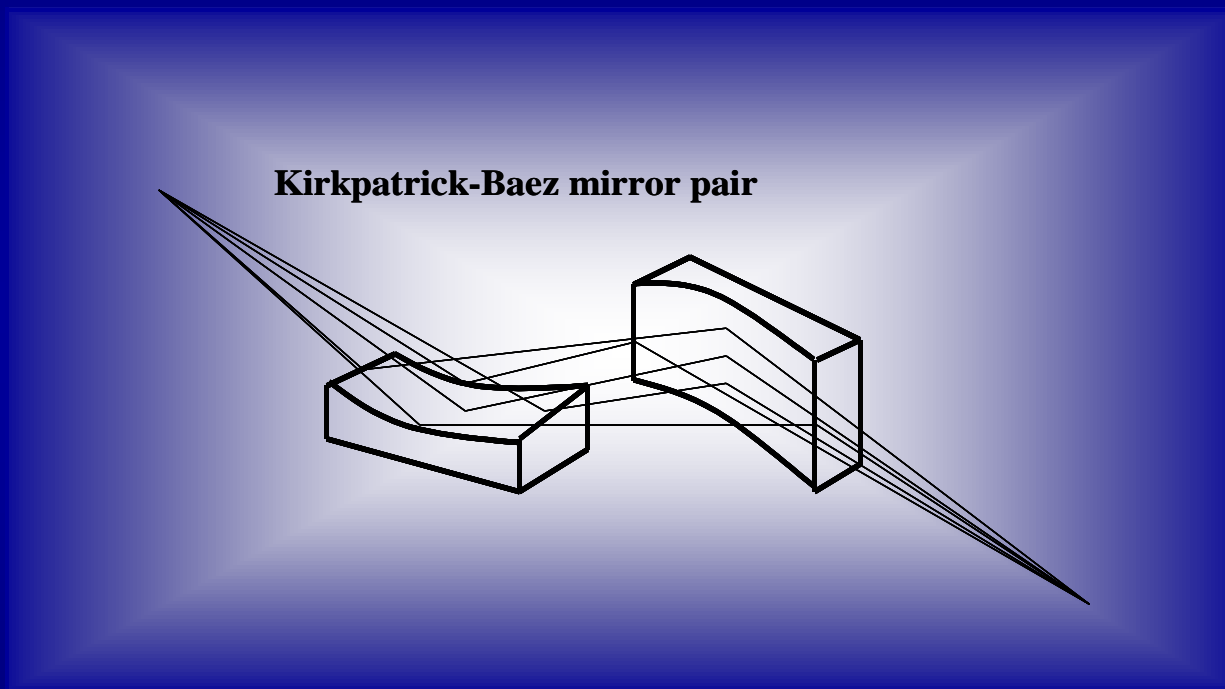
Sub-30nm focusing (2006)

Smallest size in hard-X-ray realized by total reflection achromatic mirror optics (focusing under diffraction limited condition)

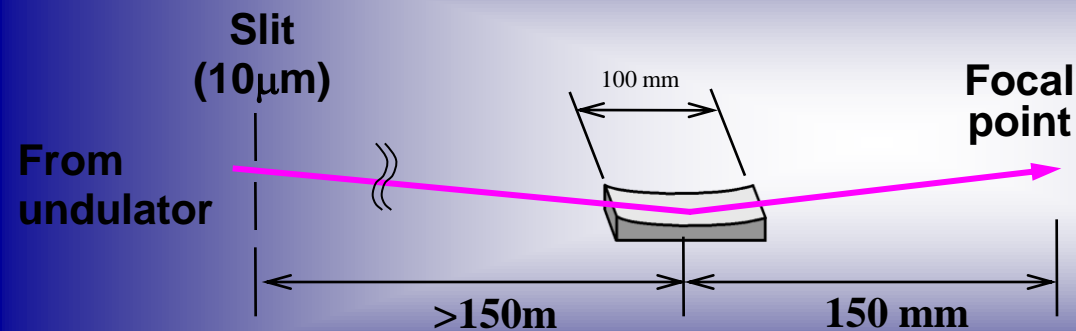


Mimura et al., APL (2007)

“Hard-X-ray sub-10nm focusing and realization of high-resolution X-ray microscopy”



To realize Sub-10nm focusing K-B mirrors

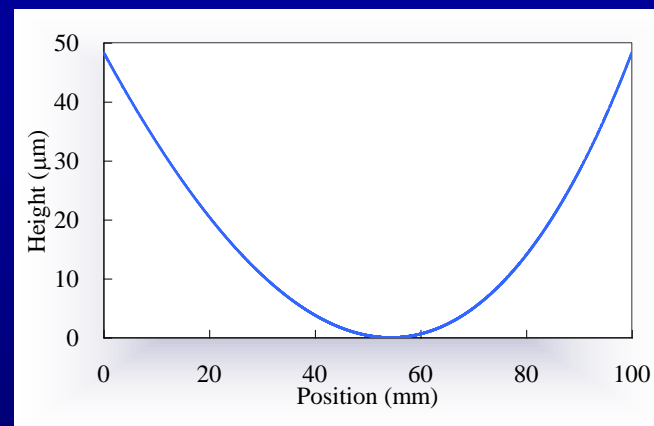
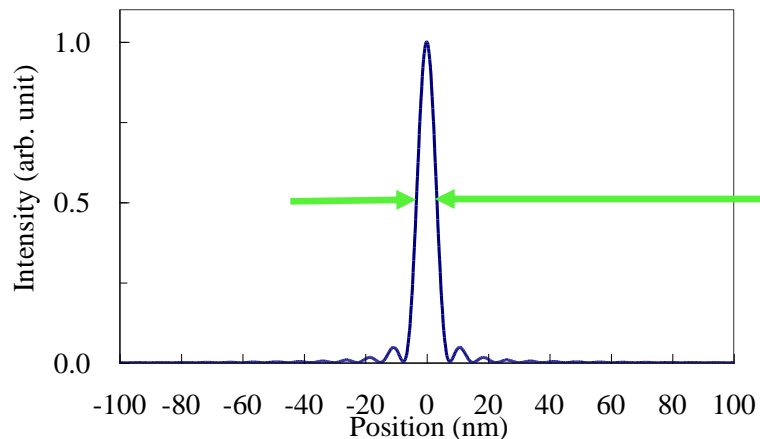


X-ray energy : 20keV

Focal length : 150mm

Acceptance width : 1.1mm

Incidence angle : 11.1mrad



MSI with RADSI and EEM can prepare the surface figure with 1nm (P-V) accuracy.

Estimation of required accuracy

@20keV Mirror length: 100mm, Focal length: 150mm

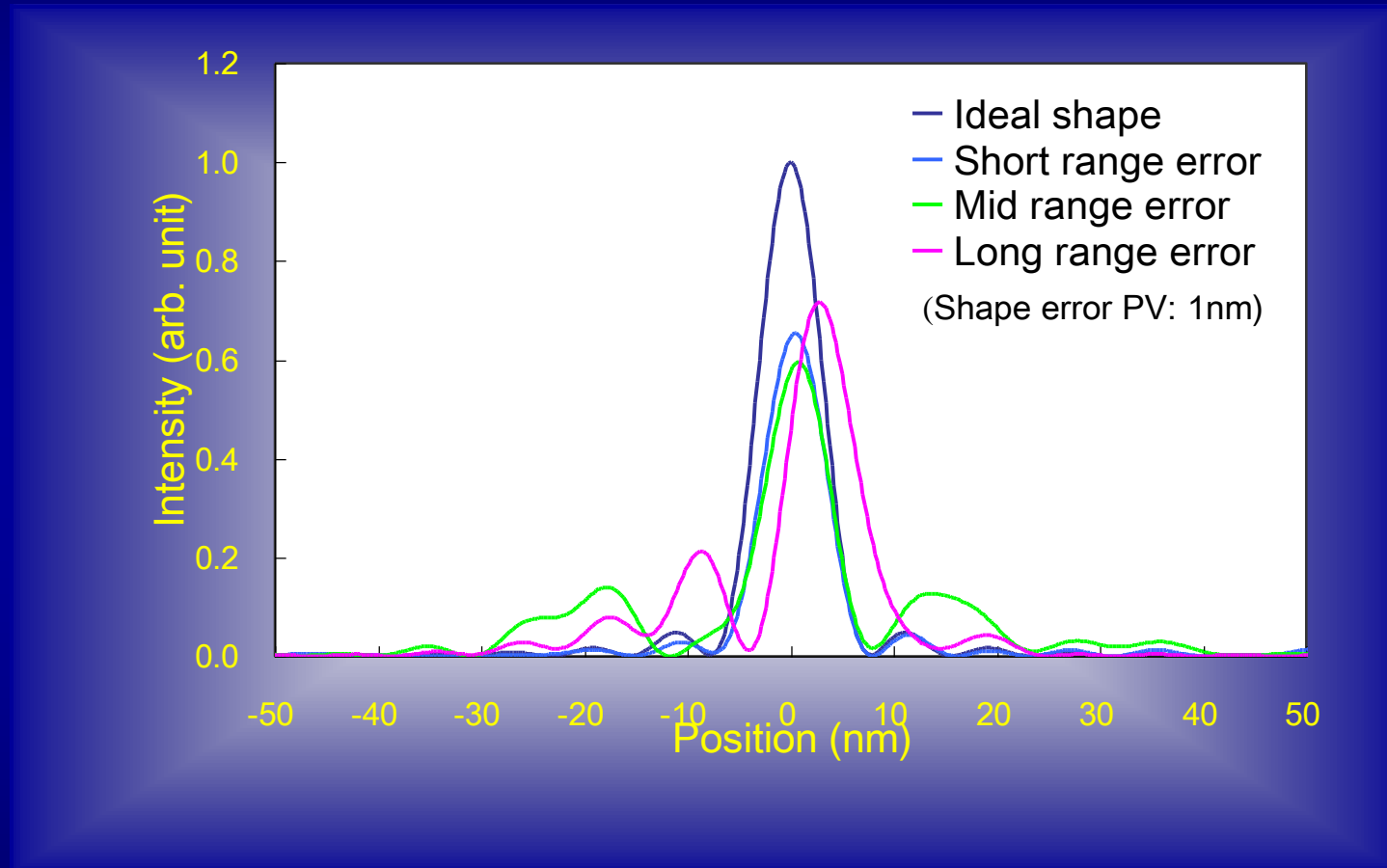
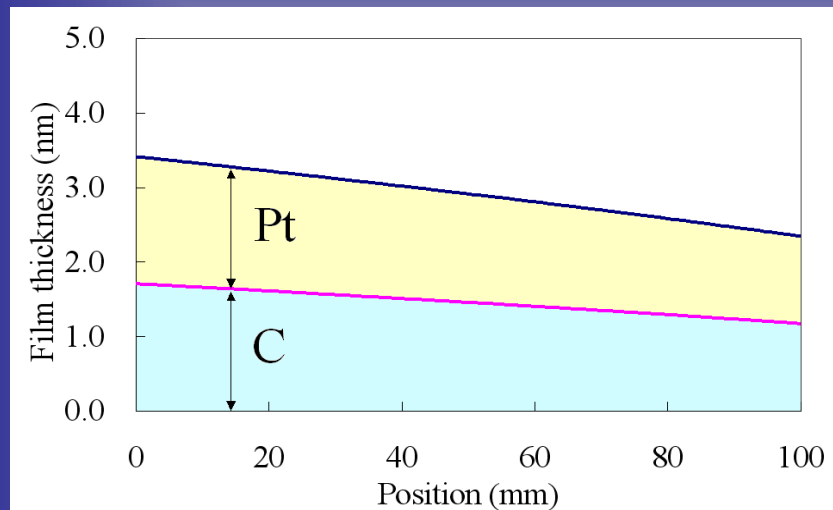
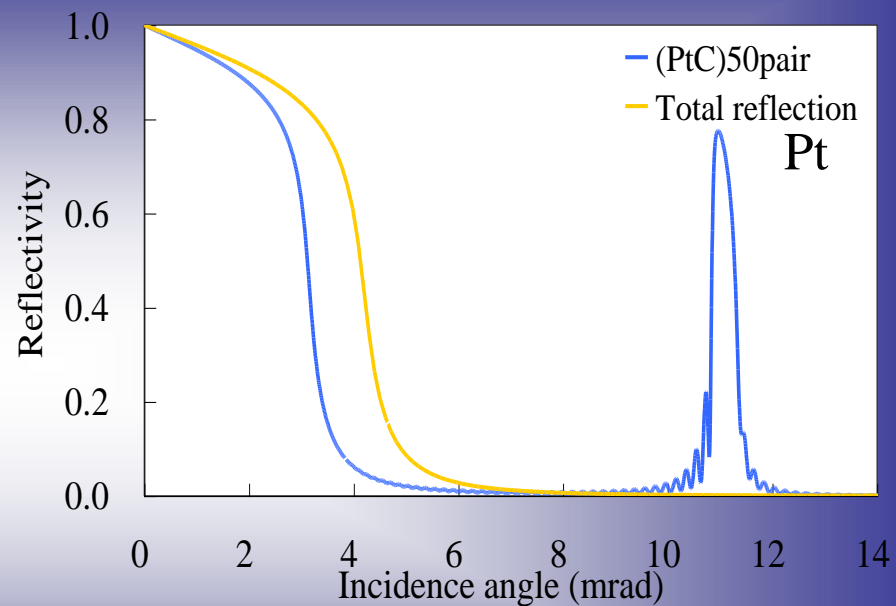


Figure error of 1nm is not allowable

Multi-layer technology is needed to realize large NA



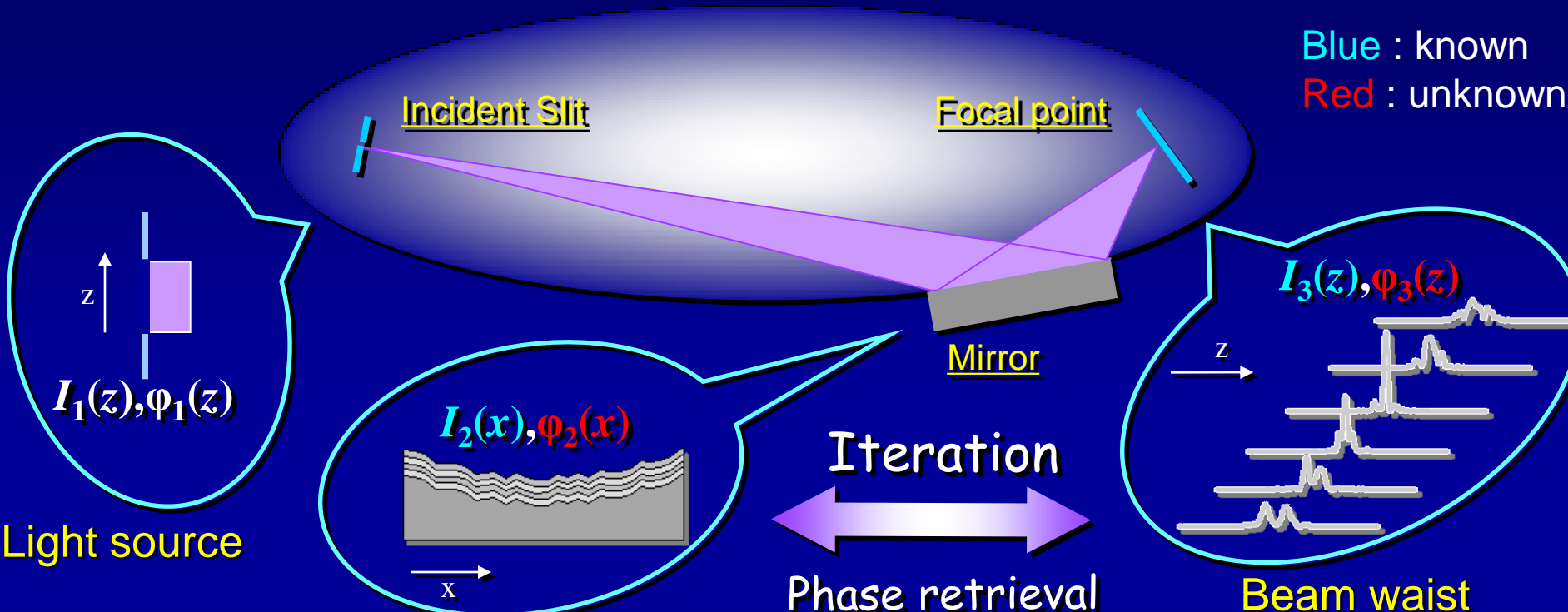
Graded multi-layer



Reflectivity

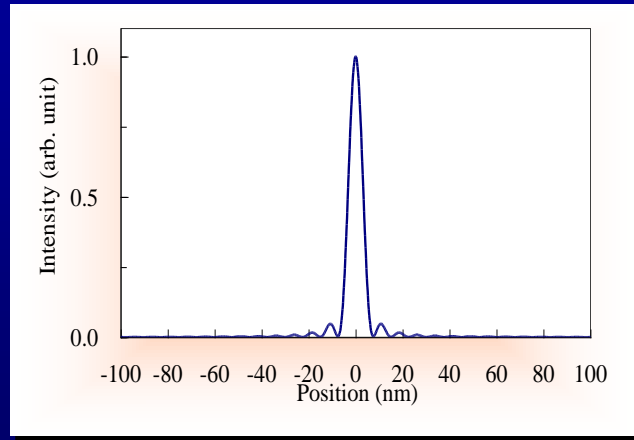
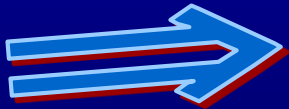
Not only figure error but also thickness deviation of the multilayer induce wavefront phase error.

At-wavelength phase-retrieval interferometry



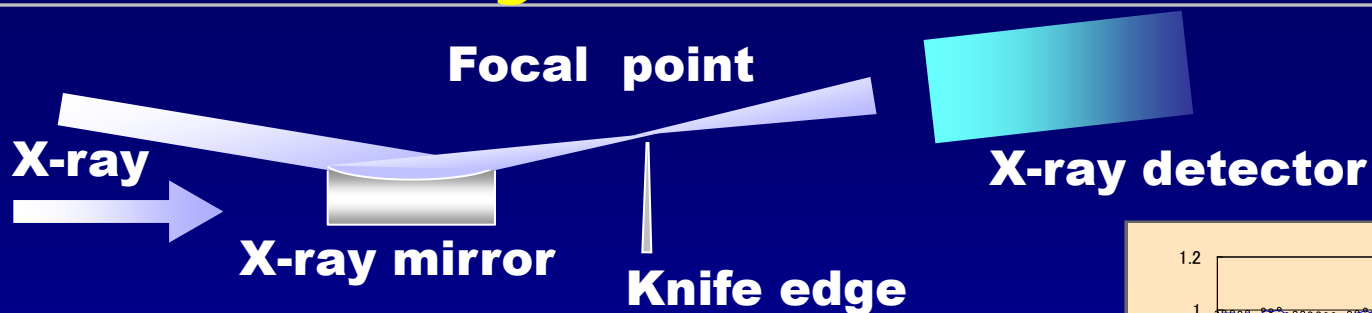
Mirror surface
(Phase error includes surface figure and ML thickness errors)

Phase error compensation



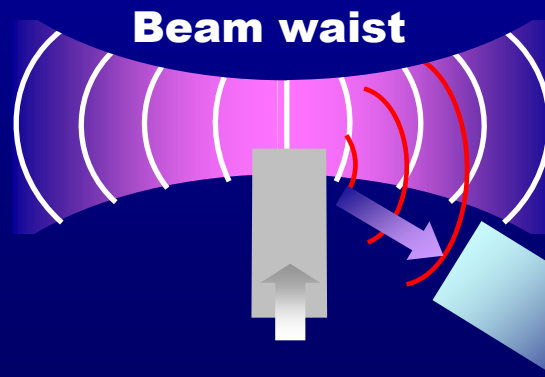
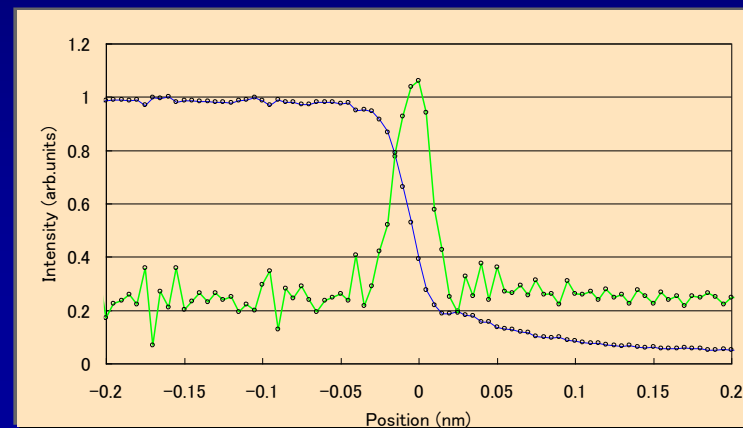
K. Yamauchi,
SPIE's Optics and Photonics 2005

New knife-edge method



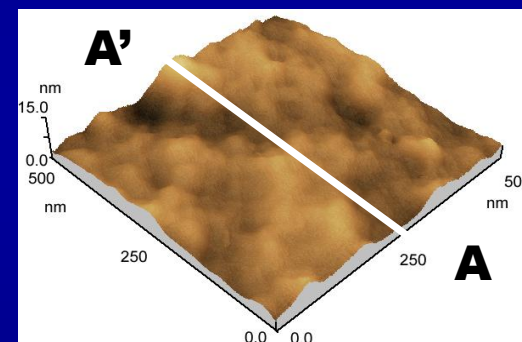
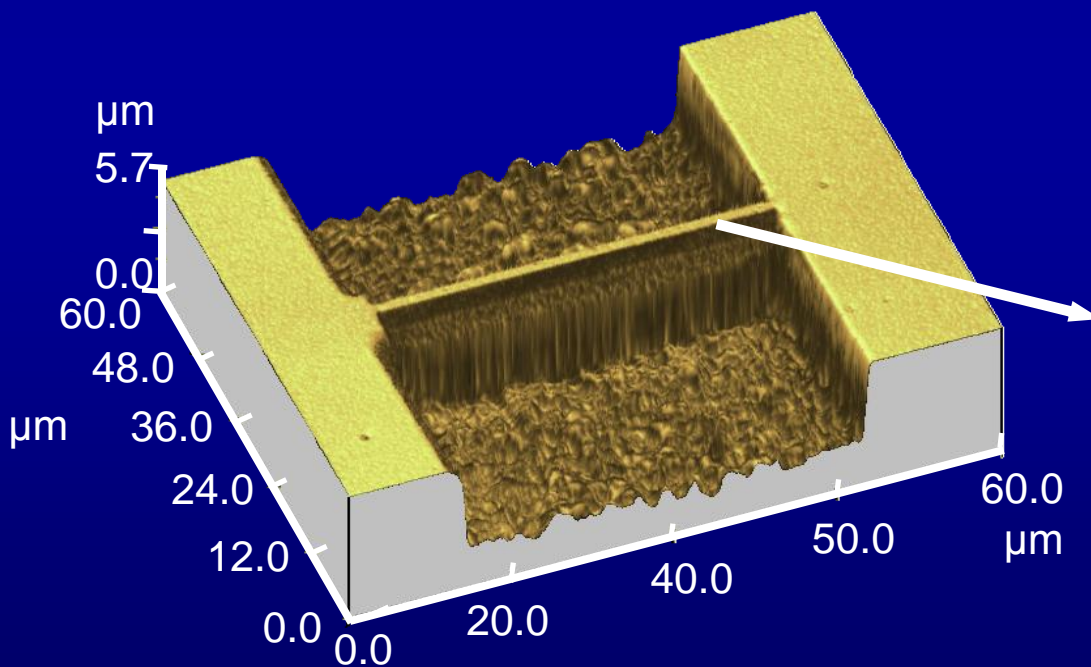
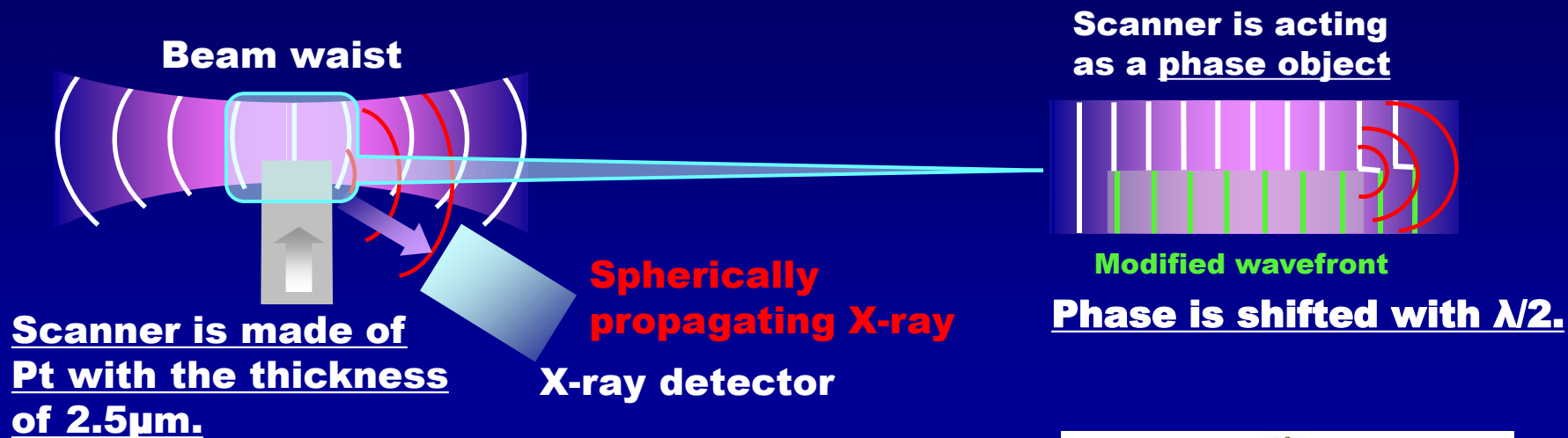
Conventional knife-edge method

New method

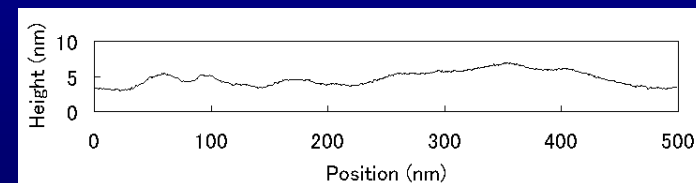


Mimura et al.
 Phys. Rev. A (2008)

Details of the new knife-edge method

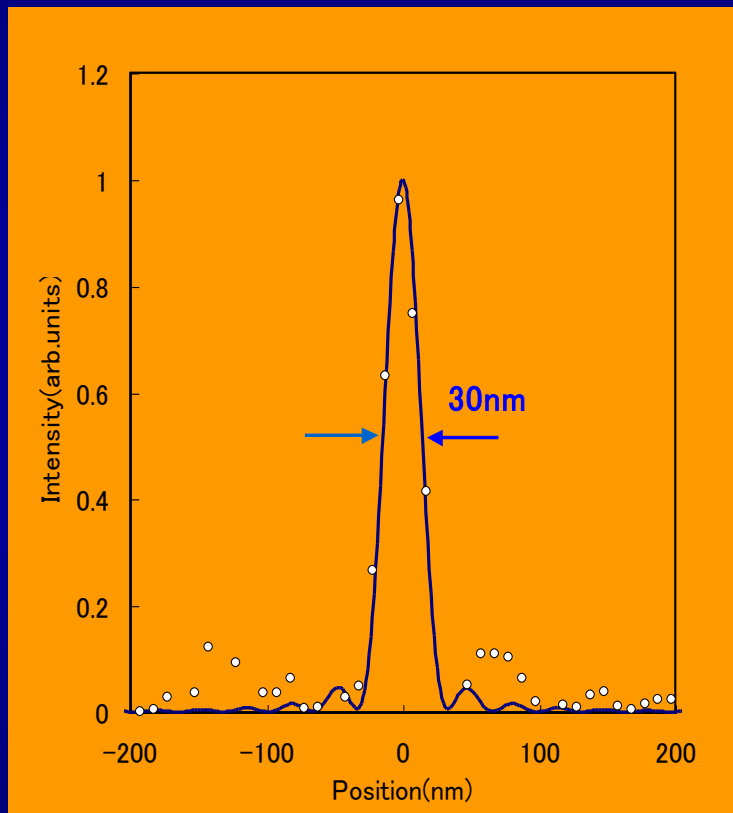


Microroughness at the bridge



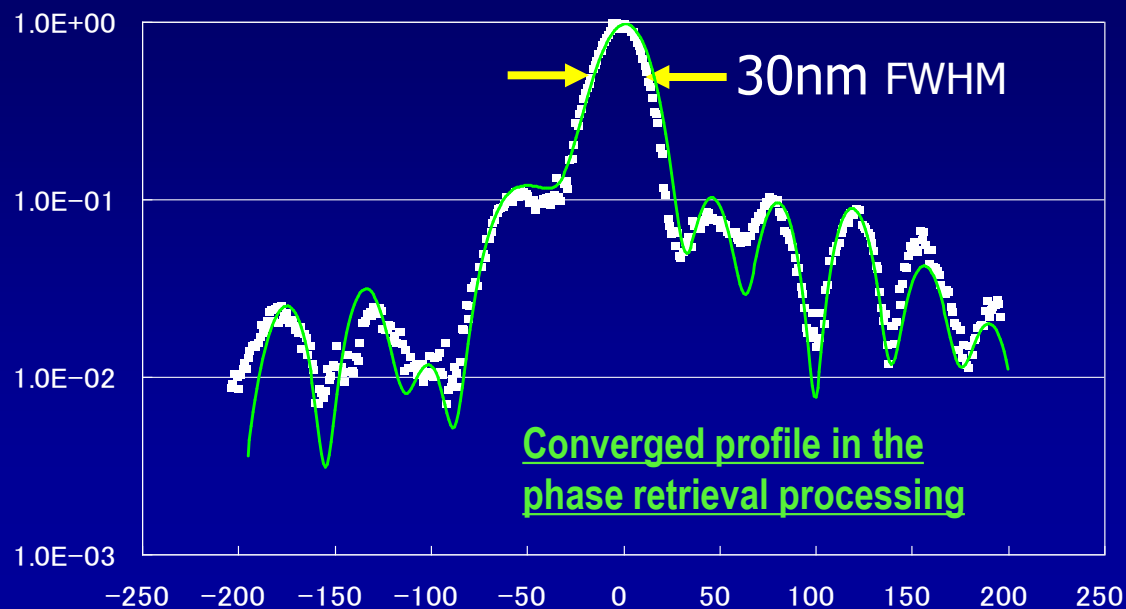
A-A' profile

30nm-focusing mirror was employed for a demonstration of the proposed at-wavelength measurement

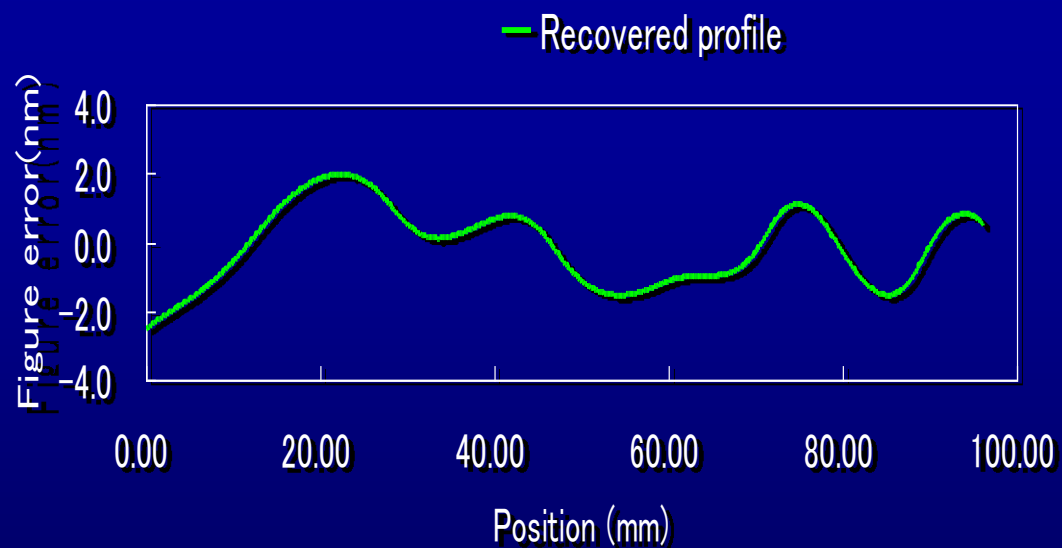


- Not a multilayer optic.
- Surface is coated by Pt.

Performance of phase retrieval



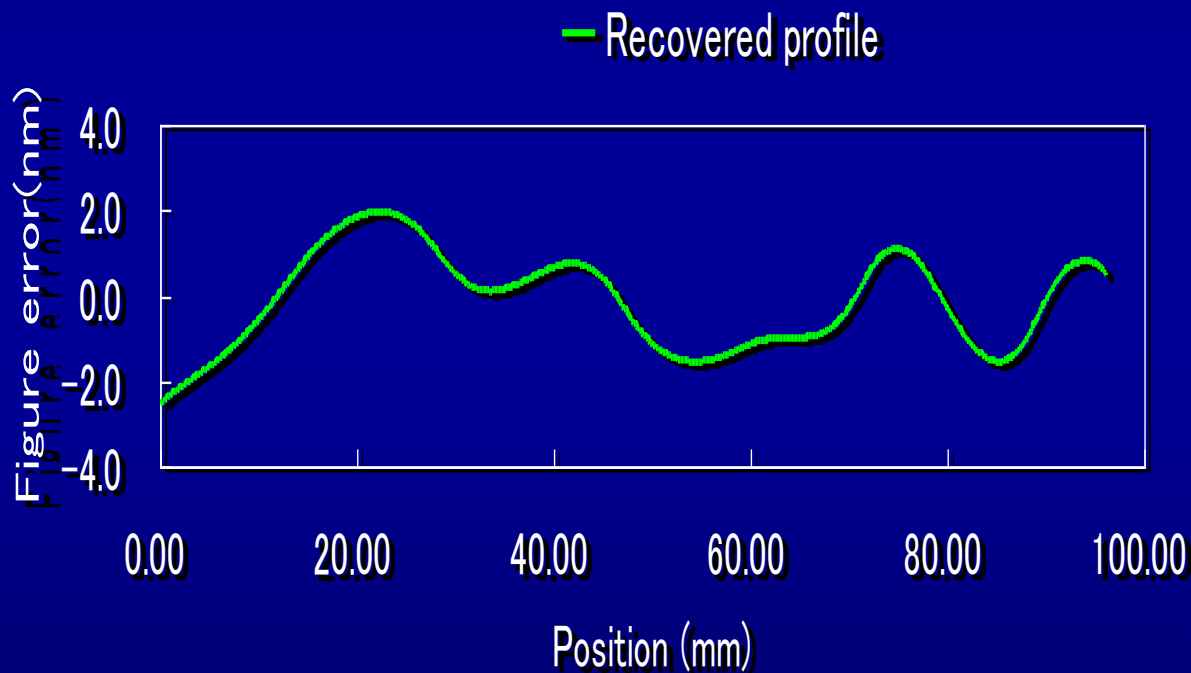
Measured beam profile



Mimura et al.
Phys. Rev. A (2008)

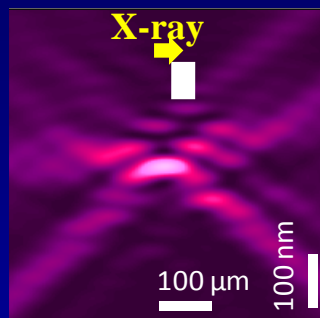
Verification

To verify the reliability of the recovered phase error profile, we actually refigured the mirror by differential deposition method (G. Ice) using the recovered profile.

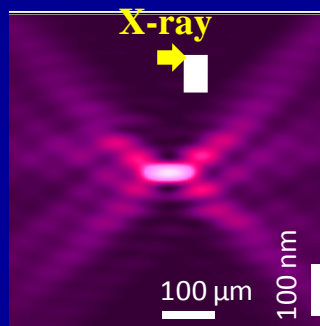


Focused beam profiles before and after DD

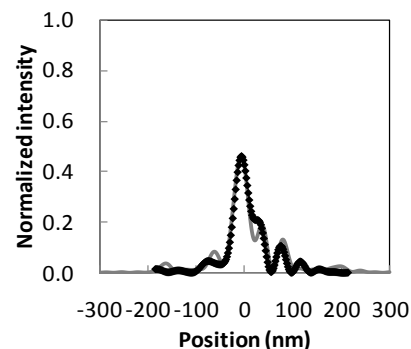
Before DD



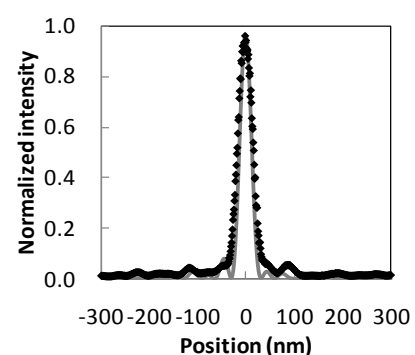
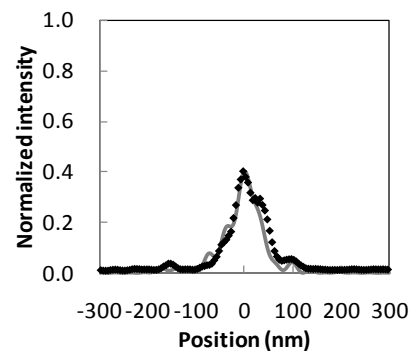
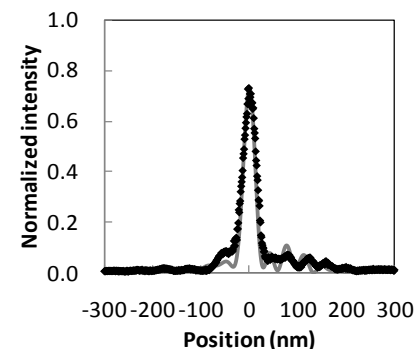
After DD



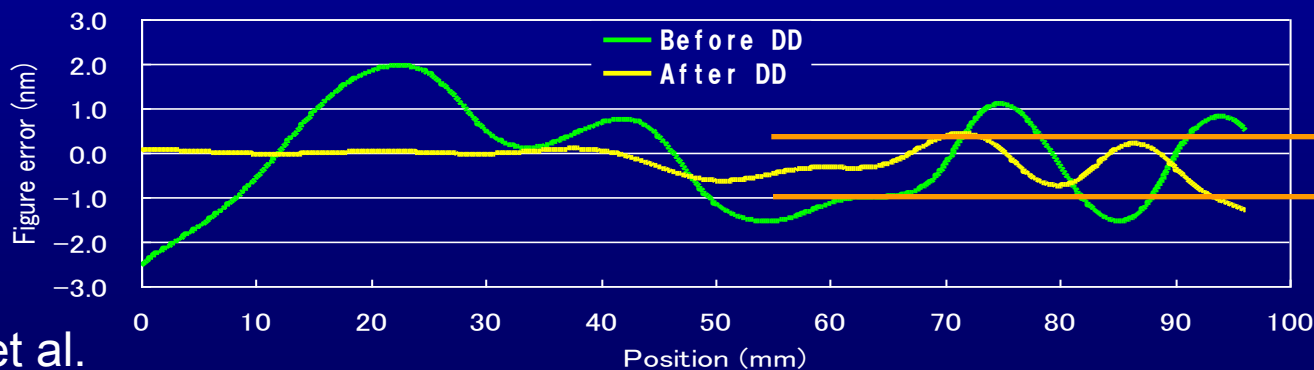
@50 μm upstream



@focal plane



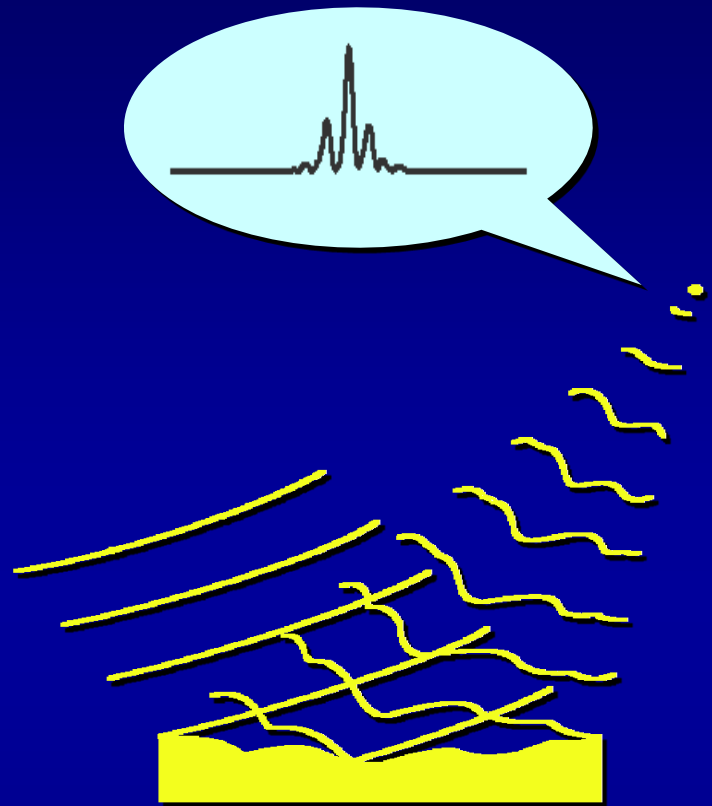
Comparison between the wave fields before and after phase compensation



Handa et al.

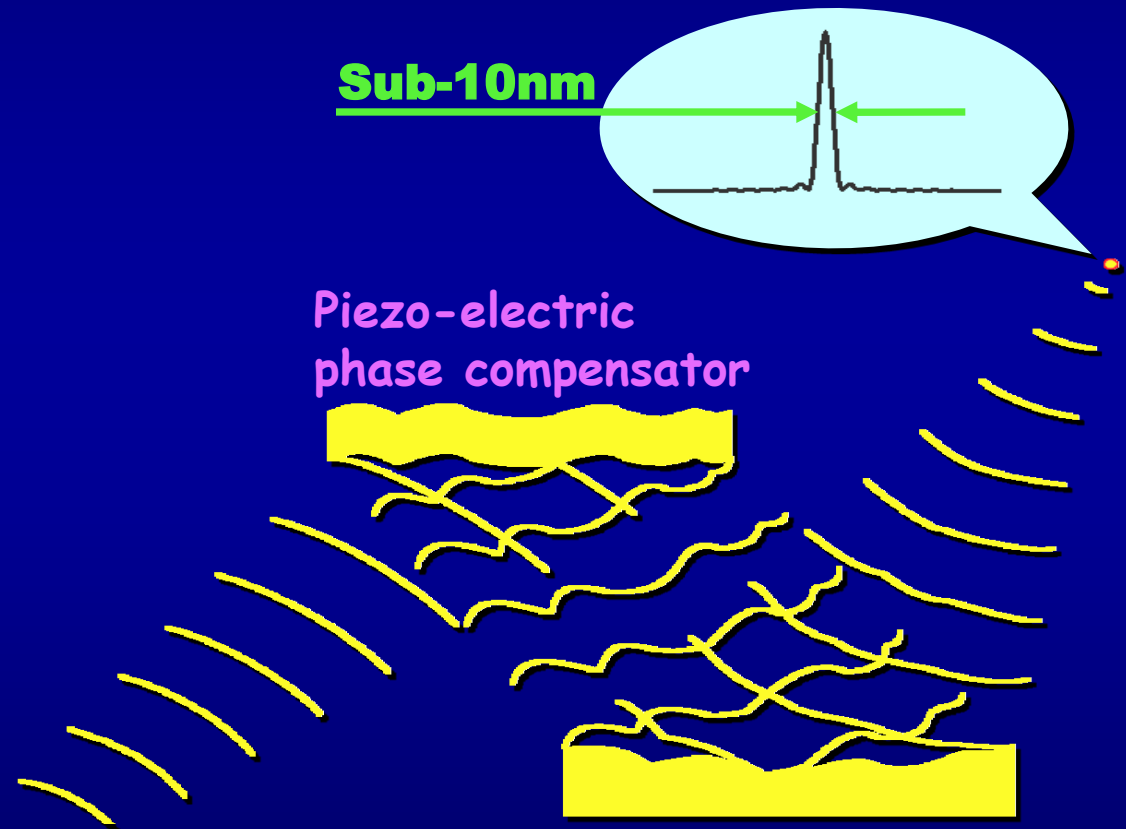
SIA(2008)

On-line compensation of wavefront



Focusing mirror with phase error

In-situ phase compensation

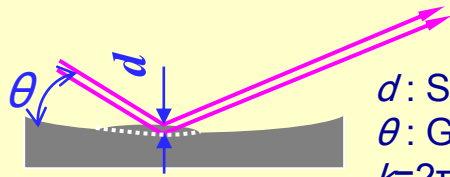


Piezo-electric
phase compensator

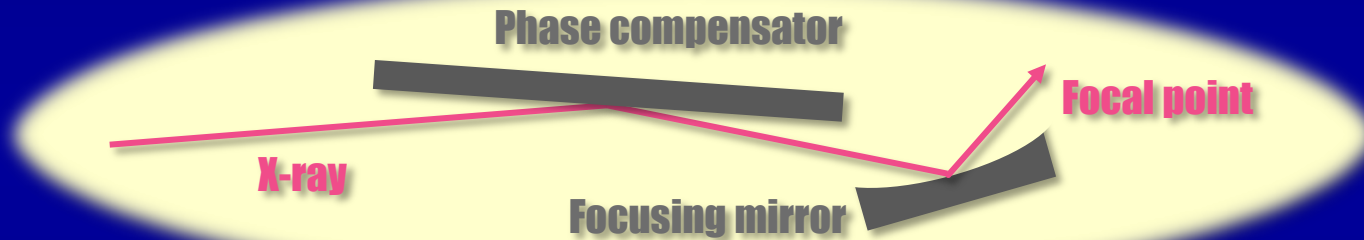
Focusing mirror with phase error

Design concept

$$\text{Phase error} = 2kd \sin \theta$$



d : Shape error
 θ : Glancing angle
 $k=2\pi/\lambda$: Wave number

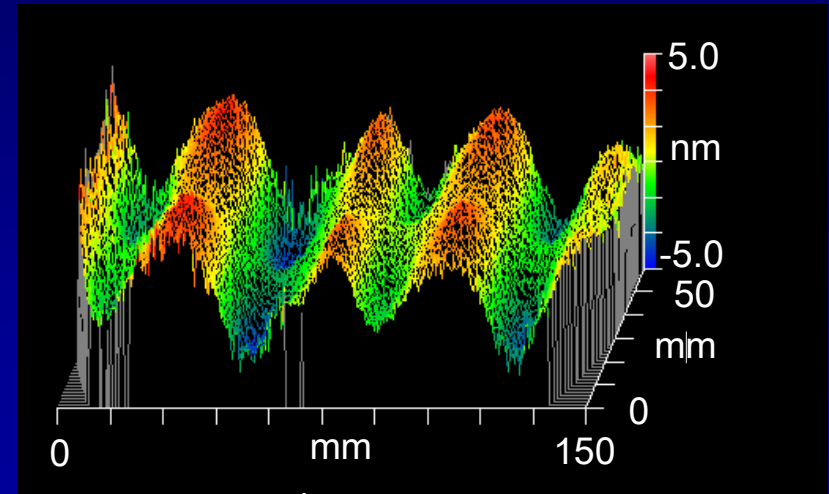
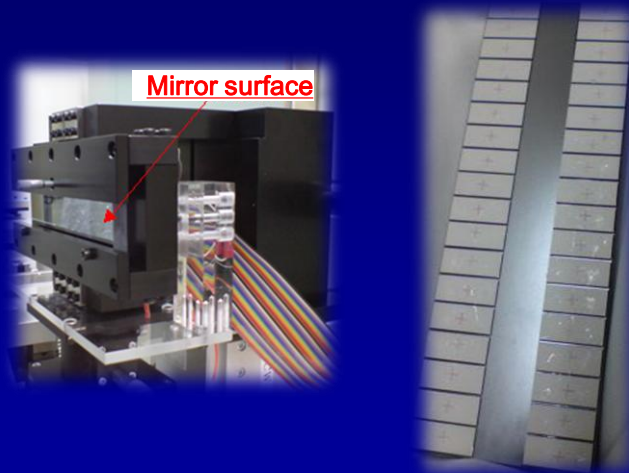


- ★ Glancing angle of compensator mirror is N times smaller.
 (However, Consequently the length of the compensator becomes longer)

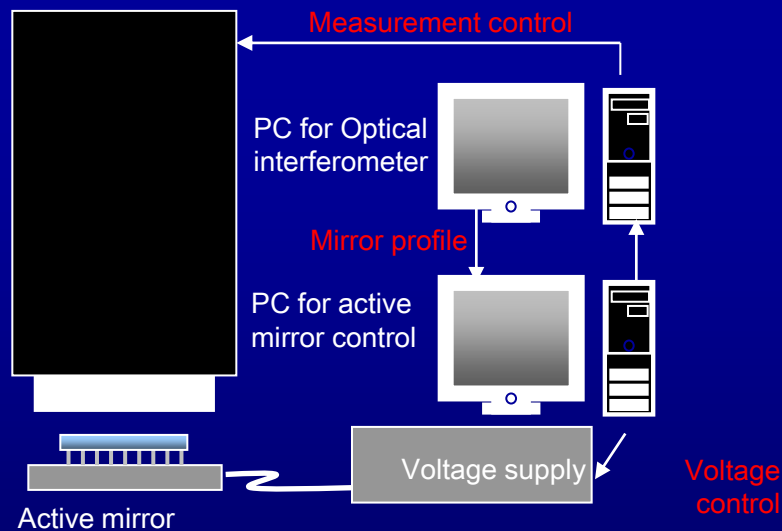


Required figure accuracy of the compensator mirror becomes N times lower.

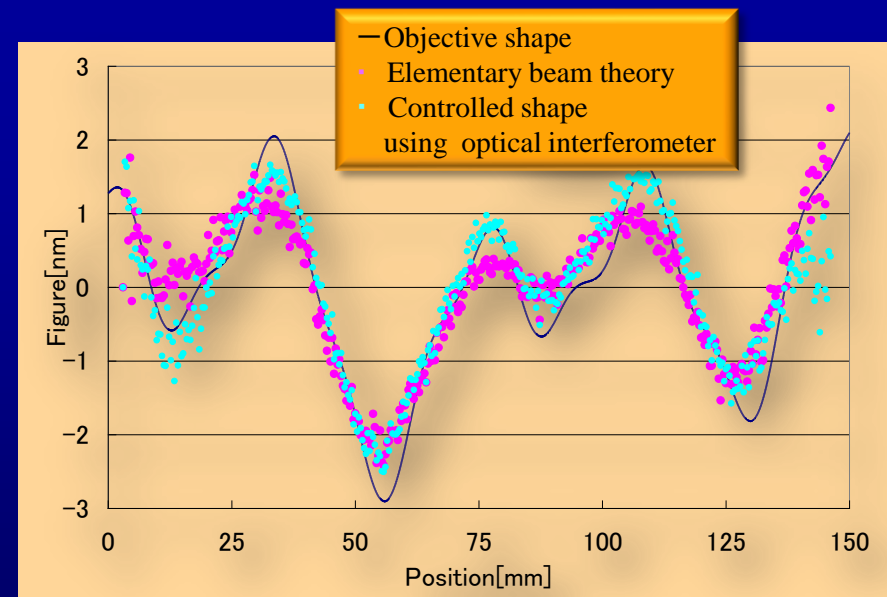
Phase compensator

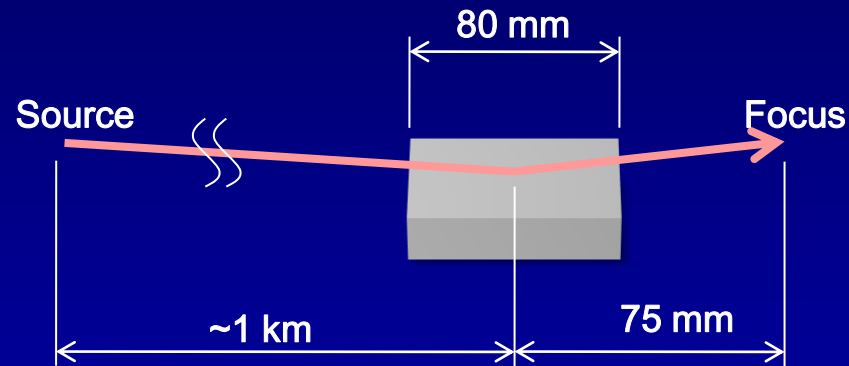


Optical interferometer



Feedback system





X-ray energy : 20 keV
Mirror length : 80 mm
Focal distance : 75 mm
Glancing angle : 7.0 mrad
Multilayer material : [Pt/C]₂₀
Substrate material : quartz glass

$$\Lambda = \frac{\lambda}{2\sqrt{n^2 - \cos^2 \theta}}$$

Λ : d-space

λ : X-ray wavelength

n : Index

θ : Glancing angle



EEM Machine

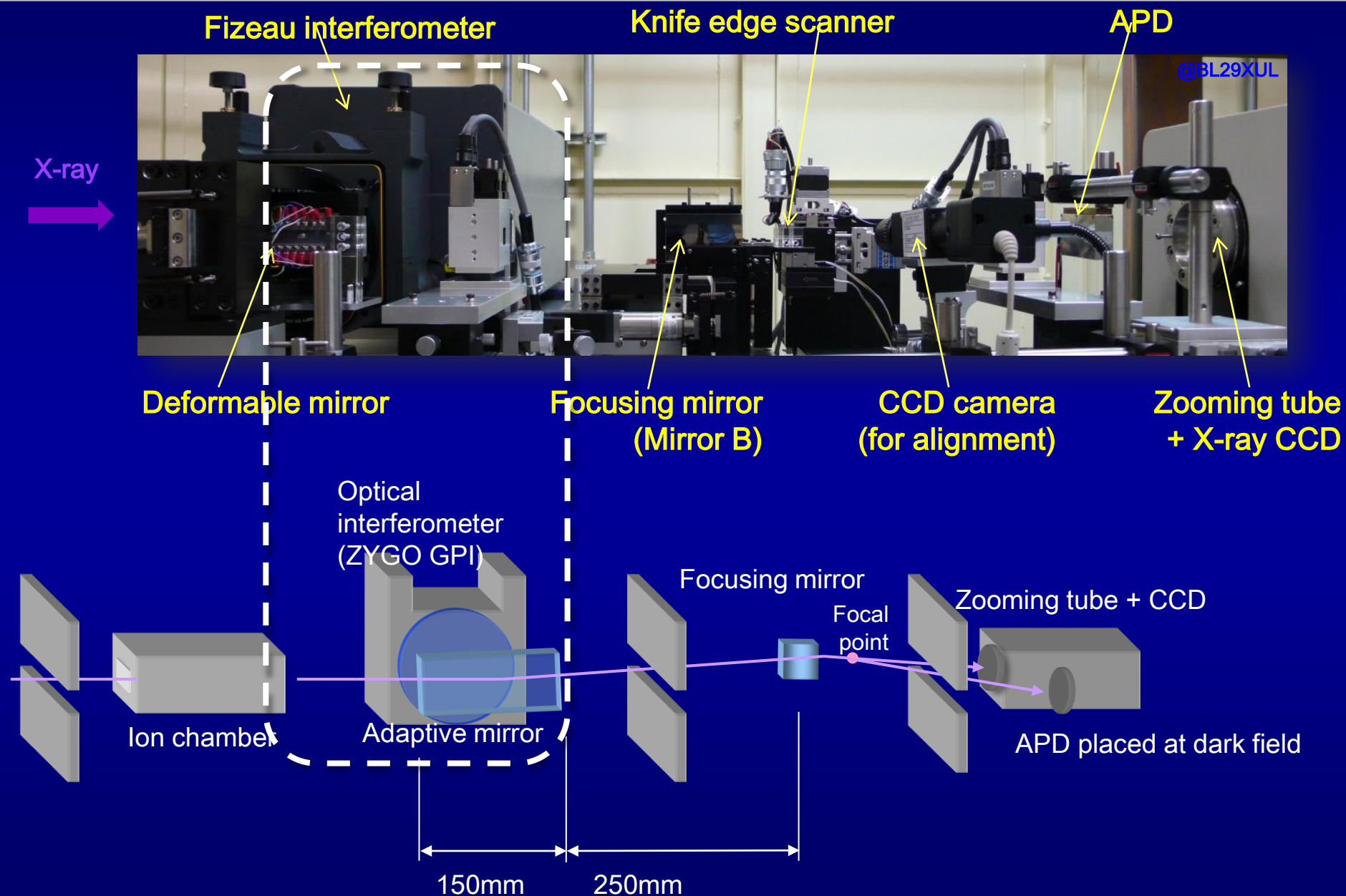


Micro- and RAD- Stitching
Optical Interferometry

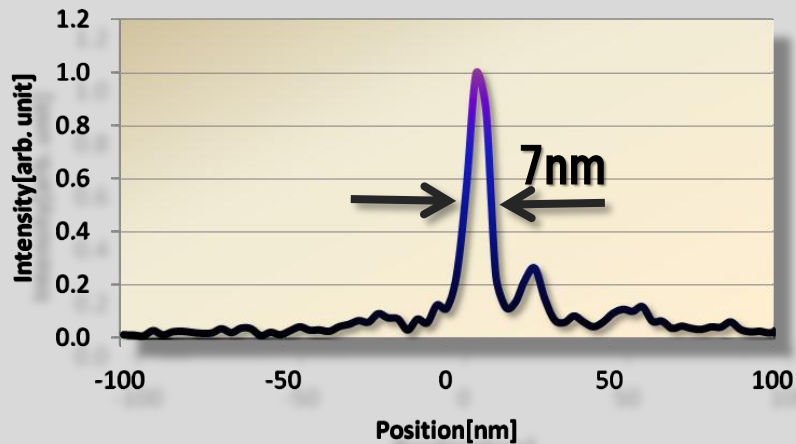


Laterally-Graded
Multilayer Coater

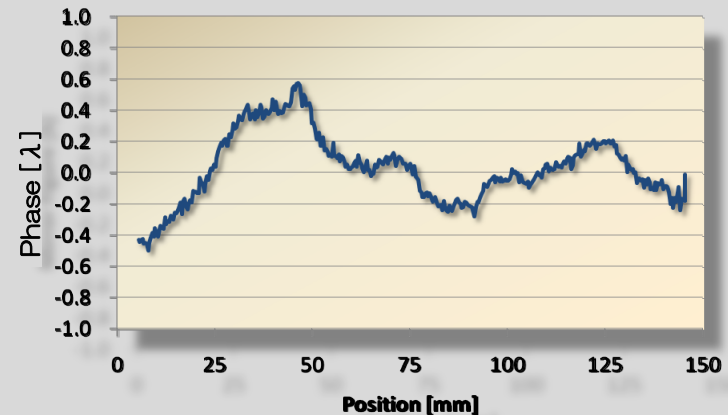
Optical configuration for active phase compensation



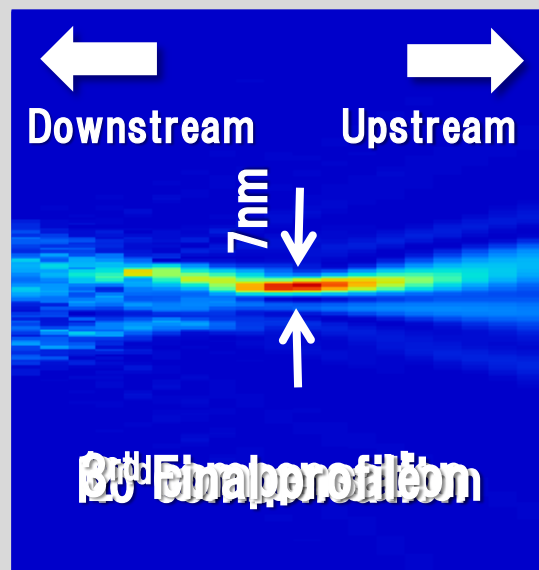
Sub-10nm focusing by using phase compensator



Profile at focal point



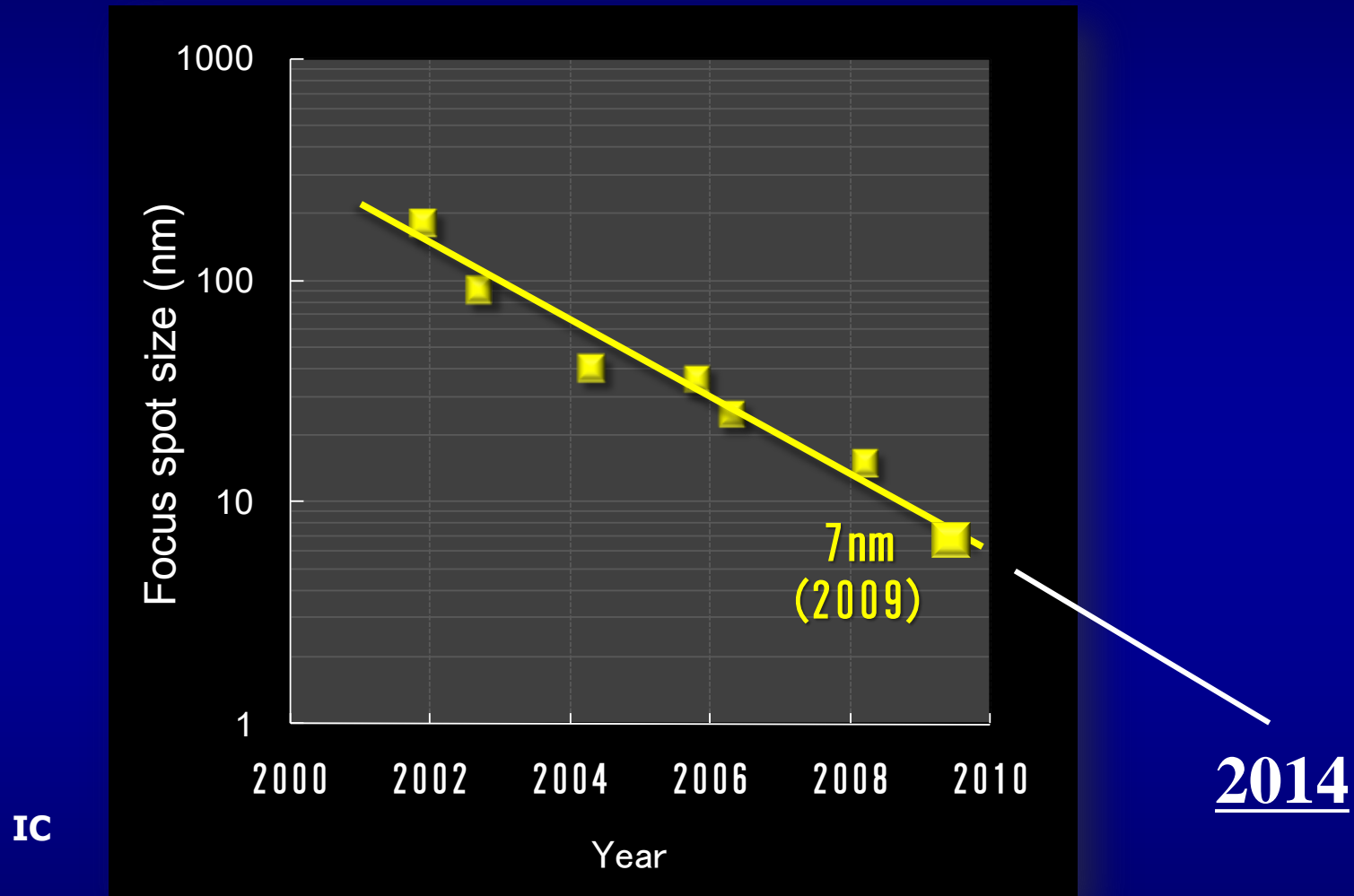
Compensated phase profile
(shape of compensation mirror)



Maximum phase compensated here was $\lambda/2$.
 λ was 0.06 nm.

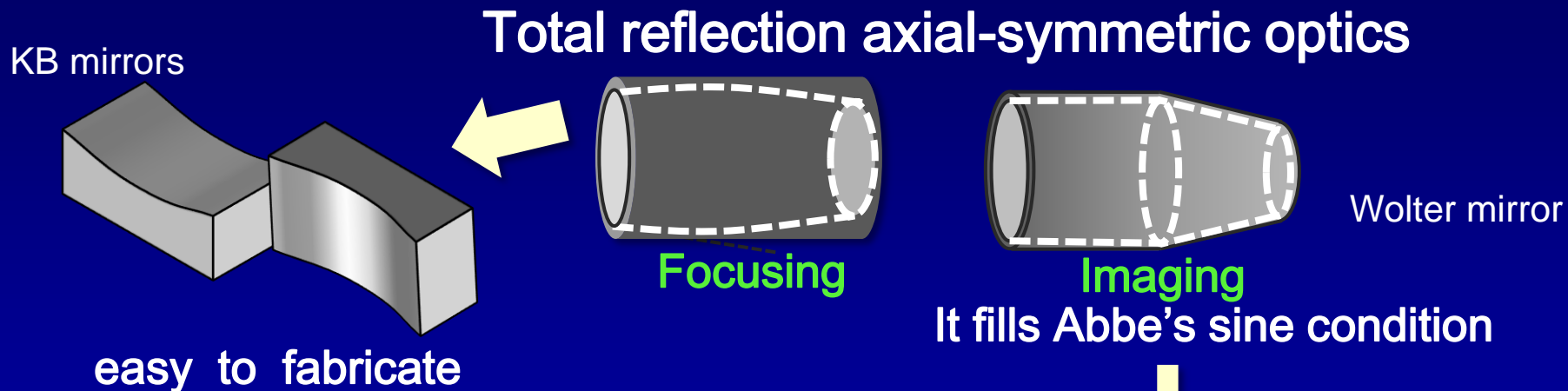
Beam waist structure

Nature Phys, (2010)



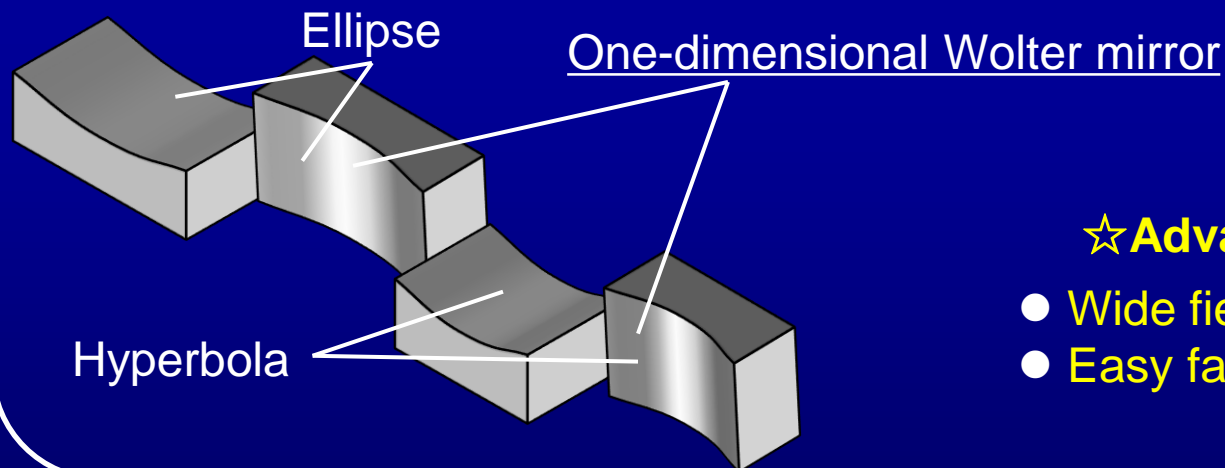
This is the smallest light beam human-made.

Achromatic imaging device (AKB Mirrors)



Advanced Kirkpatrick-Baez mirrors

R. Kodama et al., *Optics Letters* 21 (17), 1321-1323 (1996).



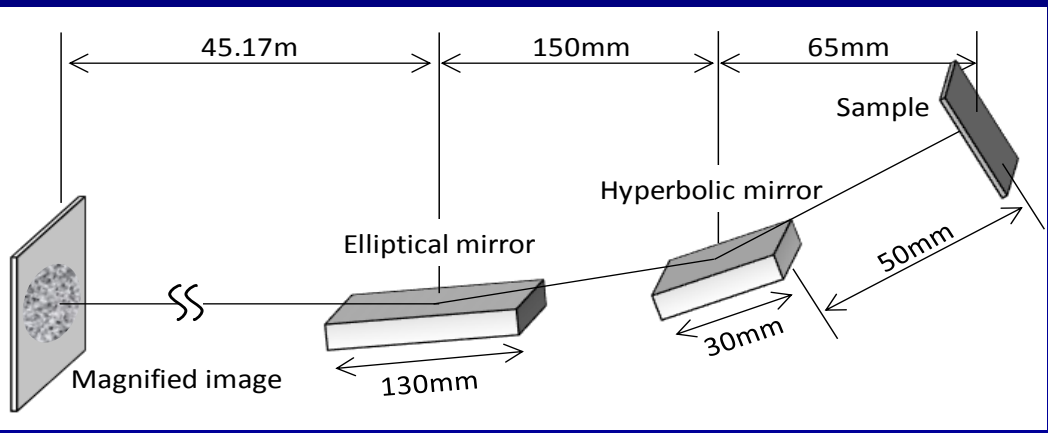
★ Advantage

- Wide field of view
- Easy fabrication

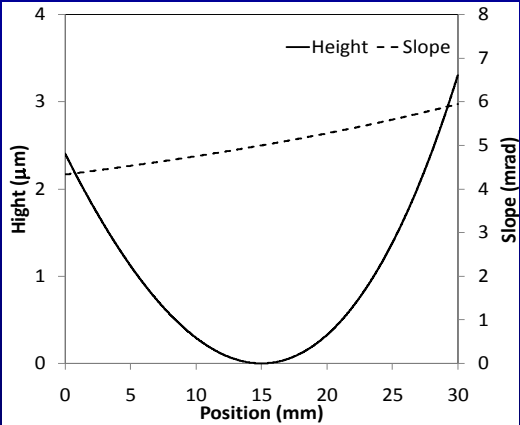
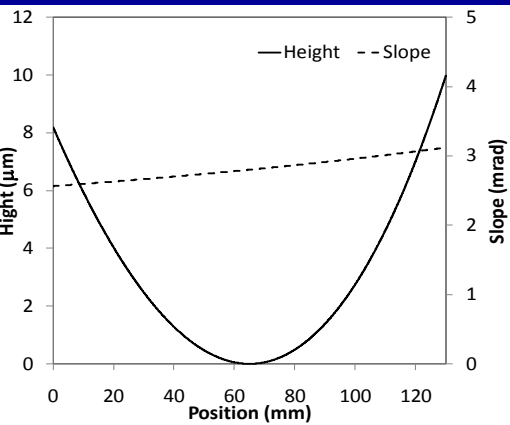
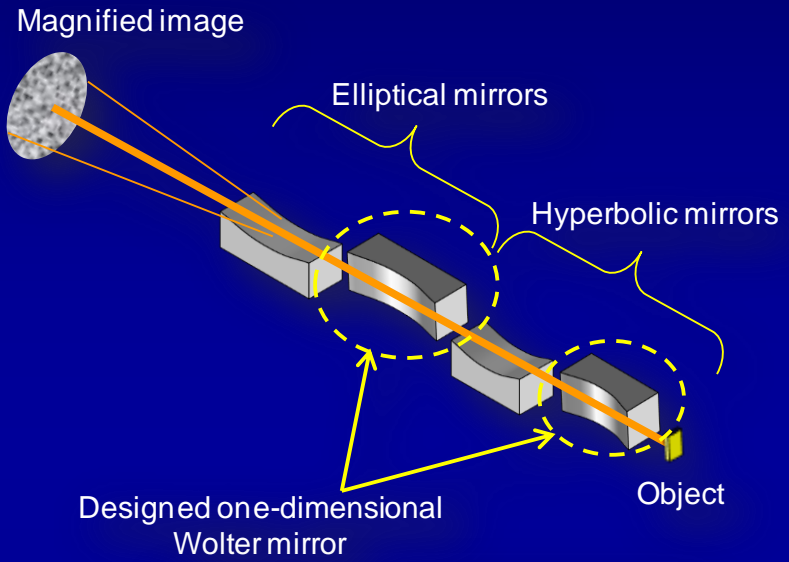
We tried to realize AKB mirrors having diffraction-limited performance.

1-dimensional Wolter mirror system

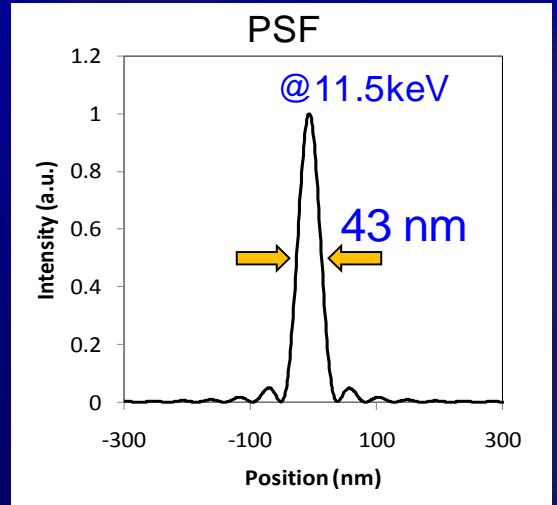
Magnification: 385x , Size of the point spread function: 43nm



Optical system of a one-dimensional Wolter optics



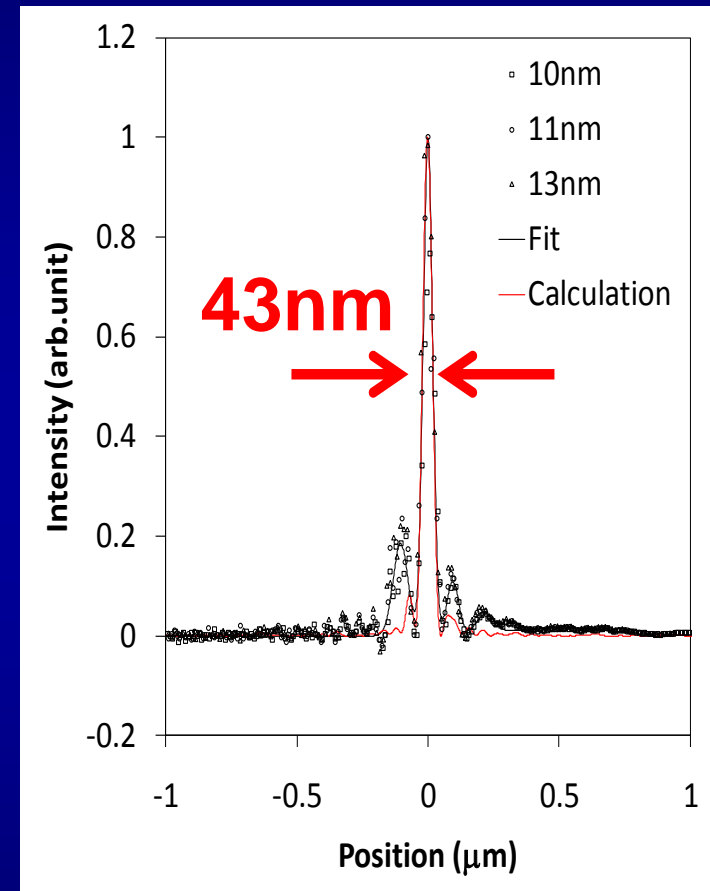
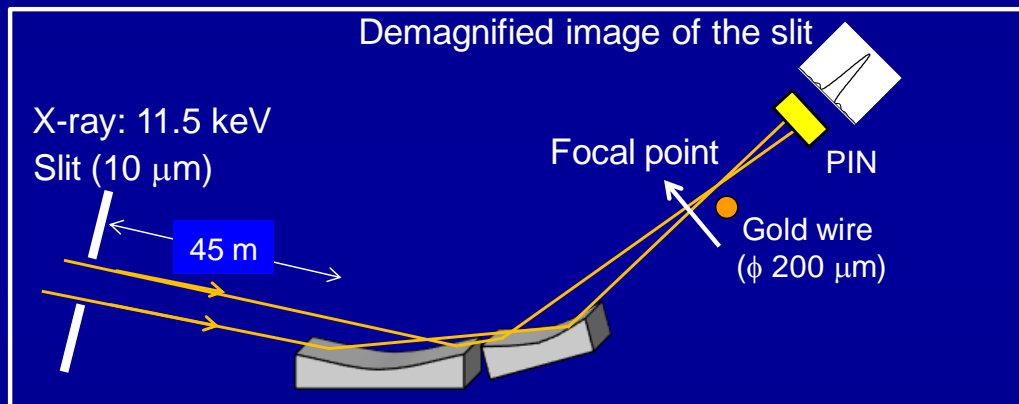
Mirror figures



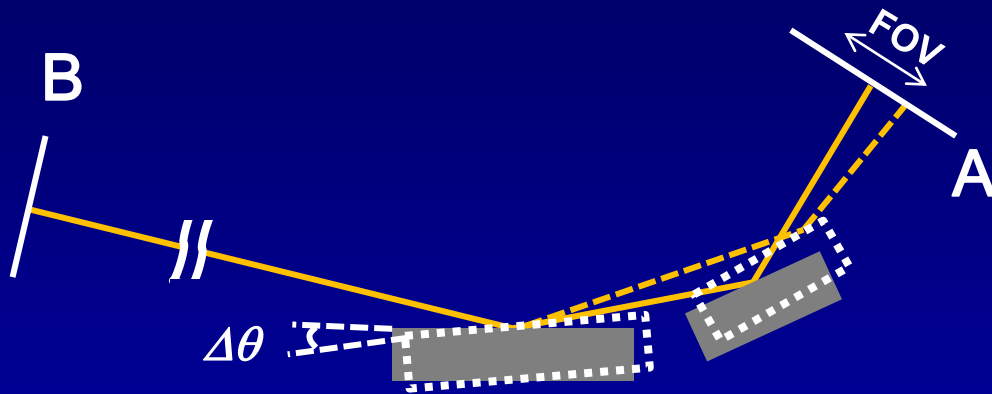
Spatial resolution test

Point spread function measurement

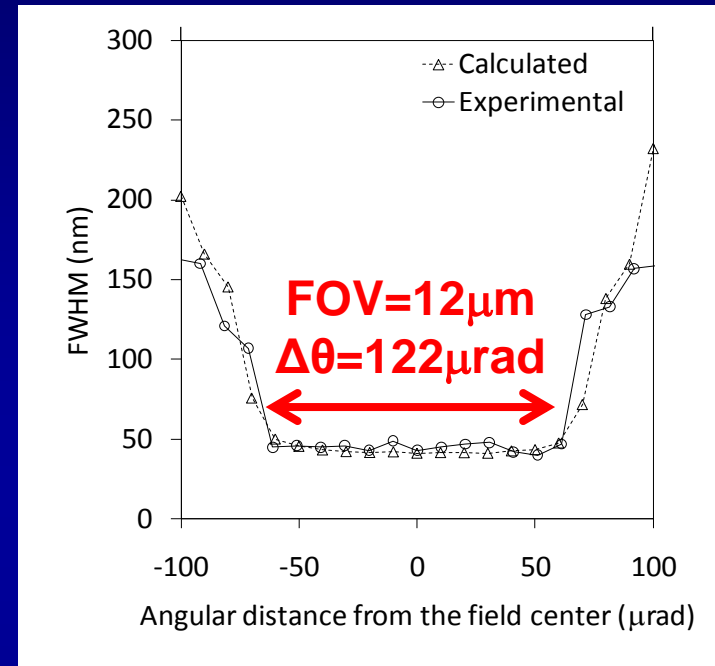
Demagnified imaging system



Evaluation of FOV

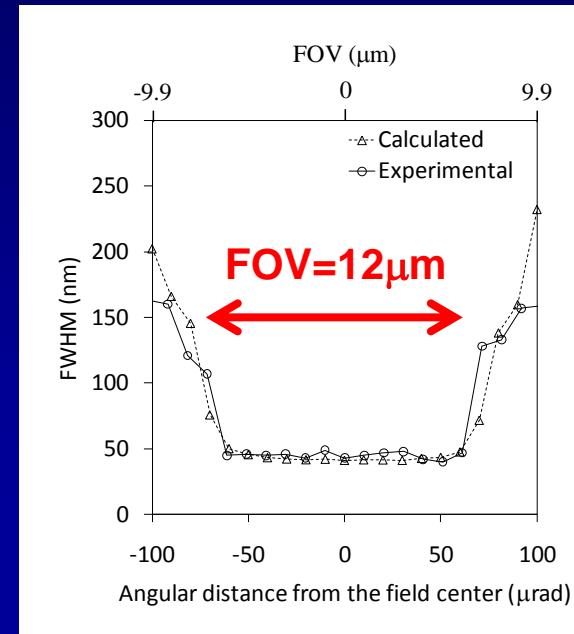
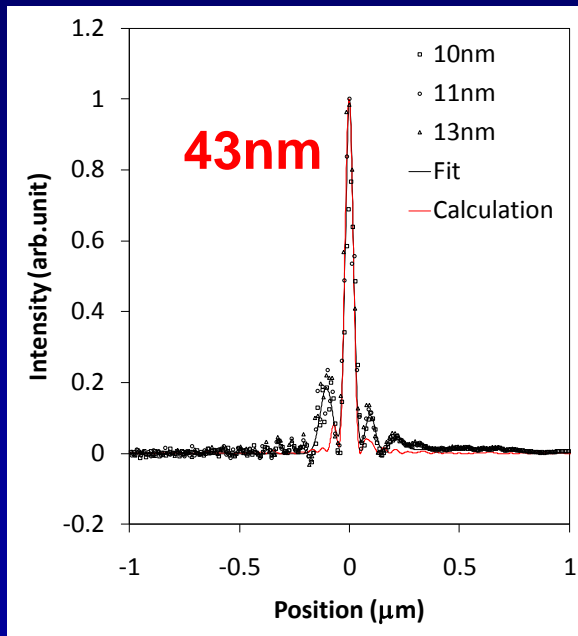


- To evaluate a field of view (FOV), we measured beam size on plane A by changing the glancing angle ($\Delta\theta$).
- This procedure is equivalent to shifting relevant points on the planes A and B.



- ◆ Very wide angular width ($\Delta\theta$) of 122 μrad was obtained.
- ◆ It is equivalent to the FOV of 12 μm .

Summary of AKB development

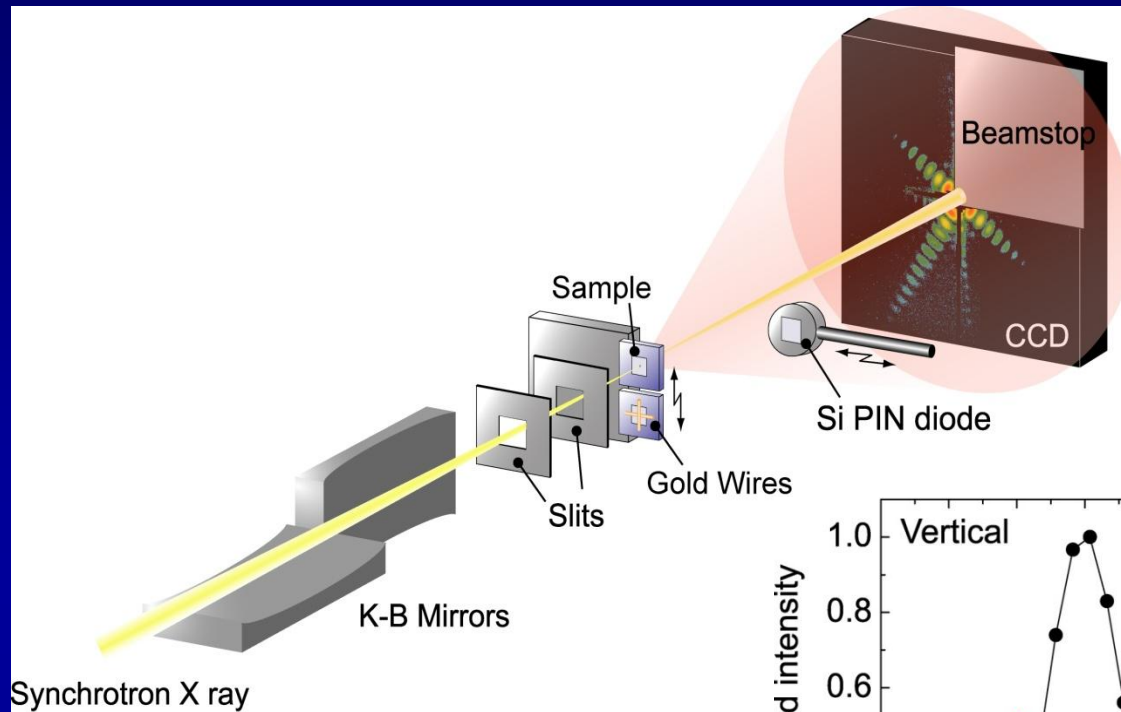


1-dimensional Wolter mirror demonstrated theoretically expected performances both in the resolution and FOV!

Matsuyama et al., Optics Lett (2010)

AKB optics will be indispensable optics especially in coming XFEL experiment.

Focused x-ray illumination for diffraction microscopy



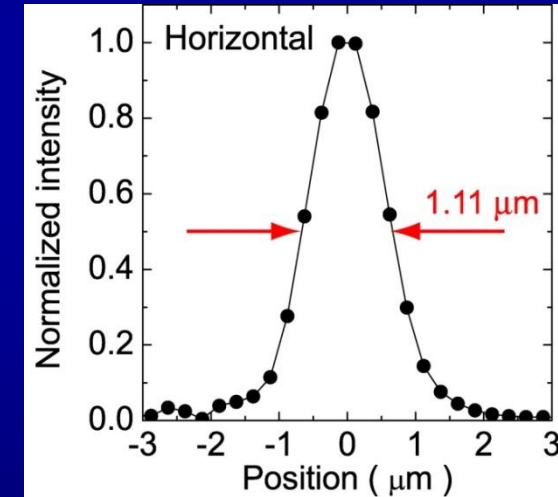
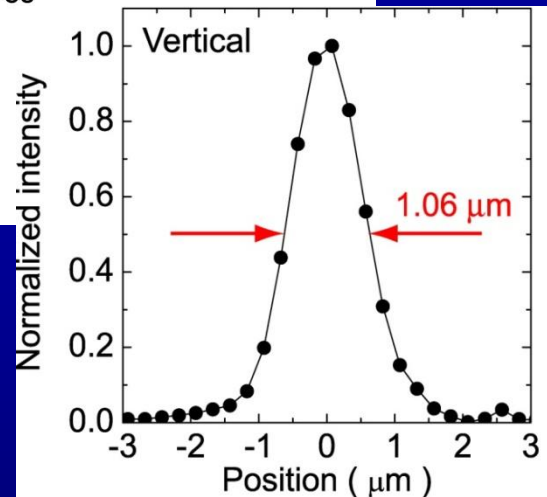
@SPring-8 BL29XUL

How wide area in k-space can we observe?



We must heighten the photon density at sample.

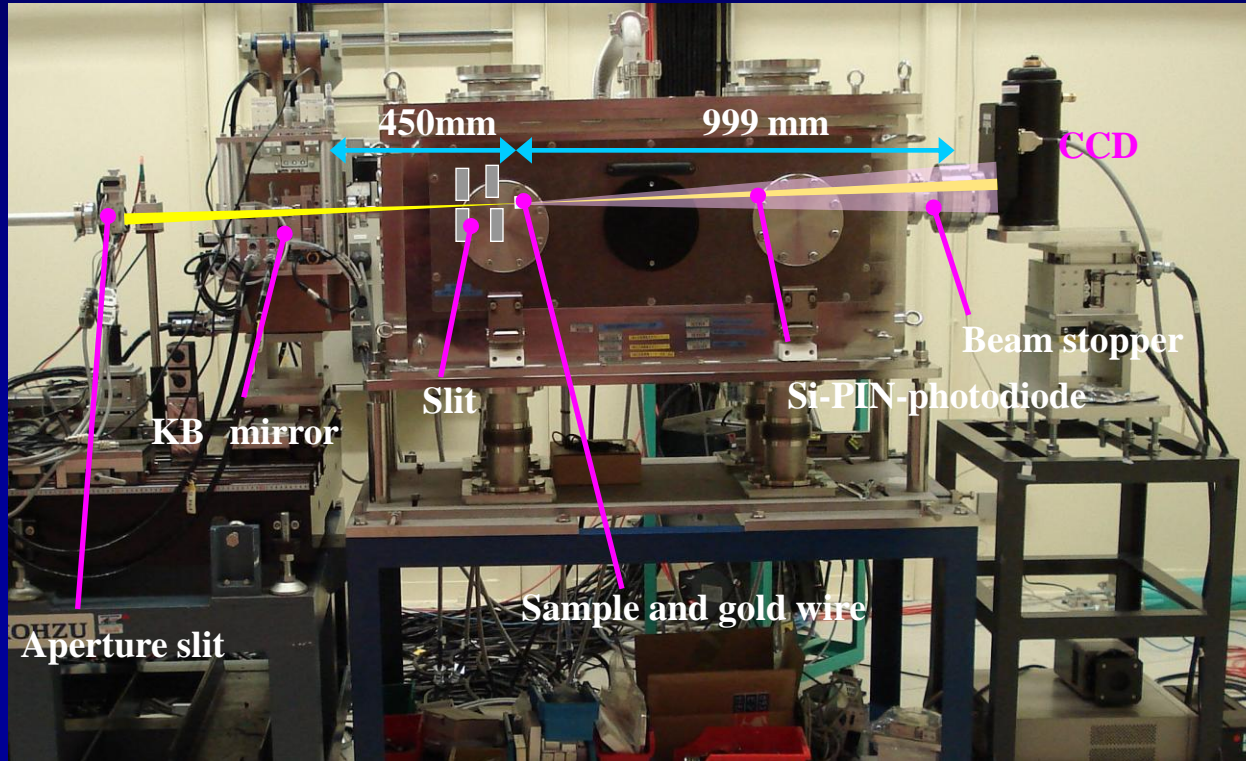
Beam profiles



- Spot size: $\sim 1 \mu\text{m}$
- Photon density: $\sim 1.0 \times 10^4$ photons/nm²/s

➡ More than 100 times larger

Set-up and samples



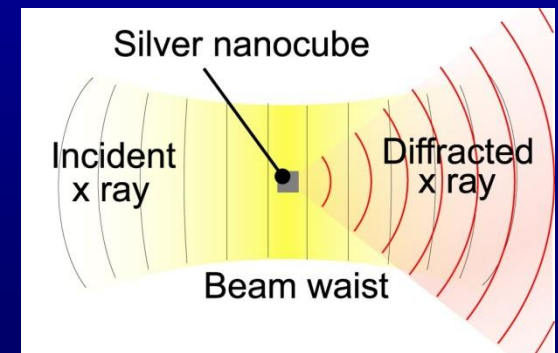
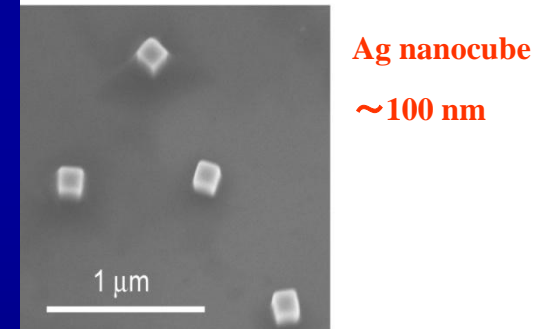
Science 298, 2176 (2002)

Shape-Controlled Synthesis of Gold and Silver Nanoparticles

Yugang Sun and Younan Xia*

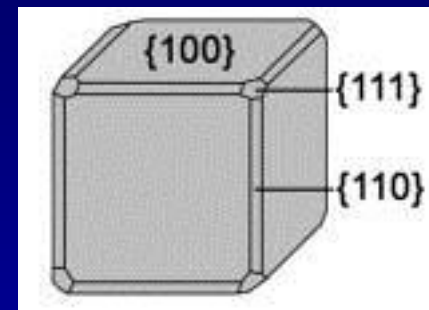
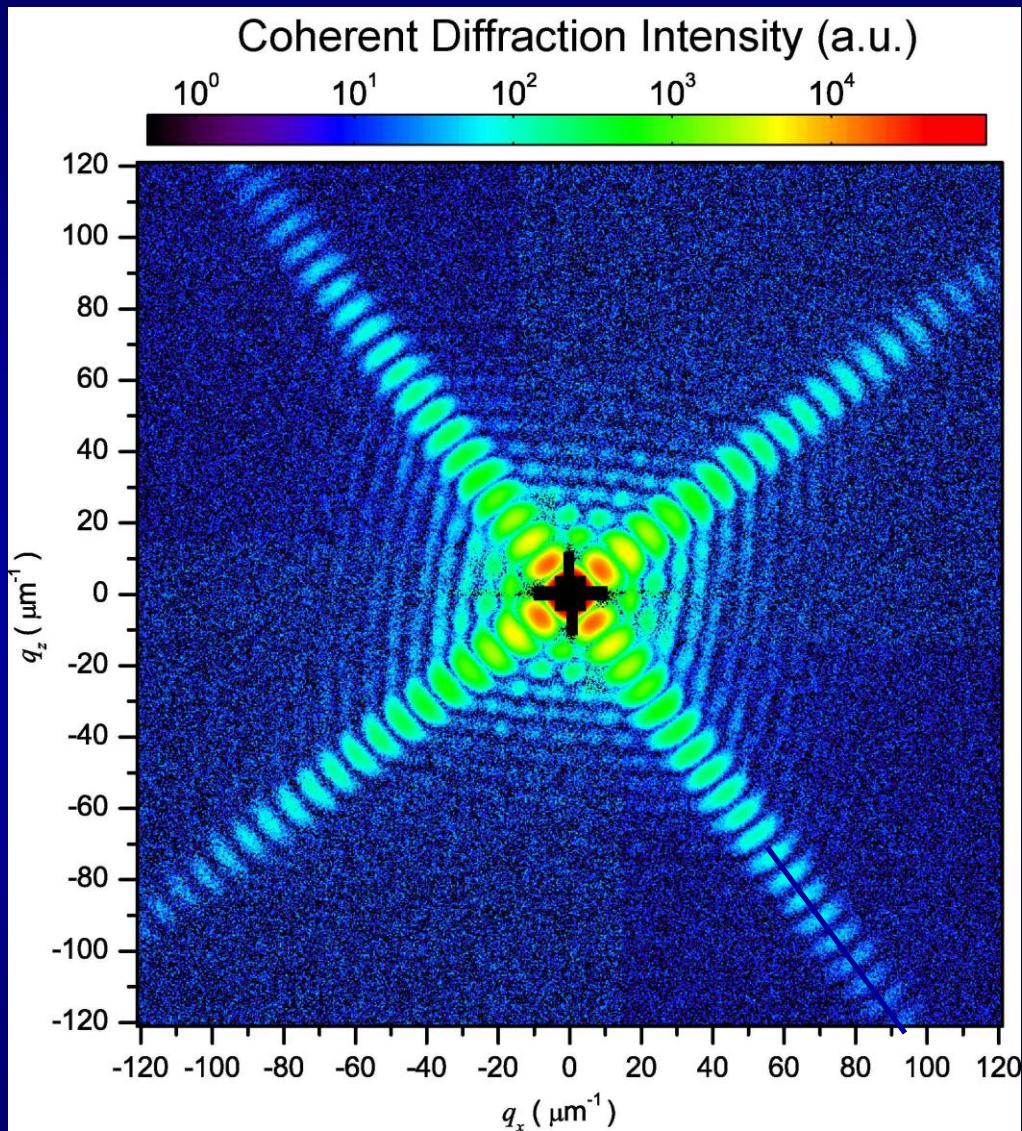
Monodisperse samples of silver nanocubes were synthesized in large quantities by reducing silver nitrate with ethylene glycol in the presence of poly(vinyl pyrrolidone) (PVP). These cubes were single crystals and were characterized by a slightly truncated shape bounded by {100}, {110}, and {111} facets. The presence of PVP and its molar ratio (in terms of repeating unit) relative to silver nitrate both played important roles in determining the geometric shape and size of the product. The silver cubes could serve as sacrificial templates to generate single-crystalline nanoboxes of gold: hollow polyhedra bounded by six {100} and eight {111} facets. Controlling the size, shape, and structure of metal nanoparticles is technologically important because of the strong correlation between these parameters and optical, electrical, and catalytic properties.

SEM image



- ◆ X-ray energy: **12keV**
- ◆ Working distance: **450mm**
- ◆ Camera length: **999mm**
- ◆ CCD (Princeton Instruments PI-LCX:1300)

Pixel size: 20 μ m
1300 \times 1340 pixels

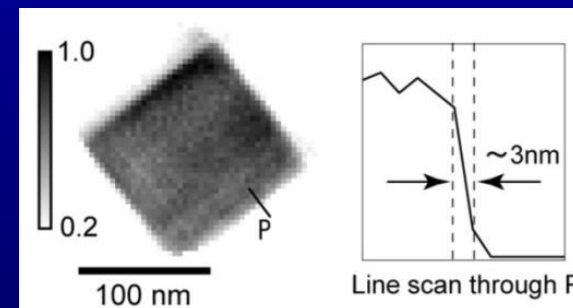


$$|q| = 2\sin(\Theta/2)/\lambda$$

λ : wavelength

Θ : Scattering angle

Sinc function: $\frac{\sin(\alpha q)}{\alpha q}$



Exposure time : 800sec, 1.5×10^{11} Photons to the cube

Y.Takahashi et al., Phys. Rev. B 80, 054103 (2009).

Summary

- Achromatic total-reflection mirrors realized sub-30nm focusing of hard X-rays.
- In-site wavefront correction are promising techniques to construct highly accurate optical system of hard X-rays.
- KB mirrors could reach sub-10nm focusing.
- AKB mirrors enable achromatic imaging of incoherent x-rays with sub-50nm-resolution.
- KB mirrors could condense x-rays with preserving coherency and could heighten the spatial resolution of diffraction microscopy up to sub-5nm.