

Polymer systems and phase identification

S4SAS 2014

Adam Squires

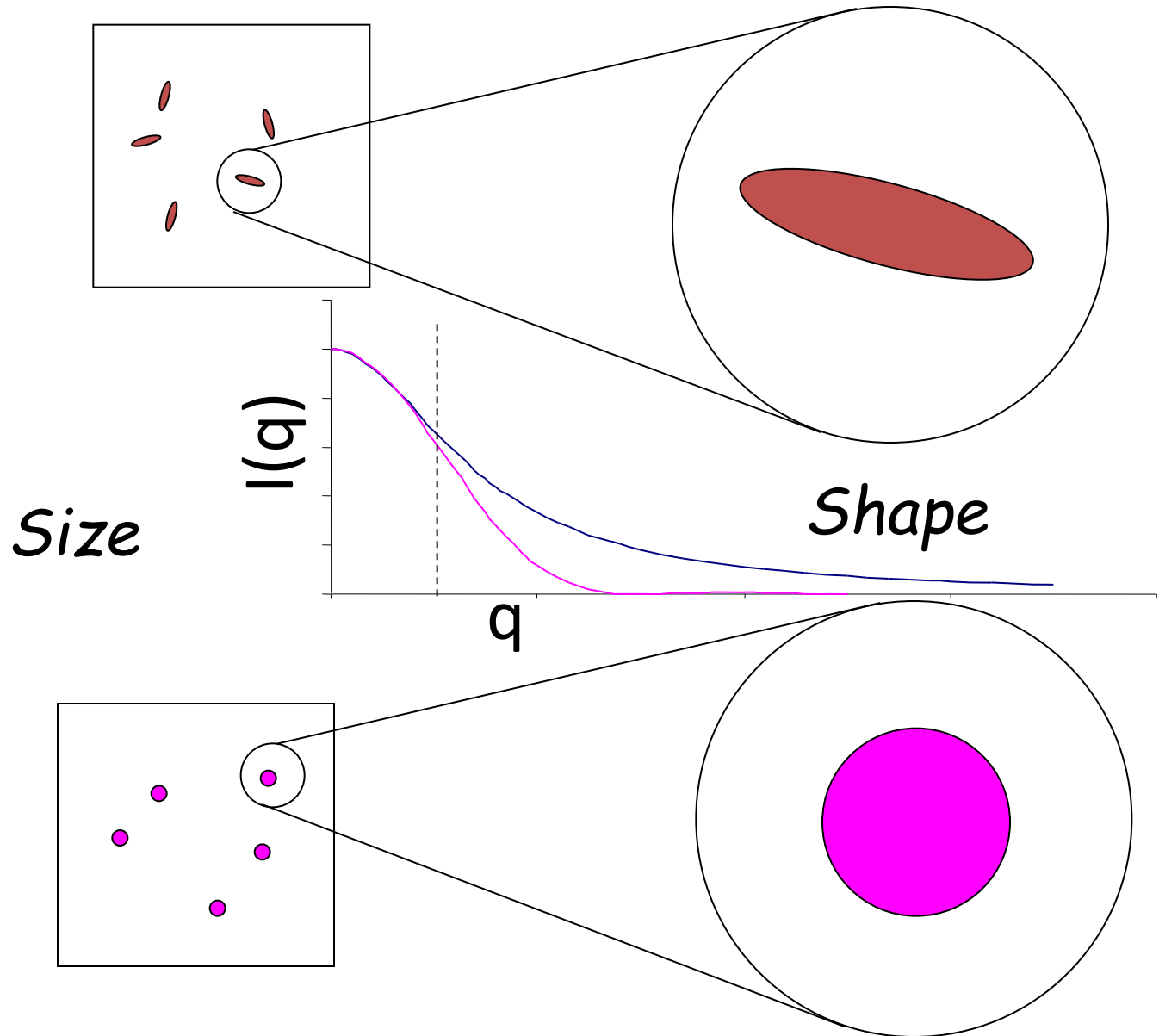
Department of Chemistry

University of Reading

Outline

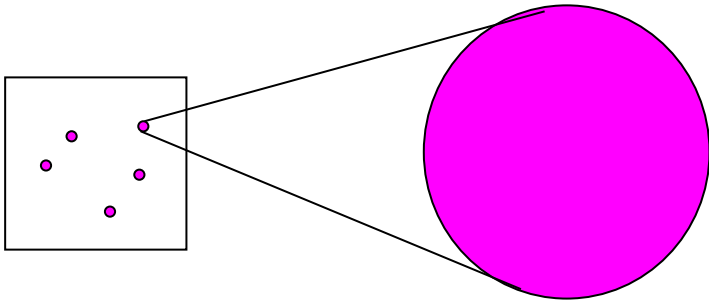
- Solutions, non-crystalline materials
 - Polymer chains, proteins
- Periodic systems
 - Block copolymers
 - Lyotropic liquid systems (surfactants; lipids)
 - Mesoporous materials
- Orientation: powder-like or aligned

Reminder:



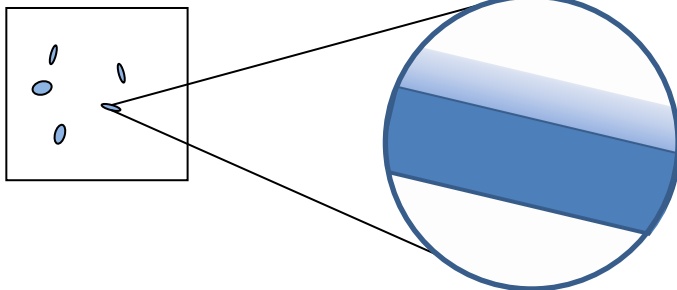
From James' talk: “Dimensionality” of different shapes

At $Rg > q$ Scattering tends to $I \sim q^{-a}$



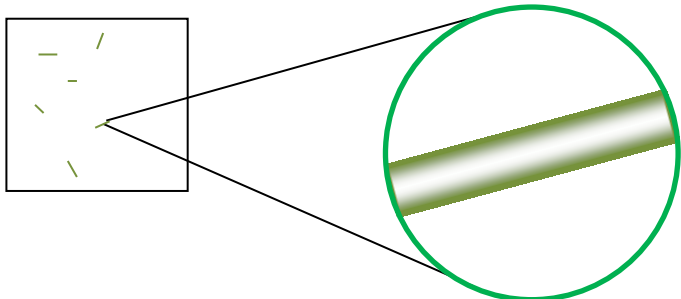
- Spheres (3D): $a = 4$

$$1/q < Rg$$



- Disks (2D): $a = 2$

$$\text{Thickness} < 1/q < \text{Radius}$$

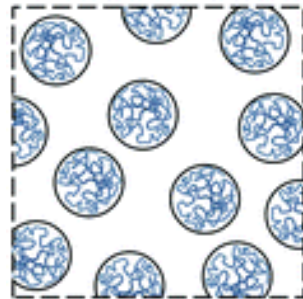


- Rods (1D): $a = 1$

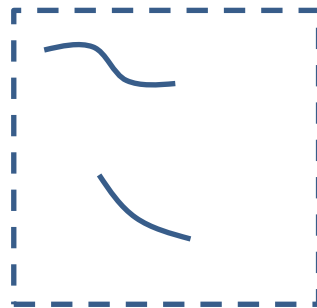
$$\text{Radius} < 1/q < \text{Length}$$

Dimensionality of a polymer chain in solution

- A (strongly) self-attracting chain would pack itself into a ball; this would make a sphere (3D; $a = 4$)



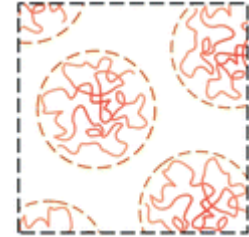
- A (strongly) self-repelling chain would stretch out into a completely extended rod (1D; $a = 1$)



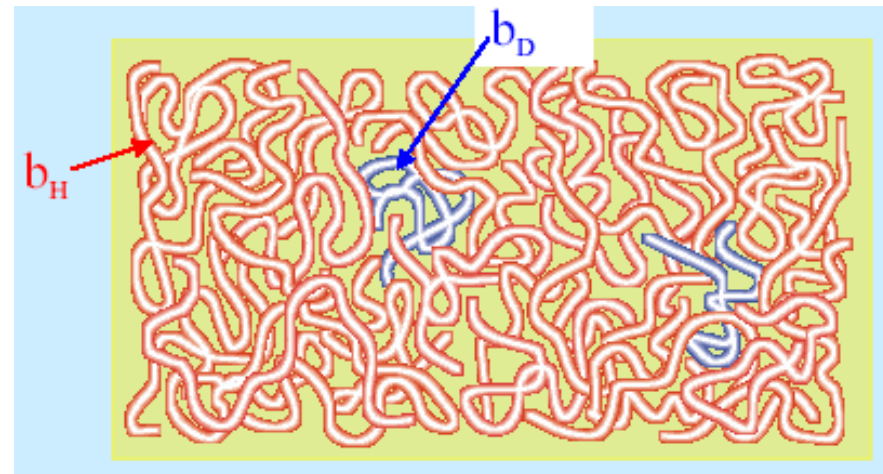
Neither attracting nor repelling?

- Polymer in a “theta” solvent

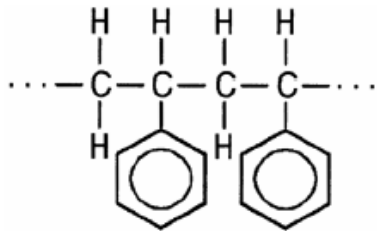
- Interactions with solvent same as interactions with self



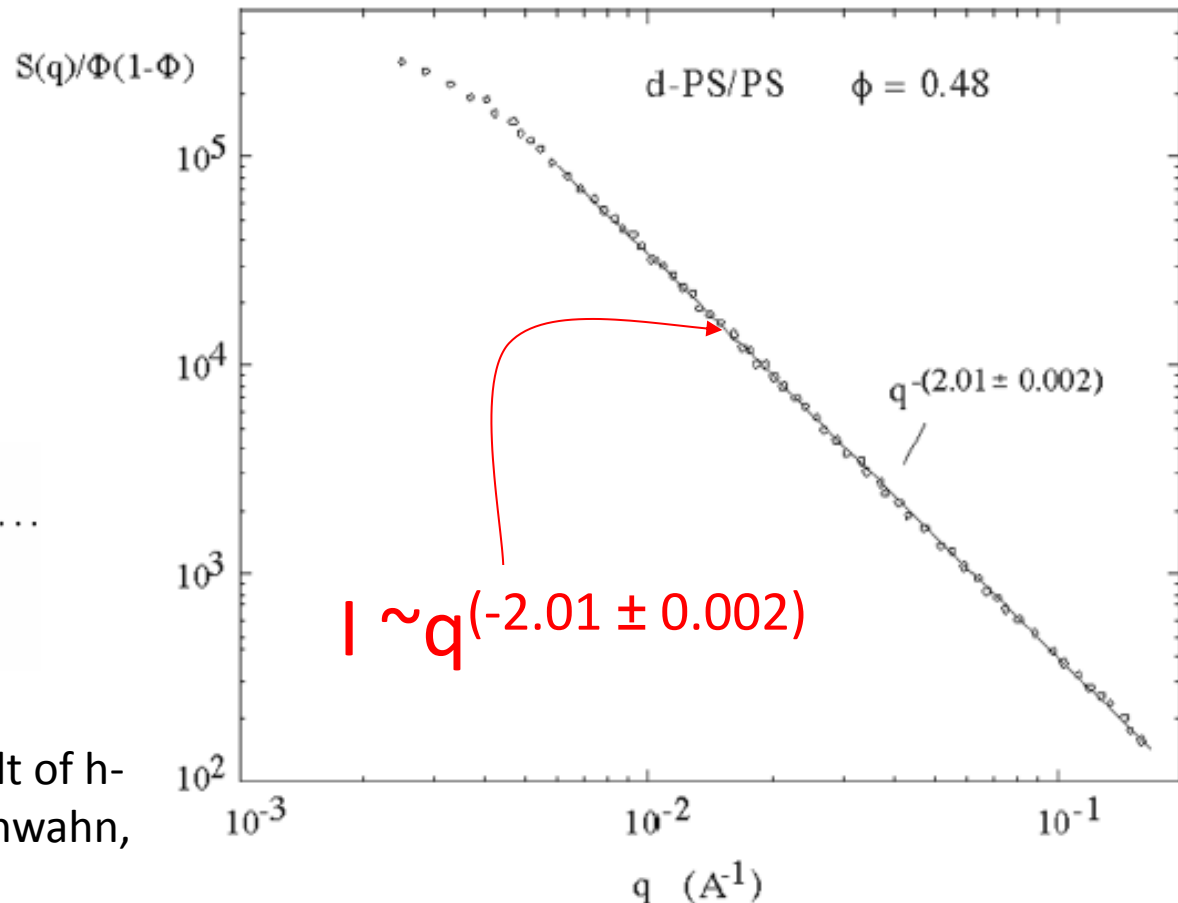
- Polymer in the melt
(use neutrons)



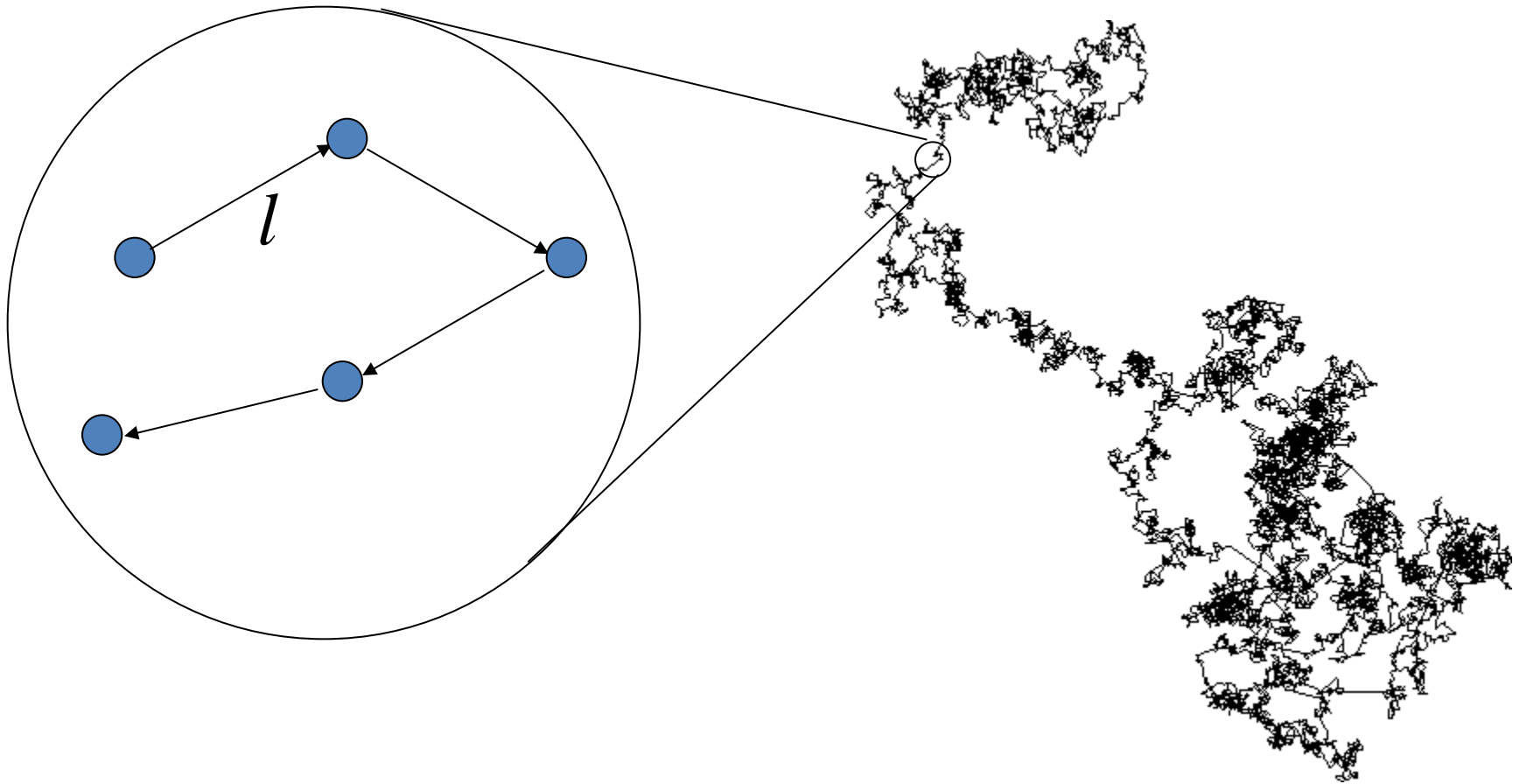
Polymer chains that neither attract nor repel themselves show $a = 2$. This corresponds to a “random walk” (“Gaussian chain”).



scattered intensity for a melt of h- and d-polystyrene (from Schwahn, 1991 using SANS)

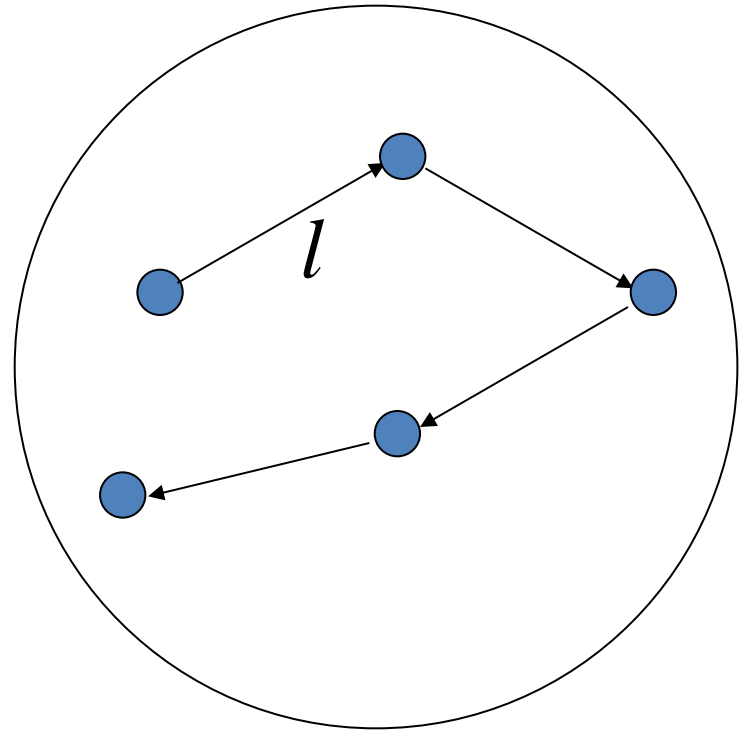


Random walks



Properties of a random walk

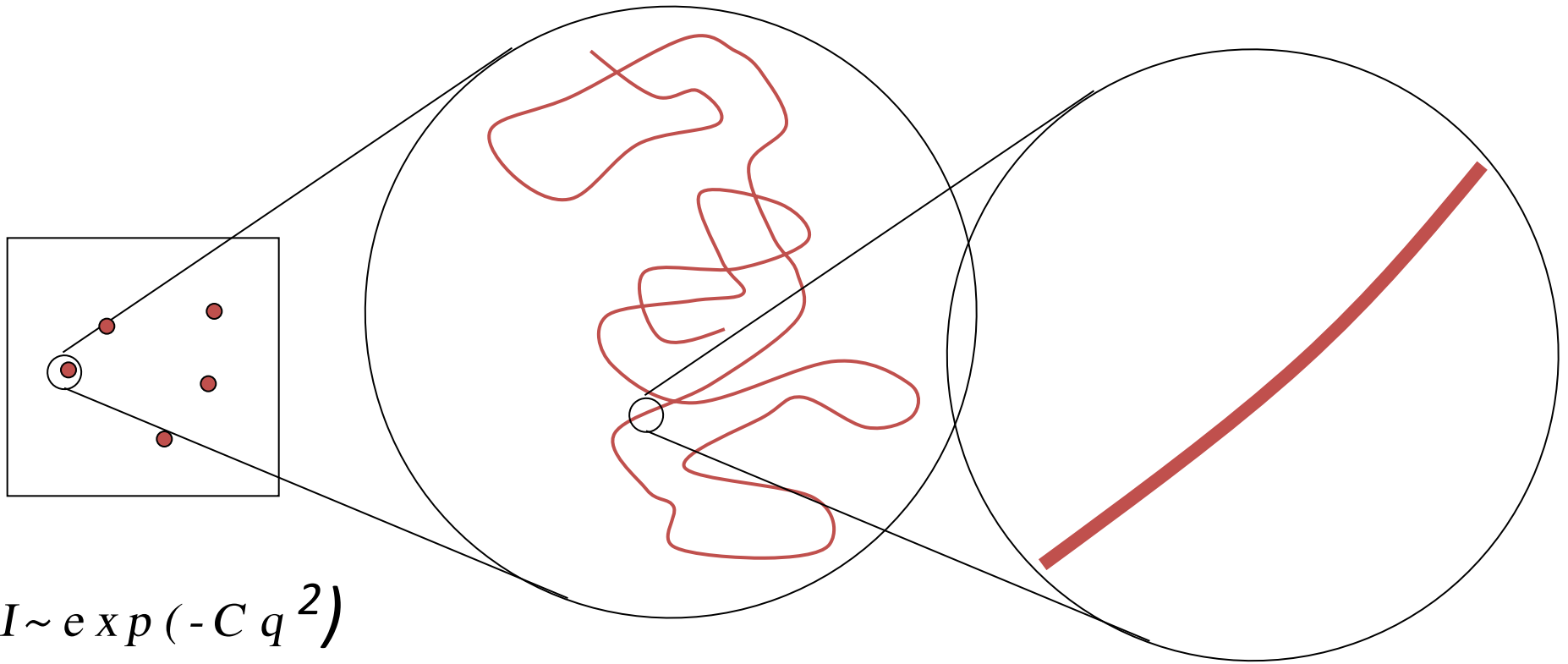
- N “steps” each of length l
- Expected end-to-end distance is $l \sqrt{N}$
- Expected $R_g = l \sqrt{(N/6)}$



Deviations from Random Walk

- (Imagine a length of rubber tubing)
- On a long enough size scale, it can behave randomly
- On a shorter size scale, because the tubing isn't infinitely flexible, bits of tubing close to each other aren't independent
- On a size scale less than the "persistence length" the tubing looks like a straight rod.

So, overall



$$I \sim \exp(-Cq^2)$$

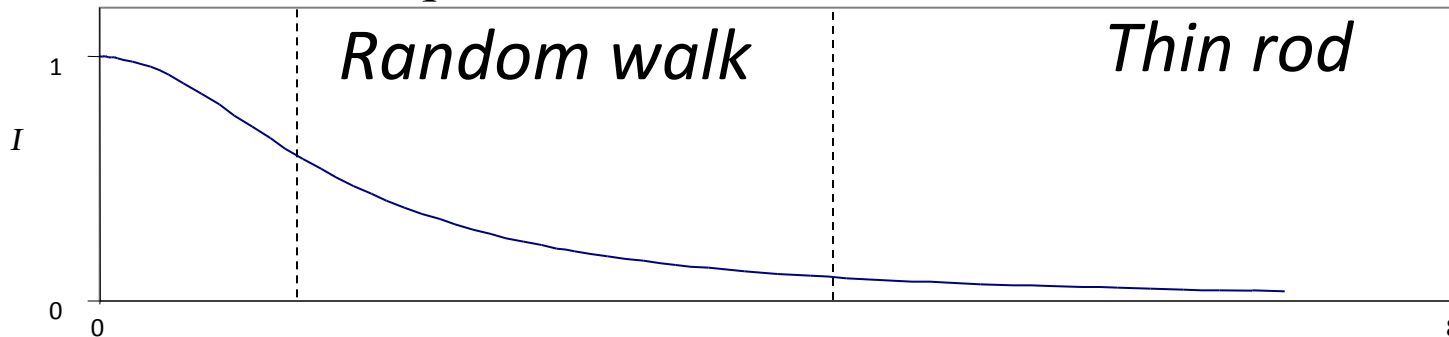
Guinier

$$I \sim q^{-2}$$

Random walk

$$I \sim q^{-1}$$

Thin rod

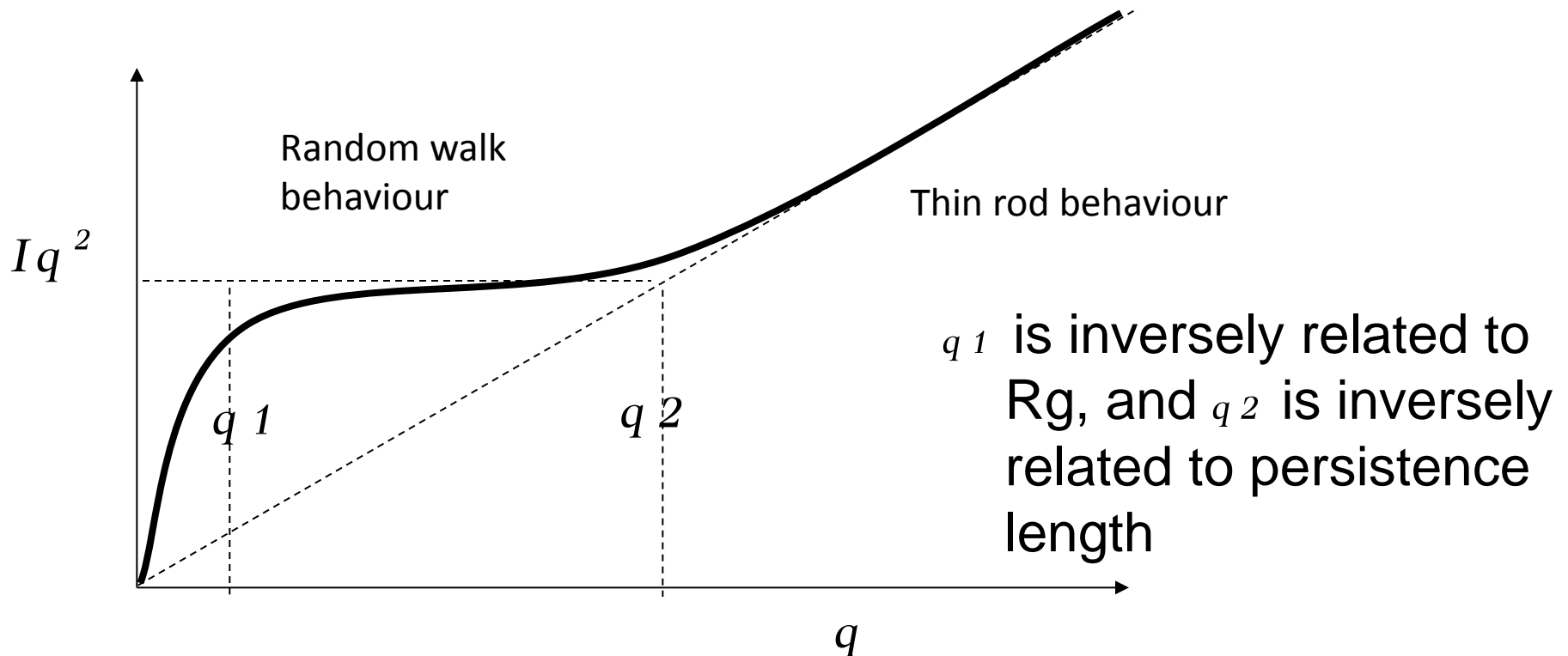


“Worm-like chain” (Kratky and Porod)

Kratky plot (see Rob and James’ talks)

If $I \sim q^{-2}$

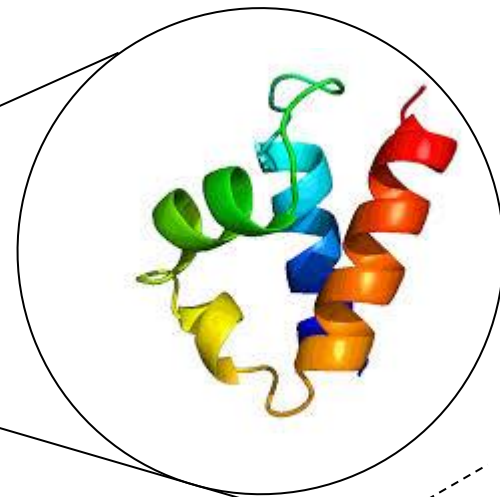
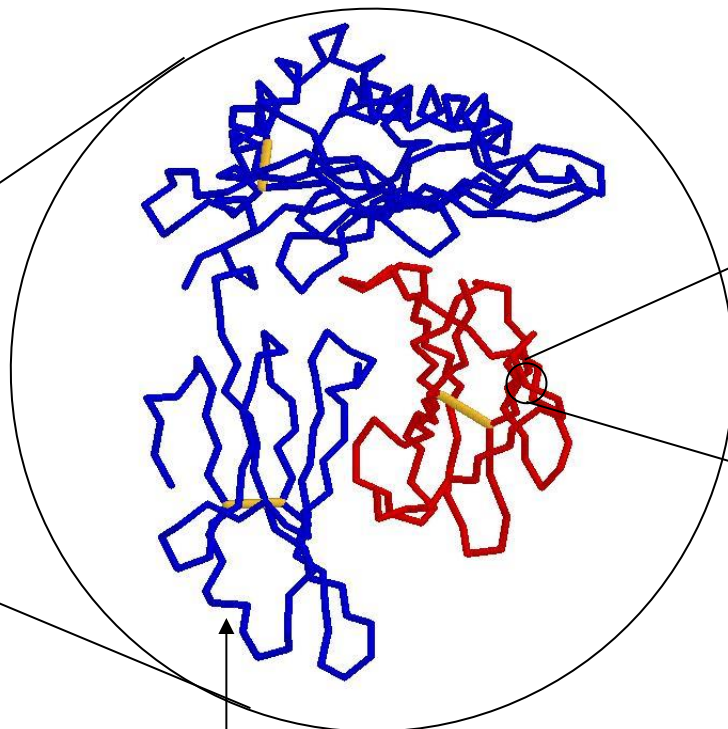
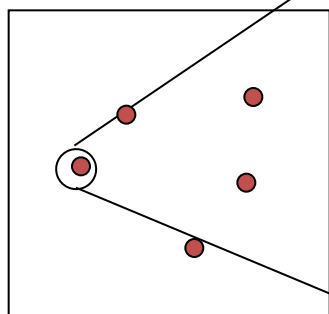
$I q^2$ is a constant



More deviations from Random Walk

- At higher q (short length scale), the Kratky-Porod Worm-like chain acted more like a rigid rod (ie, self-repelling)
- Conversely, folded proteins with internal structure are self-attracting at a short length scale: see Rob's talk

Self-attracting short-range (eg proteins)



$$I \sim \exp(-Cq^2)$$

Guinier

Iq^2

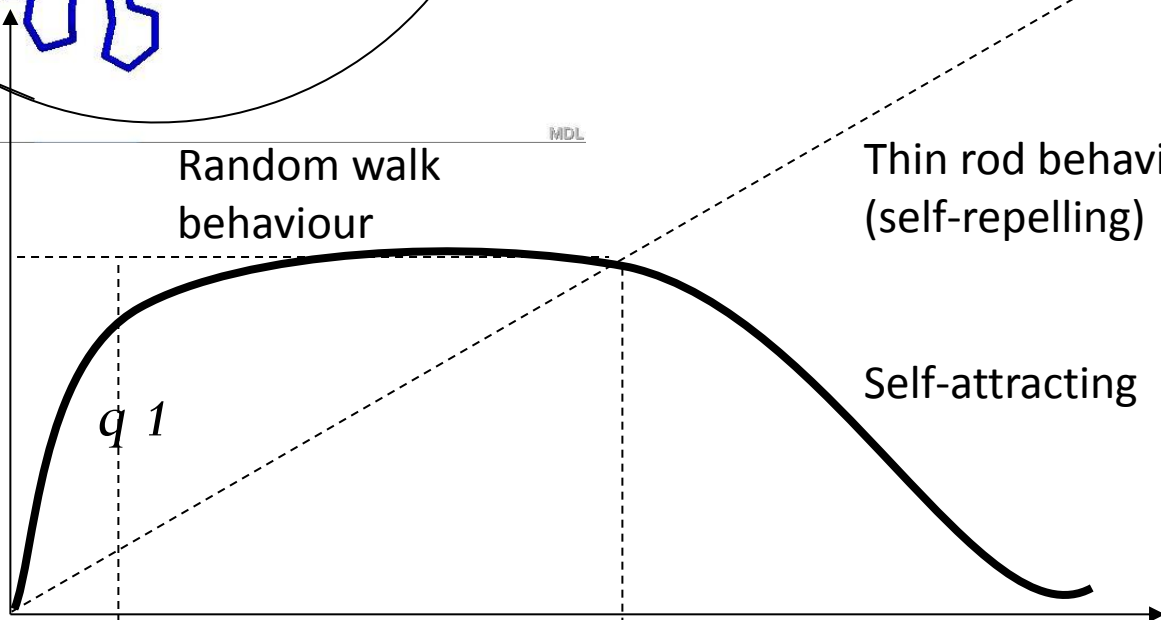
Random walk
behaviour

MDL

Thin rod behaviour
(self-repelling)

Self-attracting

q_1



Summary so far

- With solution scattering, you can measure
 - Size (R_g) from Guinier plot in very small angle region. Plot $\ln I$ vs q^2
 - Shape (dimensionality) from plot of $\ln I$ vs $\ln q$
 - Persistence length; flexibility of polymer chain (and extent of “random walk” behaviour) from Kratky plot. Plot Iq^2 against q

Task (1)

- Boffins at the Institute of Studies have, for the first time, used science to produce “Polymer nano-Wotsits”



- In a theta solvent, the polymer adopts a random walk within a cylindrical envelope (as shown).

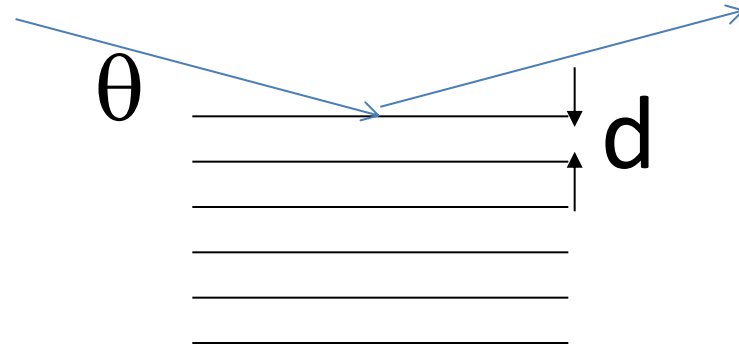
Discuss what you would expect to see in the scattering pattern.

Periodic systems

- Regular repeating features on the 10-100nm size scale are less common, requiring self-assembly:
 - Lipids / detergents (tens of nm)
 - Diblock copolymers (hundreds of nm)
 - *Biological materials (eg keratin, collagen etc) (hierarchical)*
 - Mesoporous materials (silica, metal...)

1D periodicity

- Bragg's law:
$$n\lambda = 2d \sin\theta$$



- Simplification:
X-ray reflections from
periodicity *across the
beam*.

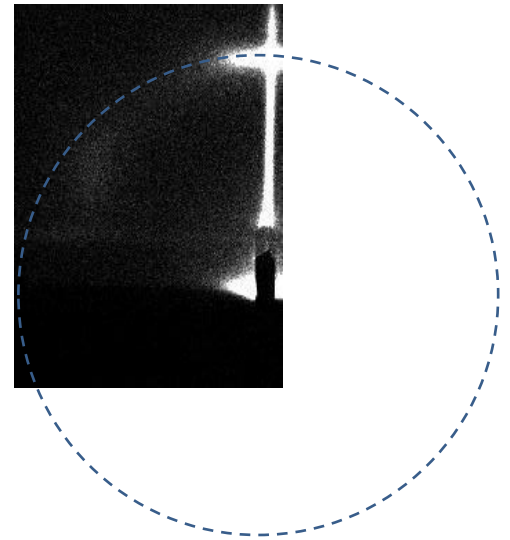
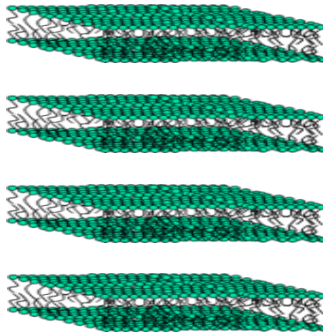
[small-angle]

Flash cartoon: powder diffraction

http://www.personal.reading.ac.uk/~scs05ams/xray_cartoon.html

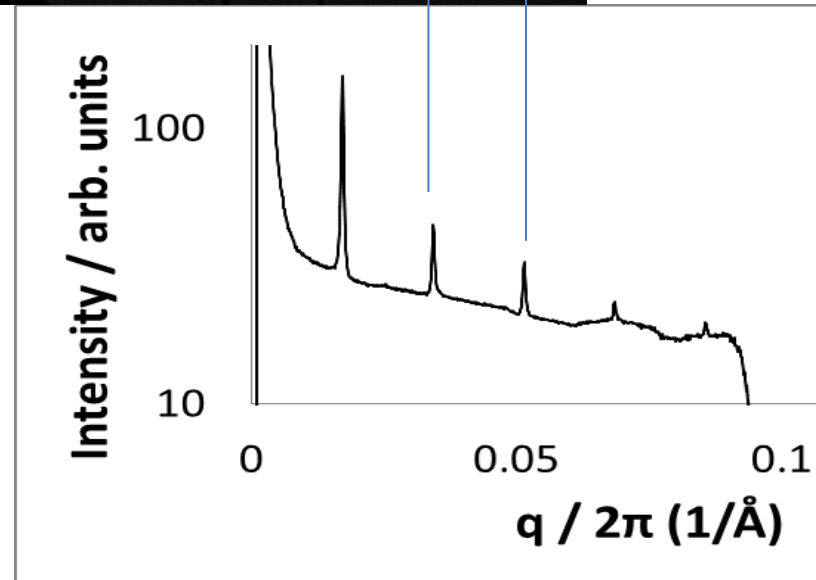
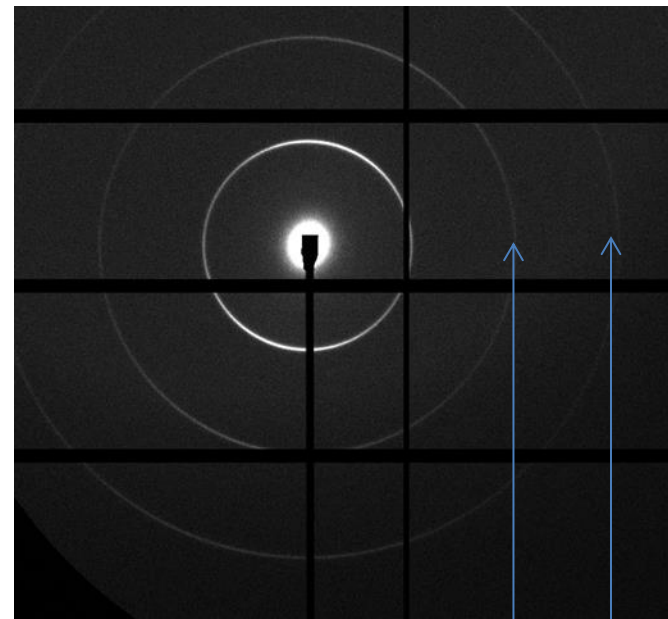
Examples

- Lamellar Phase



More complexity

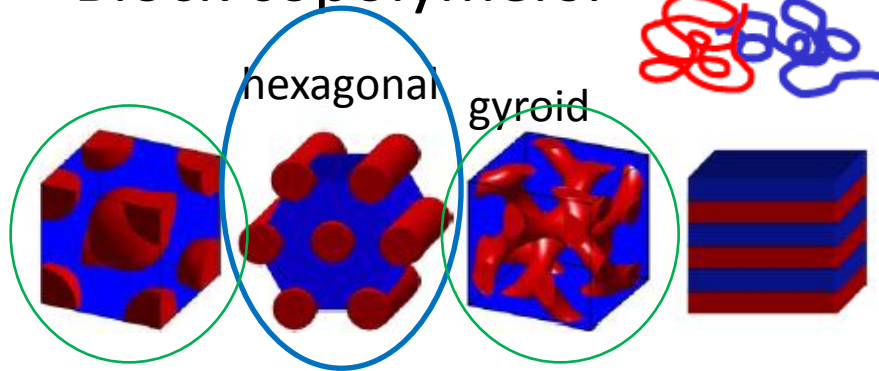
- Bragg Equation: $n\lambda = 2d \sin\theta$
 - Higher order reflections $n=2,3,4\dots$



- How about 2D or 3D periodicity?
- Block Copolymers / surfactant / lipid phases

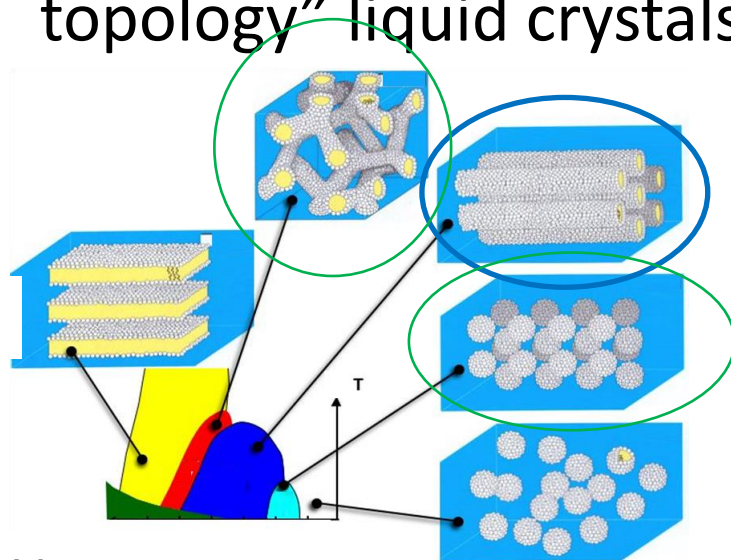
Periodic nanomaterials

- Block copolymers:

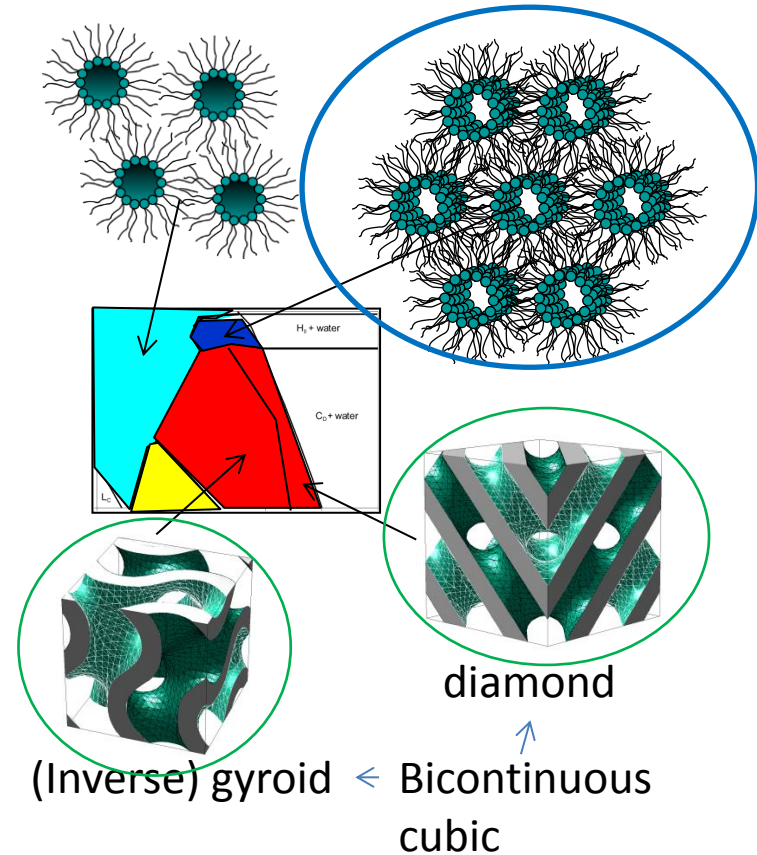


B. W. Boudouris, Purdue

- Surfactants (“normal topology” liquid crystals):



- Lipids (“inverse topology” liquid crystals):

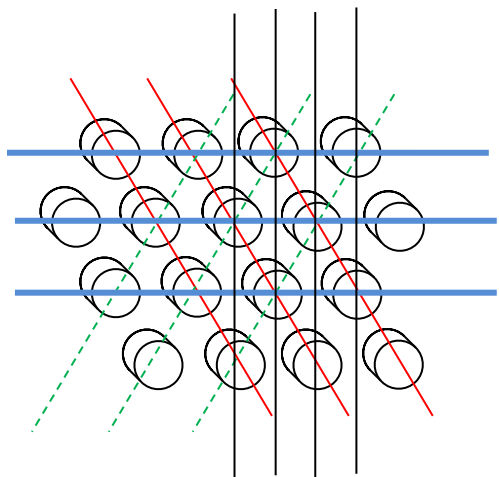


2D periodicity

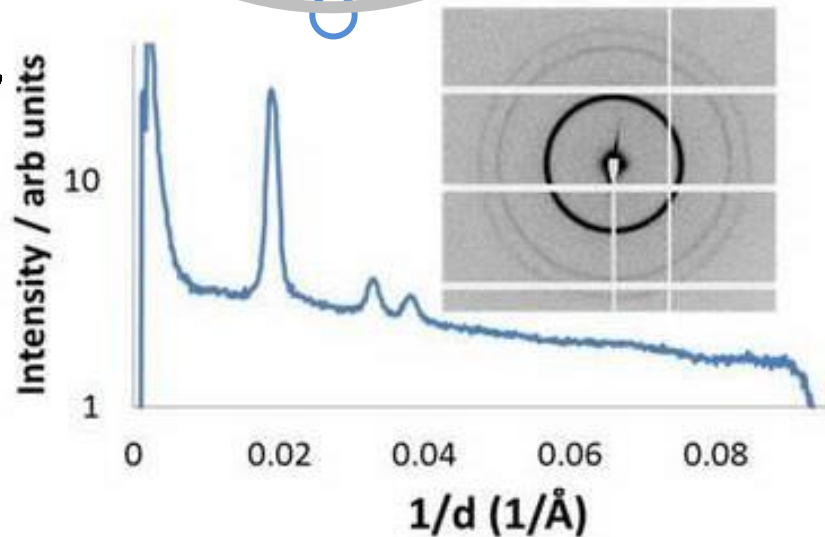
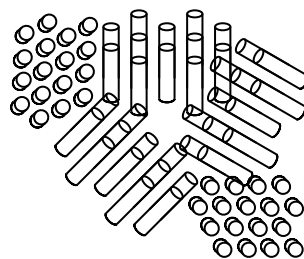
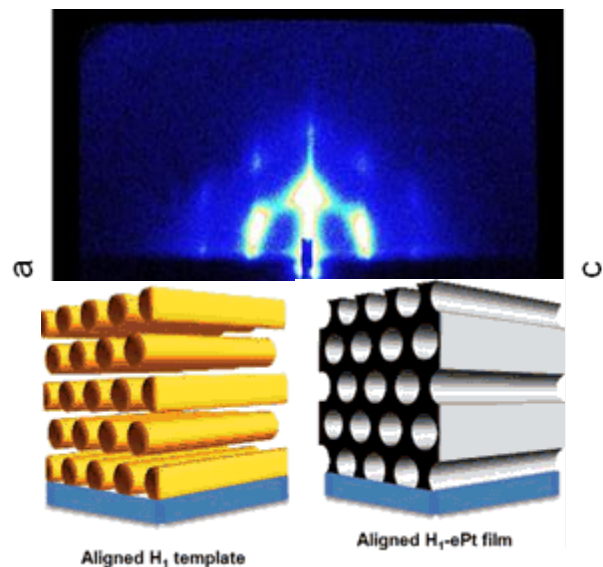
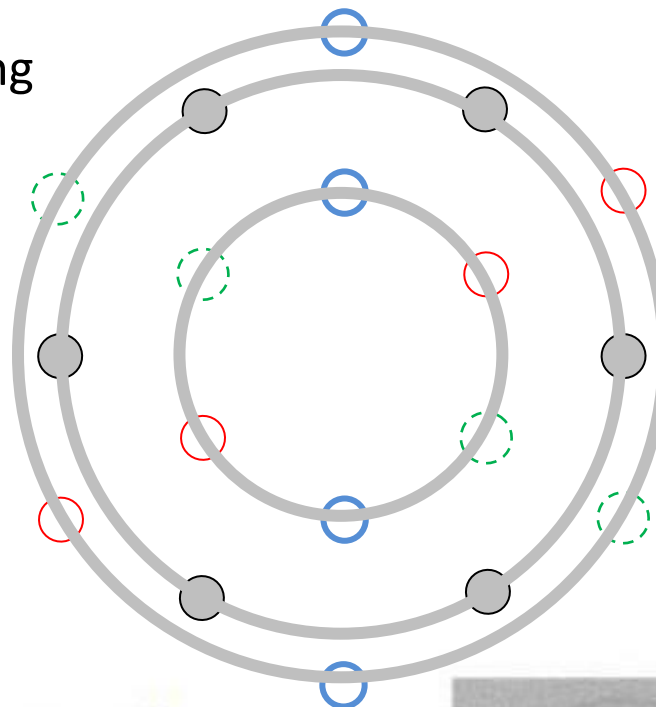
3D periodicity

SAXS patterns from hexagonal phase

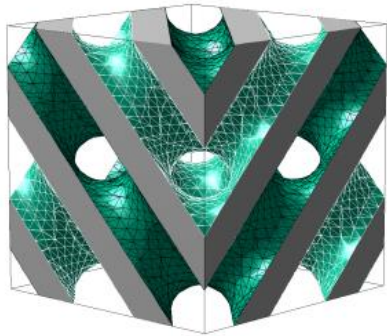
Structure:



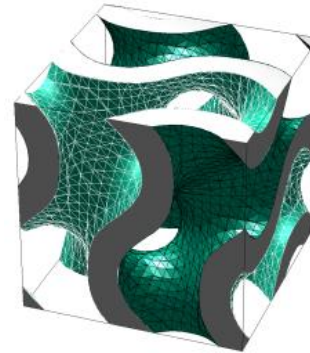
Scattering pattern:



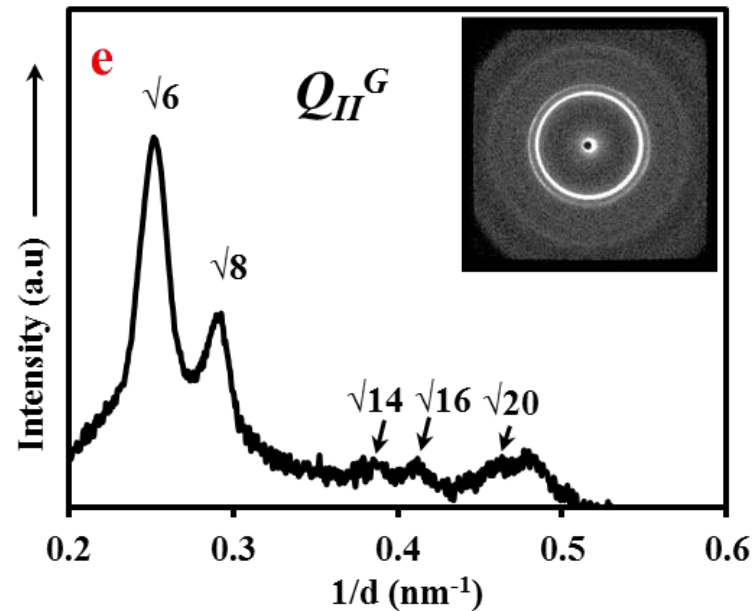
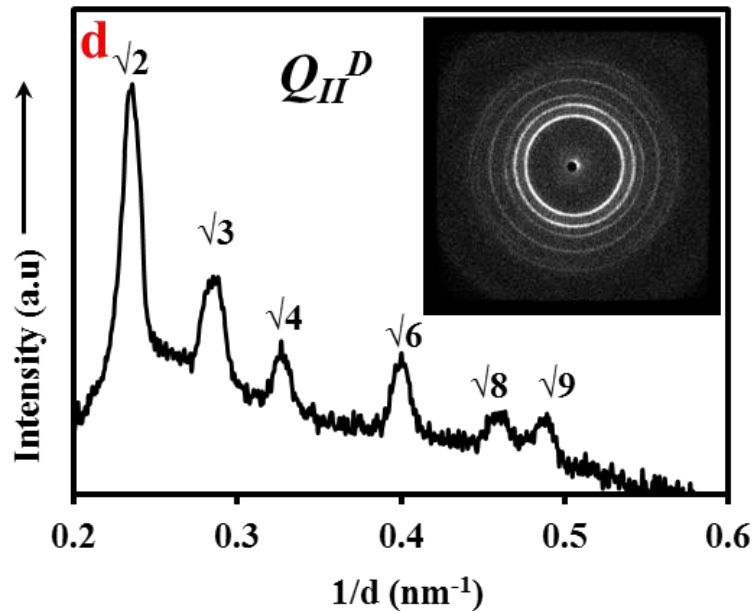
3D periodicity: cubic phases



Diamond
 $Pn3m$
(Space group 224)



Gyroid
 $Ia3d$
(Space group 230)

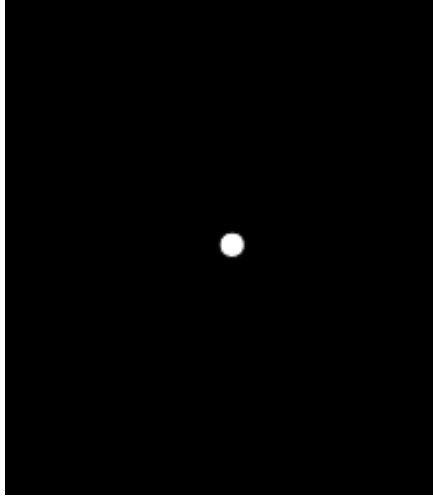


- Summary:
 - Positions of reflections
 - Lattice parameter
 - Symmetryie structure factor
- Next:
 - Intensity of reflections
 - Electron distribution
 - What shape is your repeating objectie form factor

Pattern is Fourier Transform of Electron density

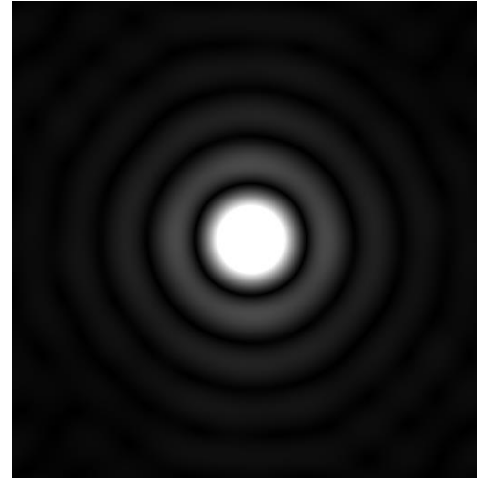
- Any object (=distribution of electron density) gives some sort of scattering pattern.
- This is an image of the Fourier Transform (FT) of the electron density distribution.
- [See previous talks]

Real Space

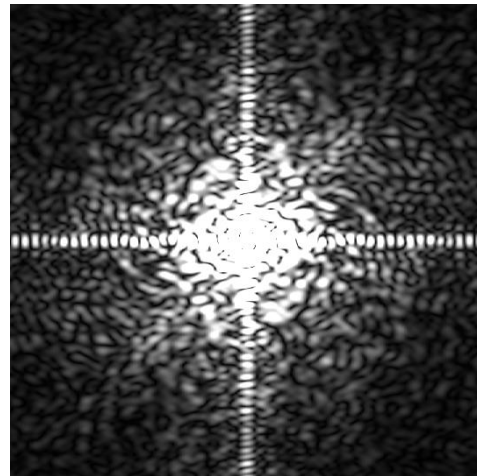


circle

Scattering Pattern (Fourier Transform)

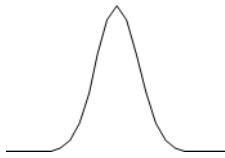


BA Baracus

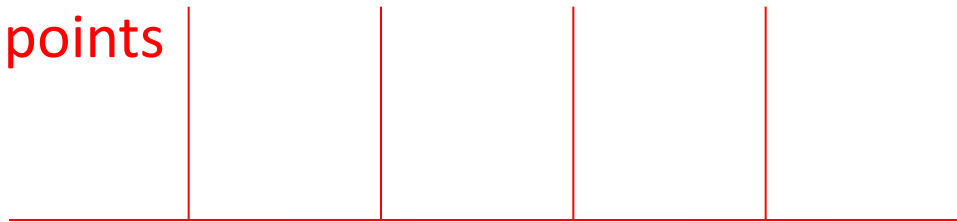


A periodic array of an object [Eg a crystal]

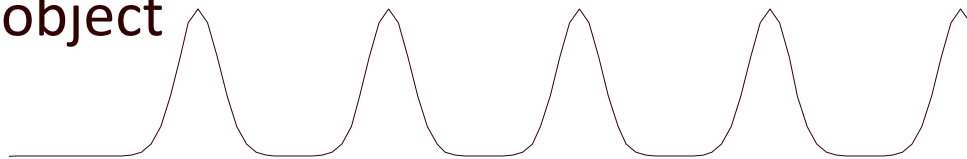
Object:



Lattice of
points



1D Crystal of an
object



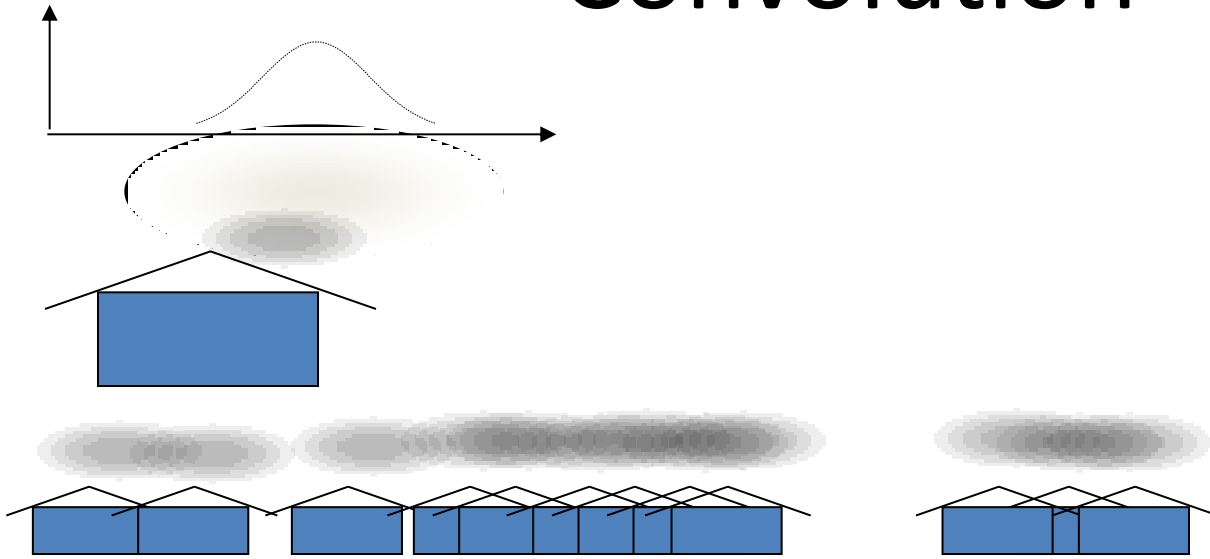
Crystal = Lattice * Object

convolute

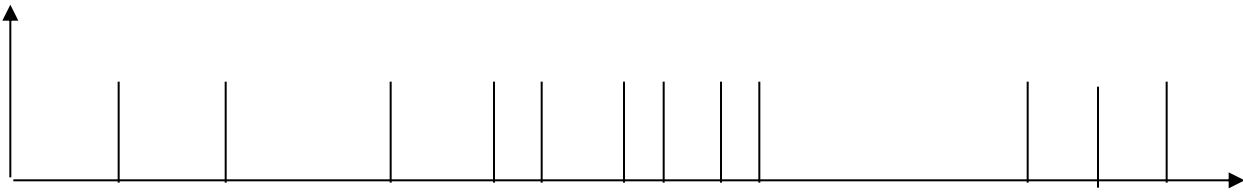
A crystal is the *convolution* of a lattice of points with whatever object is inside a unit cell.

Convolution

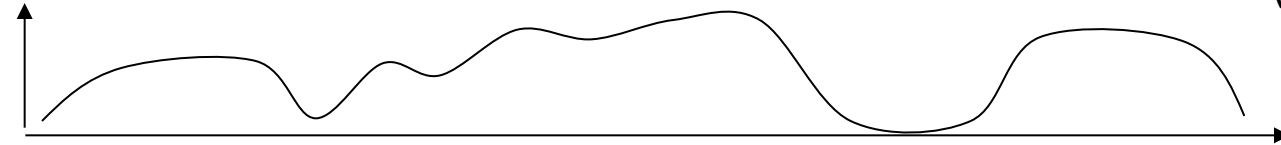
Smoke from one chimney



Houses



Smoke



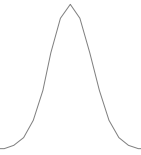
(Smoke from one chimney)

*

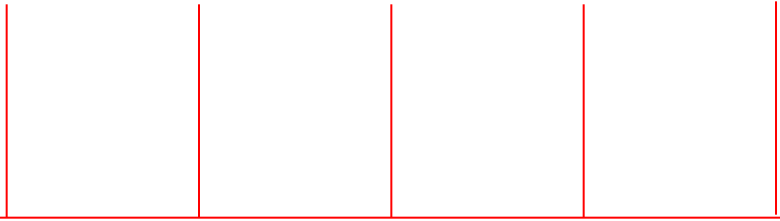
(Distribution of chimneys)

Real Space

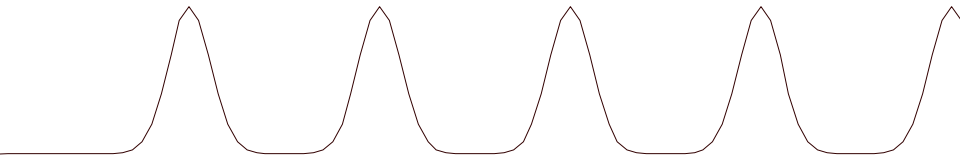
Object



Lattice
of
points



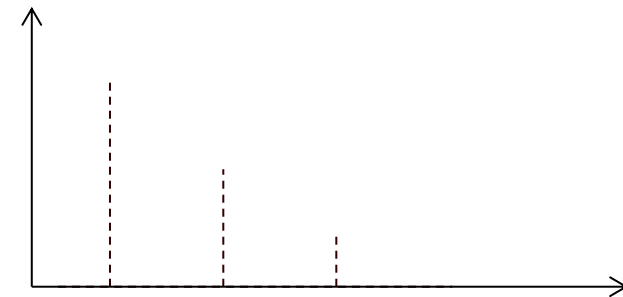
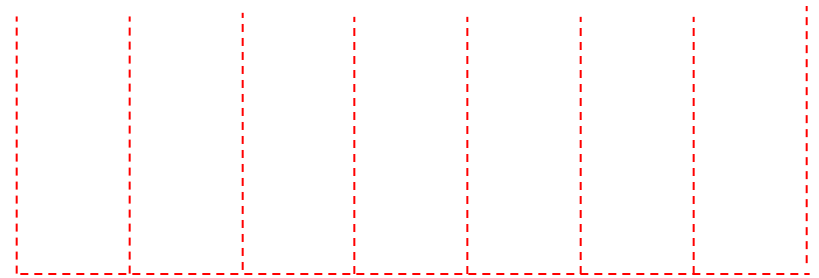
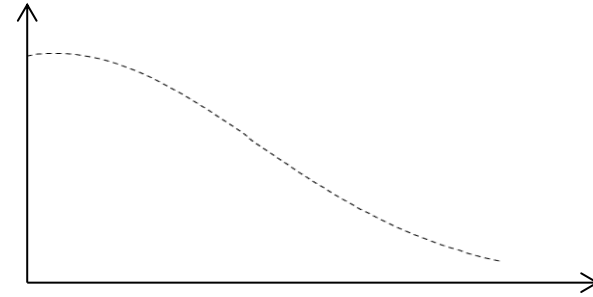
Object



$$\text{Crystal} = \text{Lattice} * \text{Object}$$

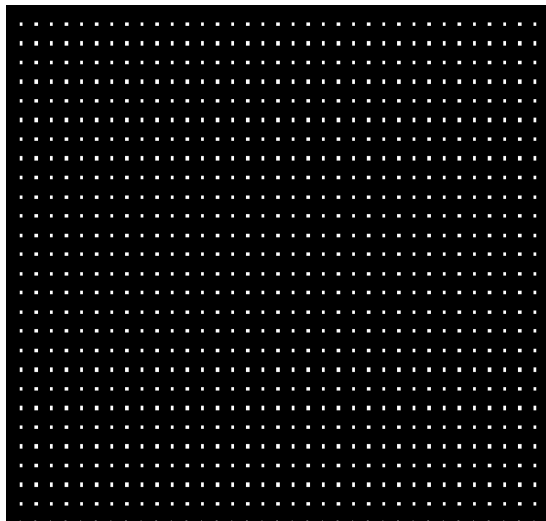
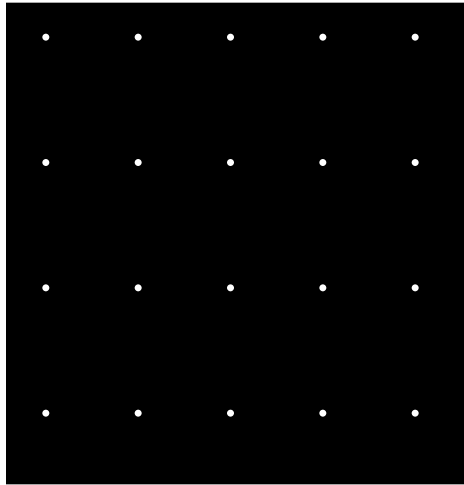
convolute

Scattering Pattern (Fourier Transform)

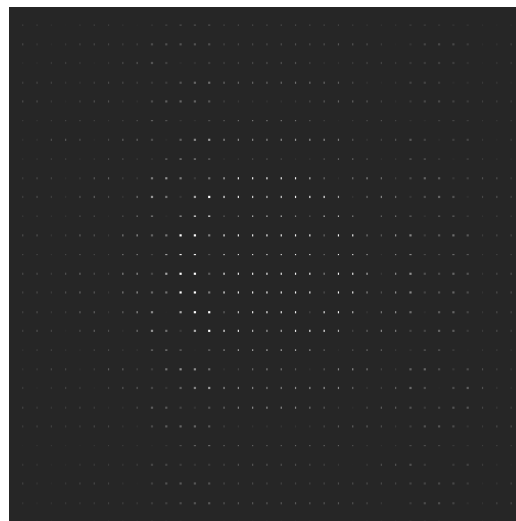
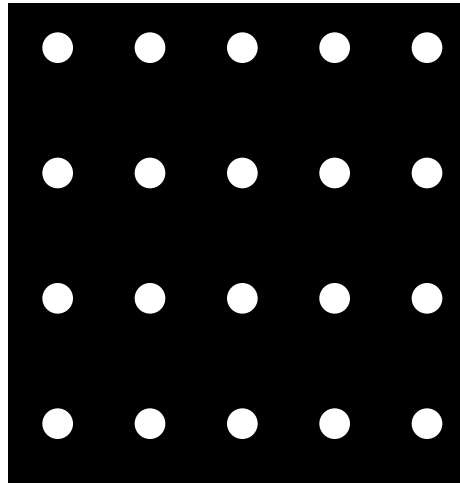


$$\text{FT}(\text{Crystal}) = \text{FT}(\text{Lattice}) \times \text{FT}(\text{Object})$$

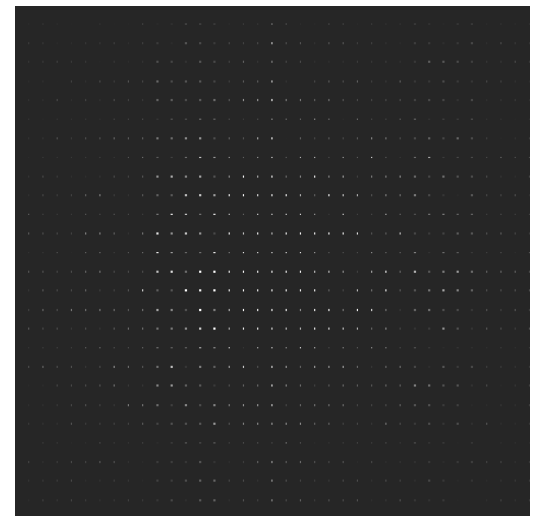
Points



Circles



BA Baracus's

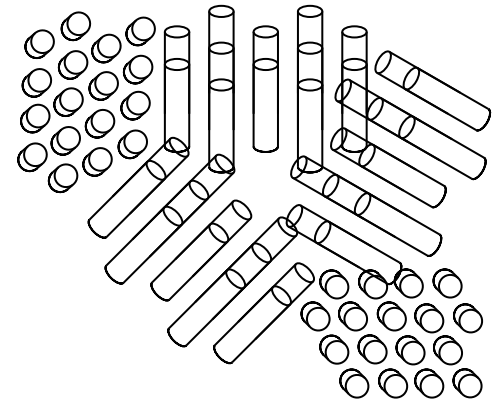


Summary

- *Positions* of spots / peaks → Symmetry of lattice
- *Intensities* of spots / peaks → Electron distribution within one unit cell of lattice

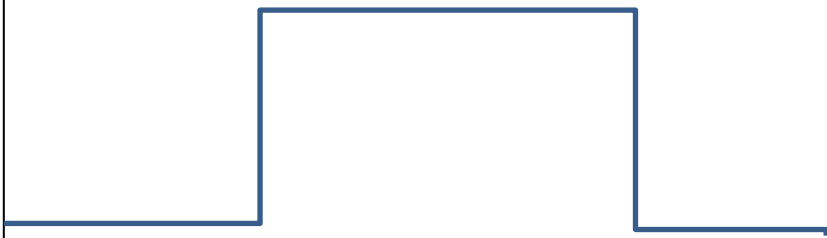
Next:

- *Width* of spots / peaks → Finite number of repeats (crystallite size?)
[or other causes]

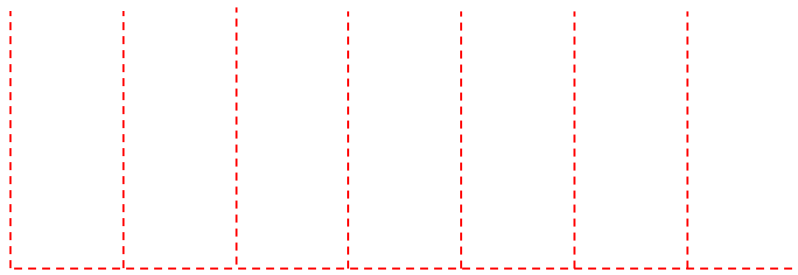


Real Space

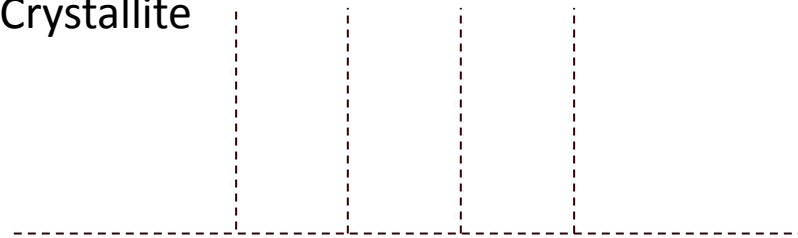
Shape of Crystallite



Infinite Lattice



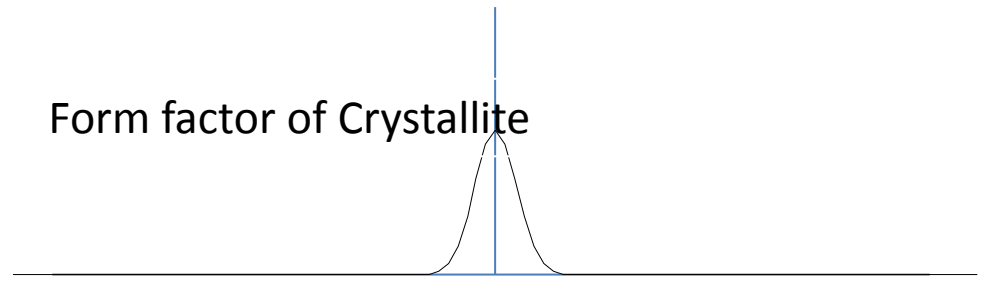
Crystallite



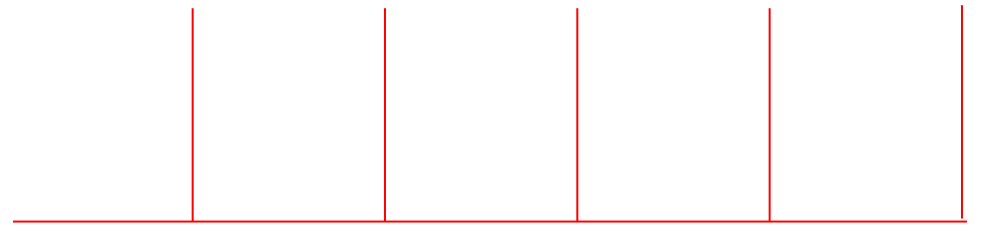
$$\text{(Crystallite)} = \text{(Lattice)} \times \text{(Crystallite shape)}$$

Scattering Pattern (Fourier Transform)

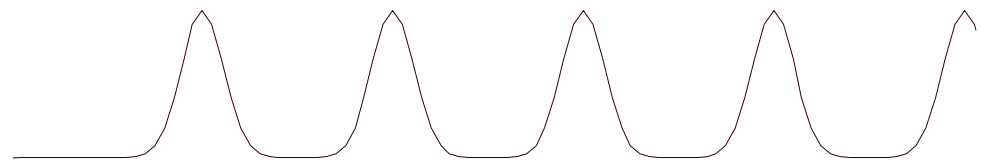
Form factor of Crystallite



FT of infinite Lattice of points



Scattering pattern



$$\text{FT(Crystallite)} = \text{FT(Lattice)} * \text{FT(Crystallite shape)}$$

convolute



Crystallite size estimation

- Scherrer equation

Dimensionless shape factor
(close to 1)

Wavelength

$$\tau = \frac{K\lambda}{\beta \cos \theta}$$

Bragg angle

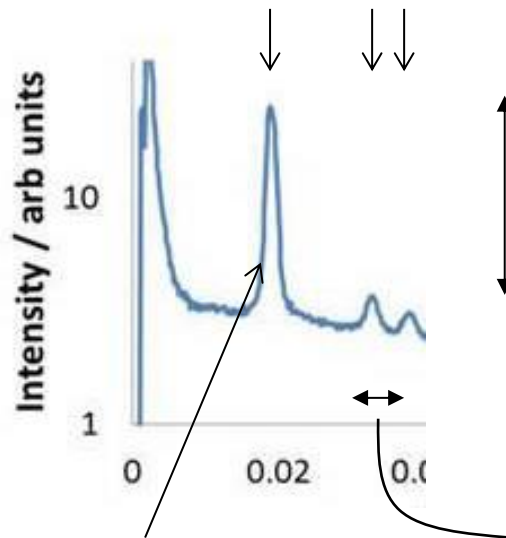
Mean crystallite size
(units: as λ)

Line broadening
(full width half maximum)
(in radians)

- Note: broadening might also come from *instrument (beam shape); polydispersity*

Summary

Relative positions:
symmetry

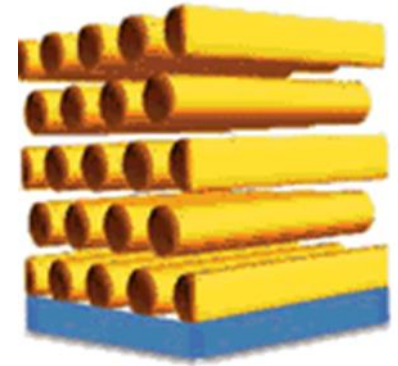


Peak position:
unit cell size
(lattice
parameter)

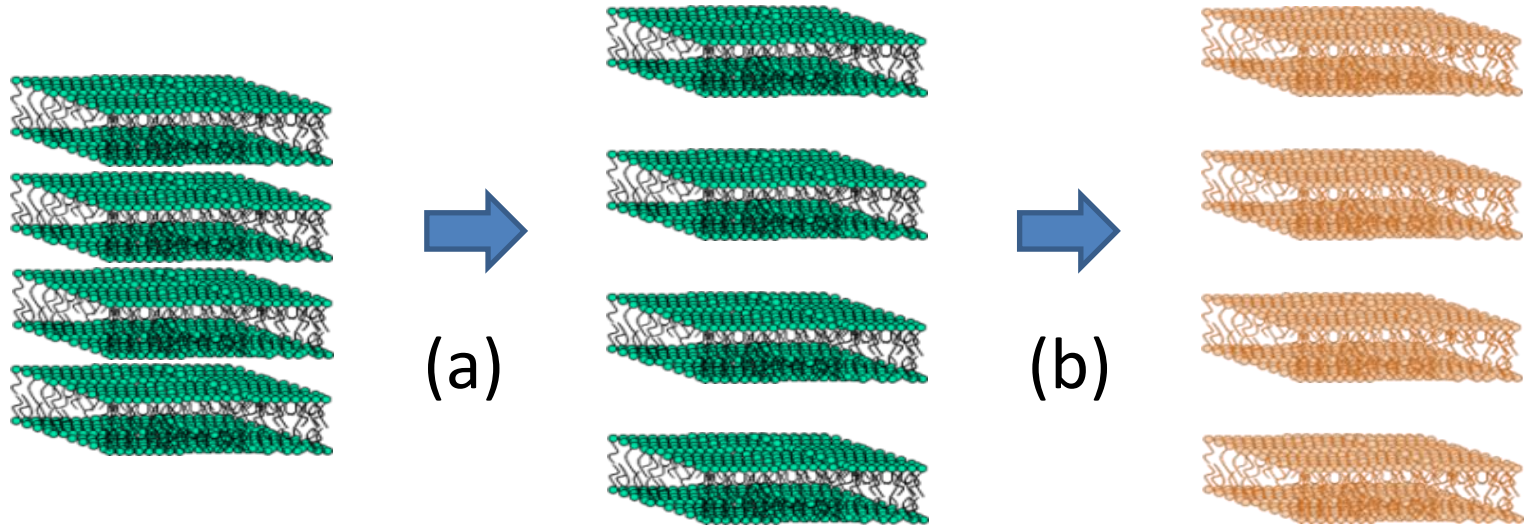
Peak heights:
Electron density within
unit cell (ie shape / size /
composition of each
cylinder)

Peak widths:

- Finite number of repeats
- OR
- Polydispersity
- Instrument: beam broadening



Task (2)



(a) Add water: bilayers move further apart

(b) Add metal nanoparticles that don't change spacing but adhere to interface

Discuss qualitatively what the scattering pattern looks like and how it changes