

PAUL SCHERRER INSTITUT



Marco Calvi :: ID group :: Paul Scherrer Institute

Hall Probe Measurements in Insertion Device

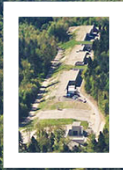
Tutorial – IMMW20, Diamond Light Source, June 4, 2017

- Introduction to Light Sources: PSI examples
- Dipole Radiation
- Undulator fundamental relation
- Measurement bench:
 - Alignment
 - K-value
 - RMS phase error
 - Orbit distortion
- Optimisation
- **An example of measurement & optimisation campaign**
- The operation based on magnetic measurements
- Open for questions



Alps

SwissFEL



SLS



Aare

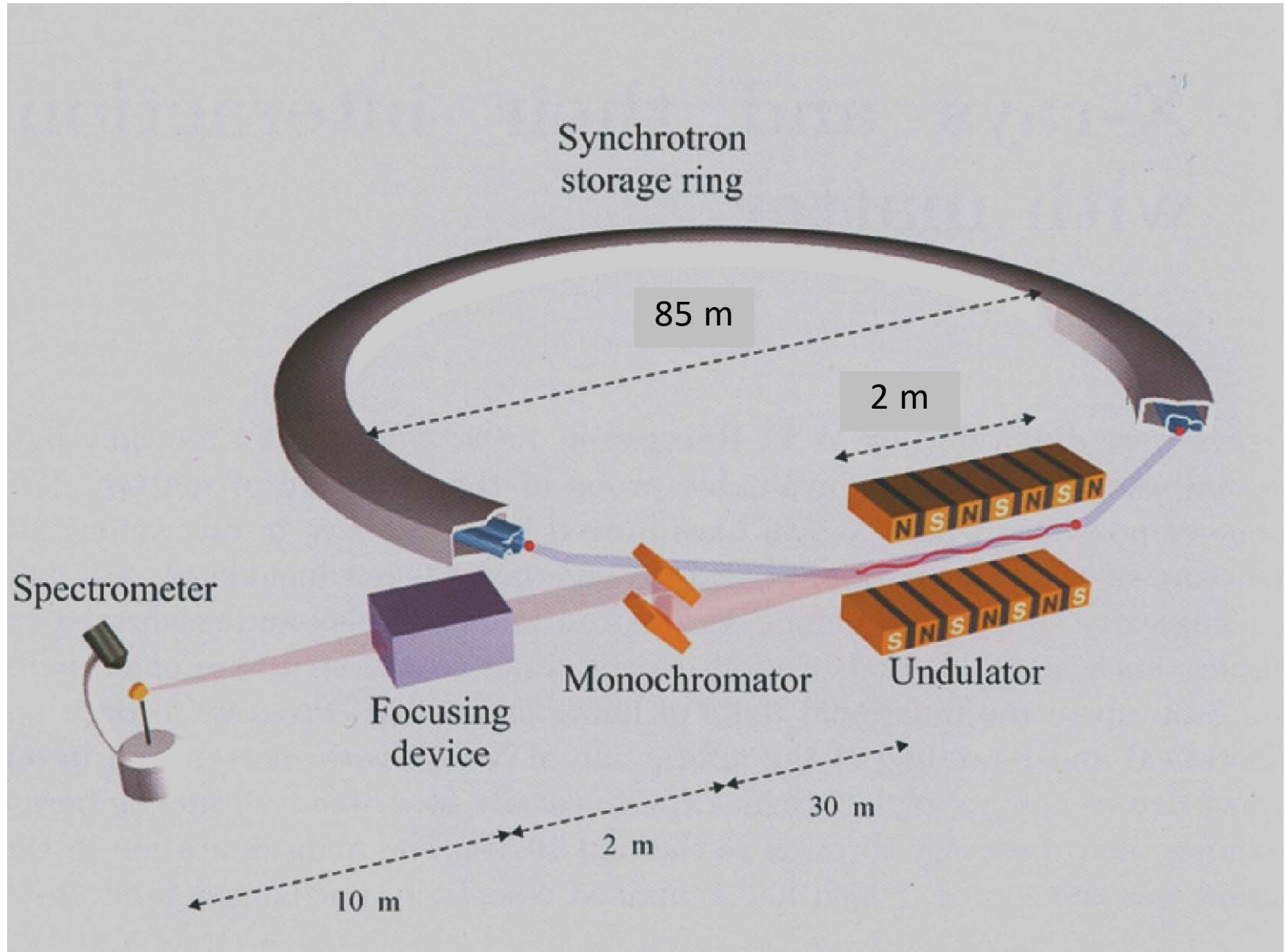
SLS – 2.4 GeV Light Source



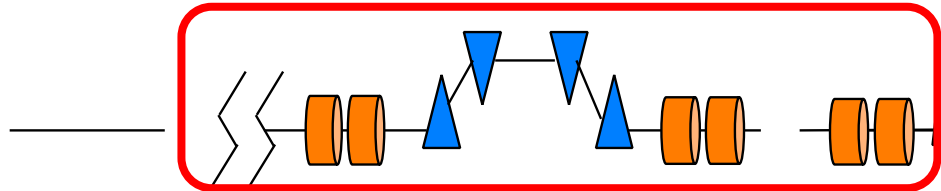
SLS – 2.4 GeV Light Source



SLS – 2.4 GeV Light Source





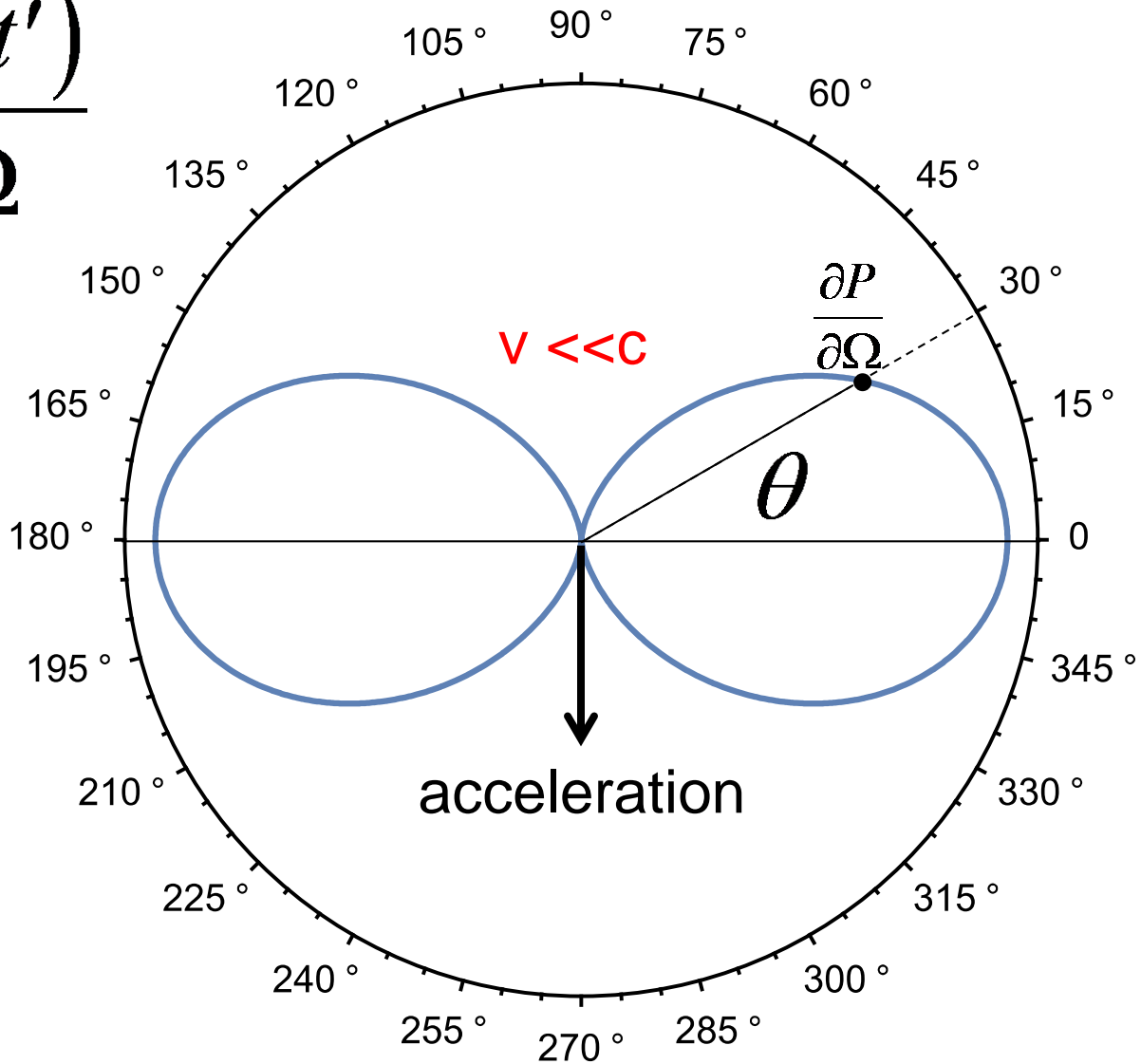




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- **Dipole Radiation**
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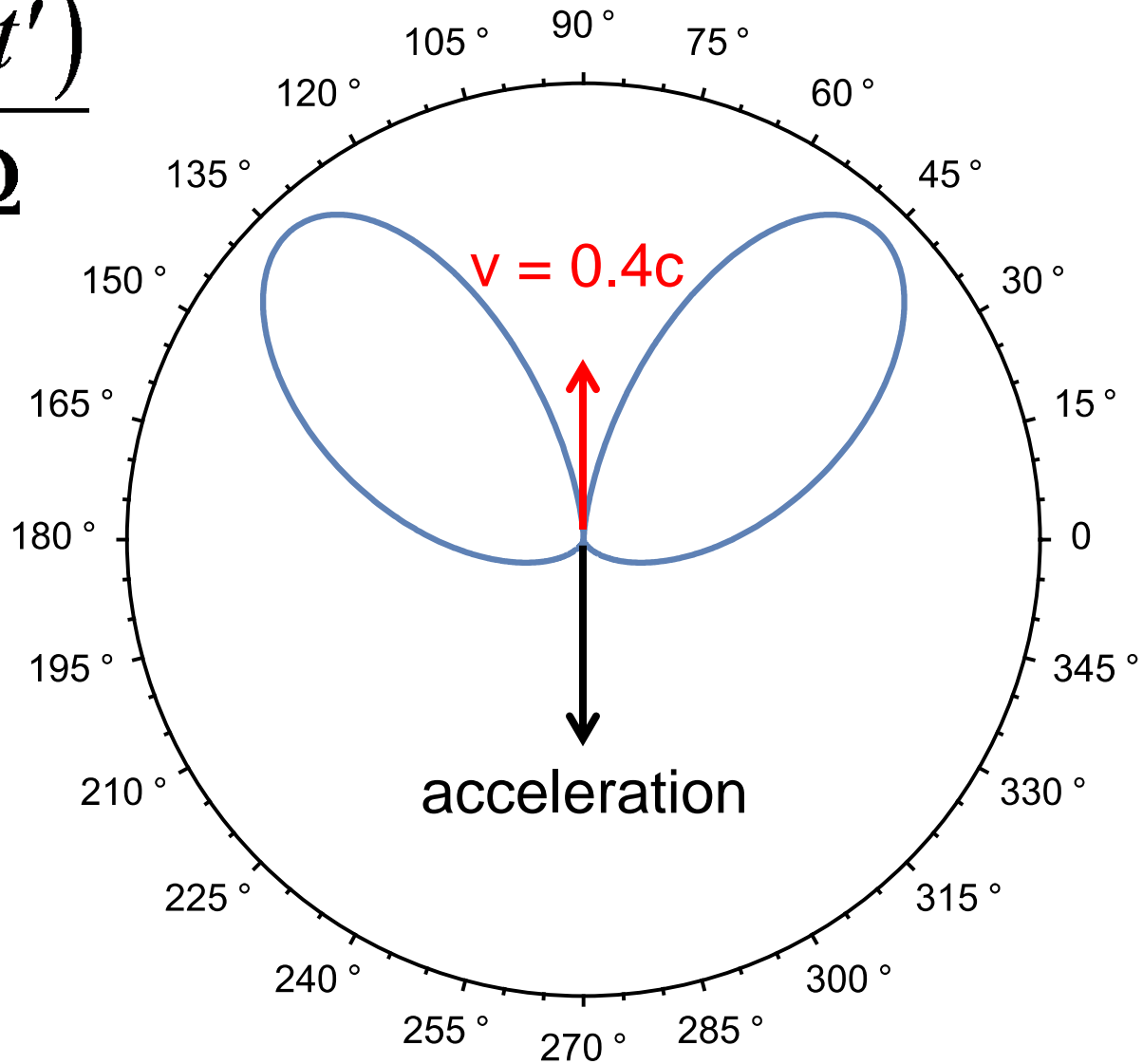
Dipole Radiation

$$\frac{\partial P(t')}{\partial \Omega}$$



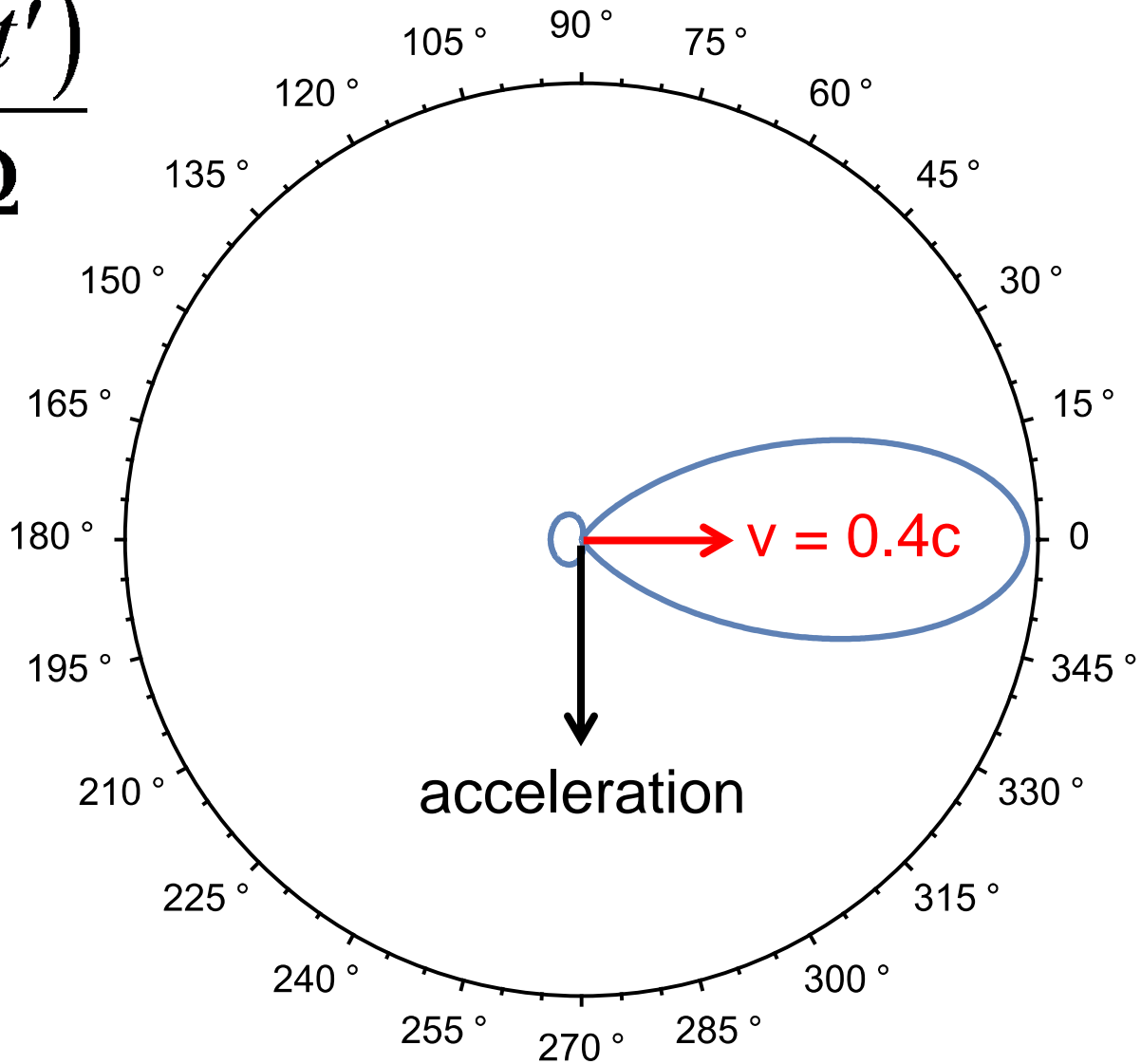
$$\frac{\partial P(t')}{\partial \Omega}$$

$$\partial \Omega$$



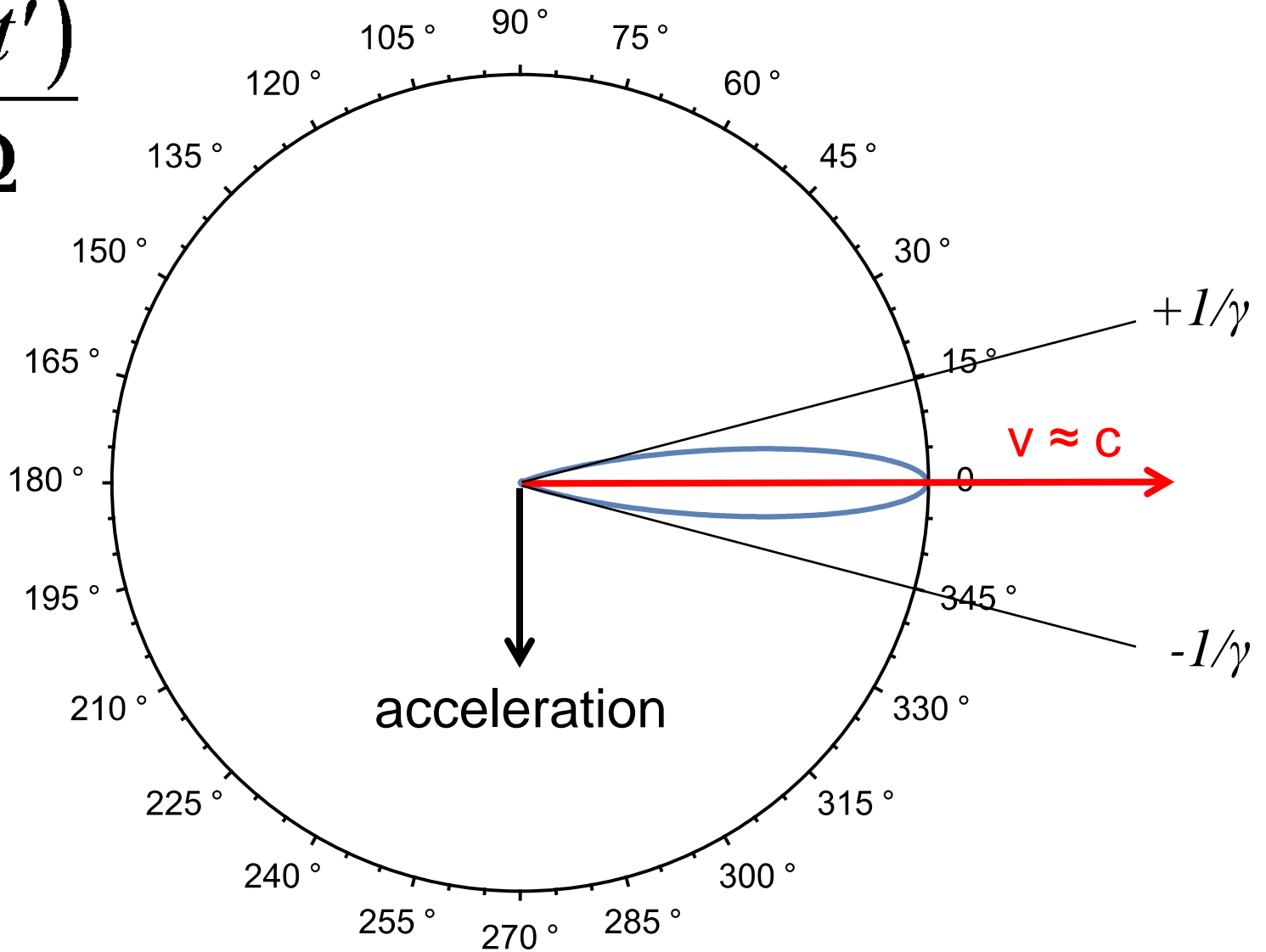
velocity \perp acceleration

$$\frac{\partial P(t')}{\partial \Omega}$$



velocity \perp acceleration

$$\frac{\partial P(t')}{\partial \Omega}$$



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Undulator Fundamental Relation

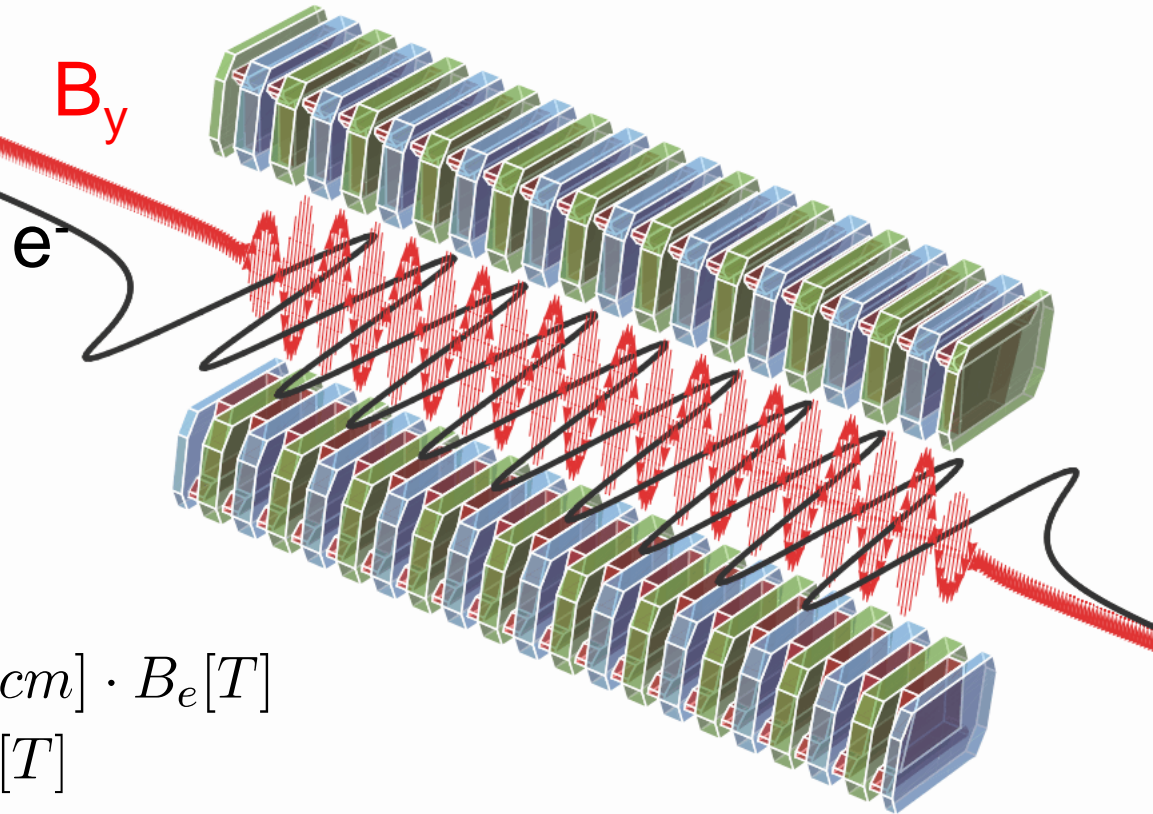
$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} \right)$$

λ_u period length

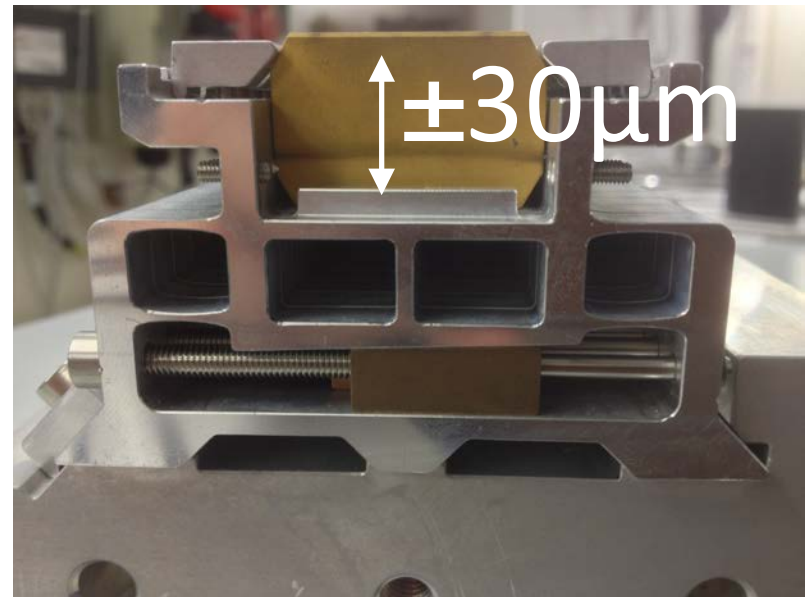
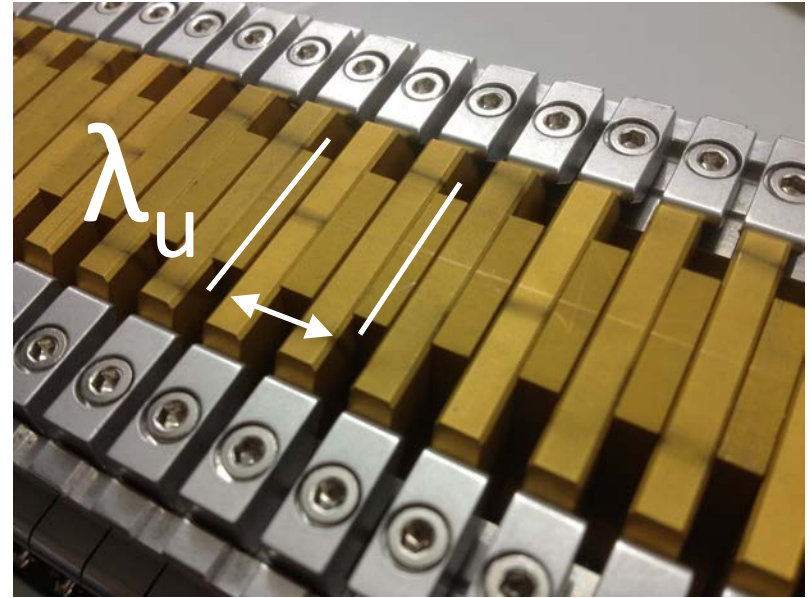
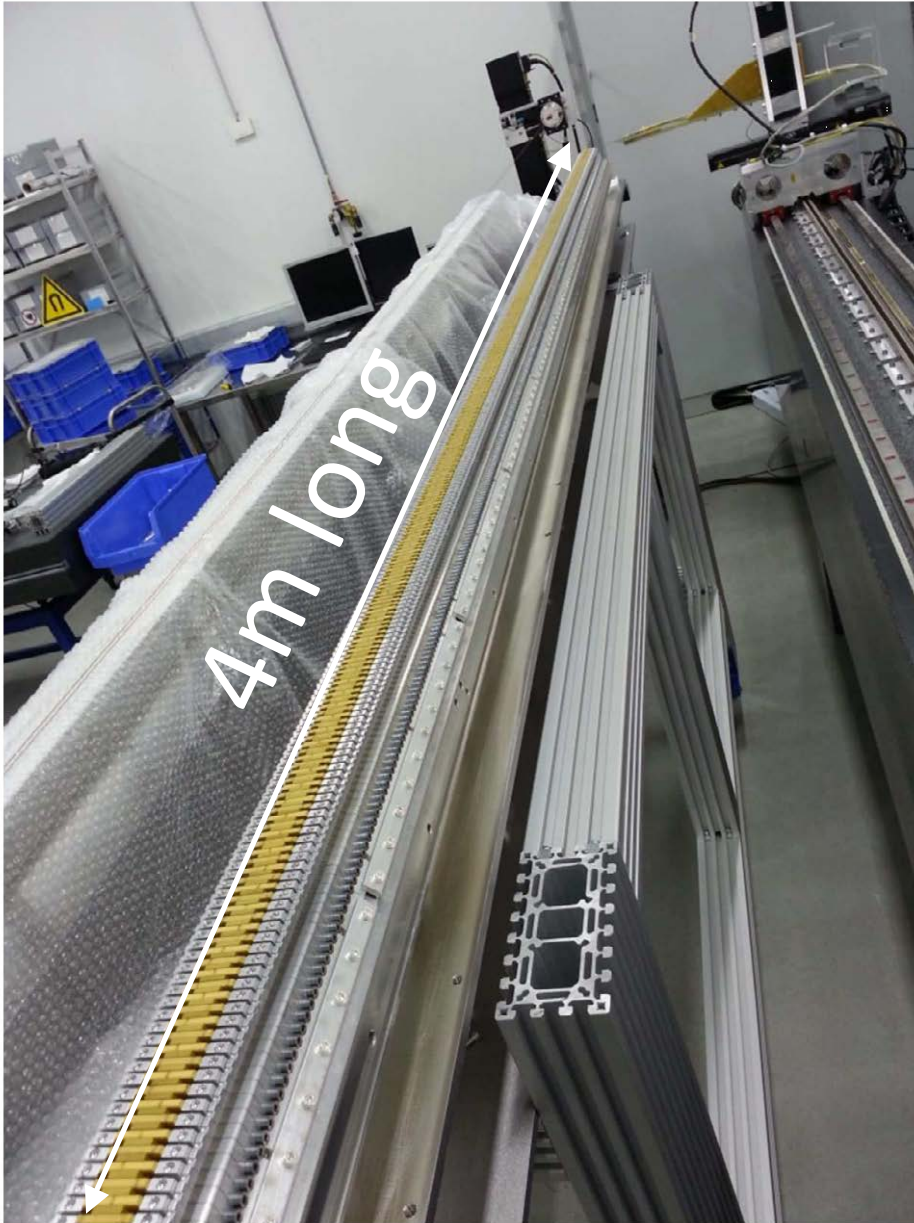
γ Lorentz factor

$$K = \frac{e}{2\pi m c} \lambda_u B_e$$

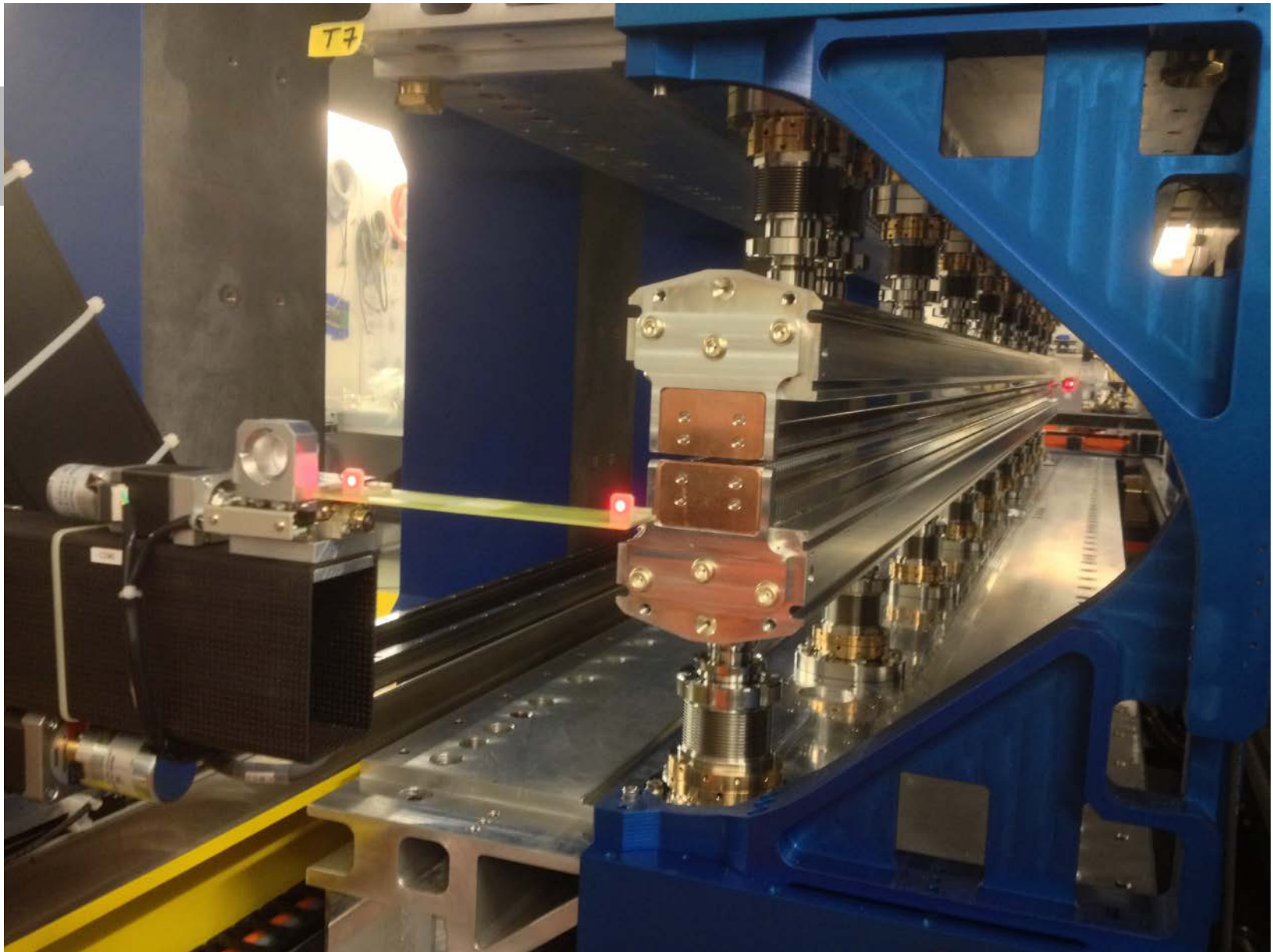
$$\begin{aligned} &\approx 0.9336 \cdot \lambda_u [cm] \cdot B_e [T] \\ &\approx \lambda_u [cm] \cdot B_e [T] \end{aligned}$$



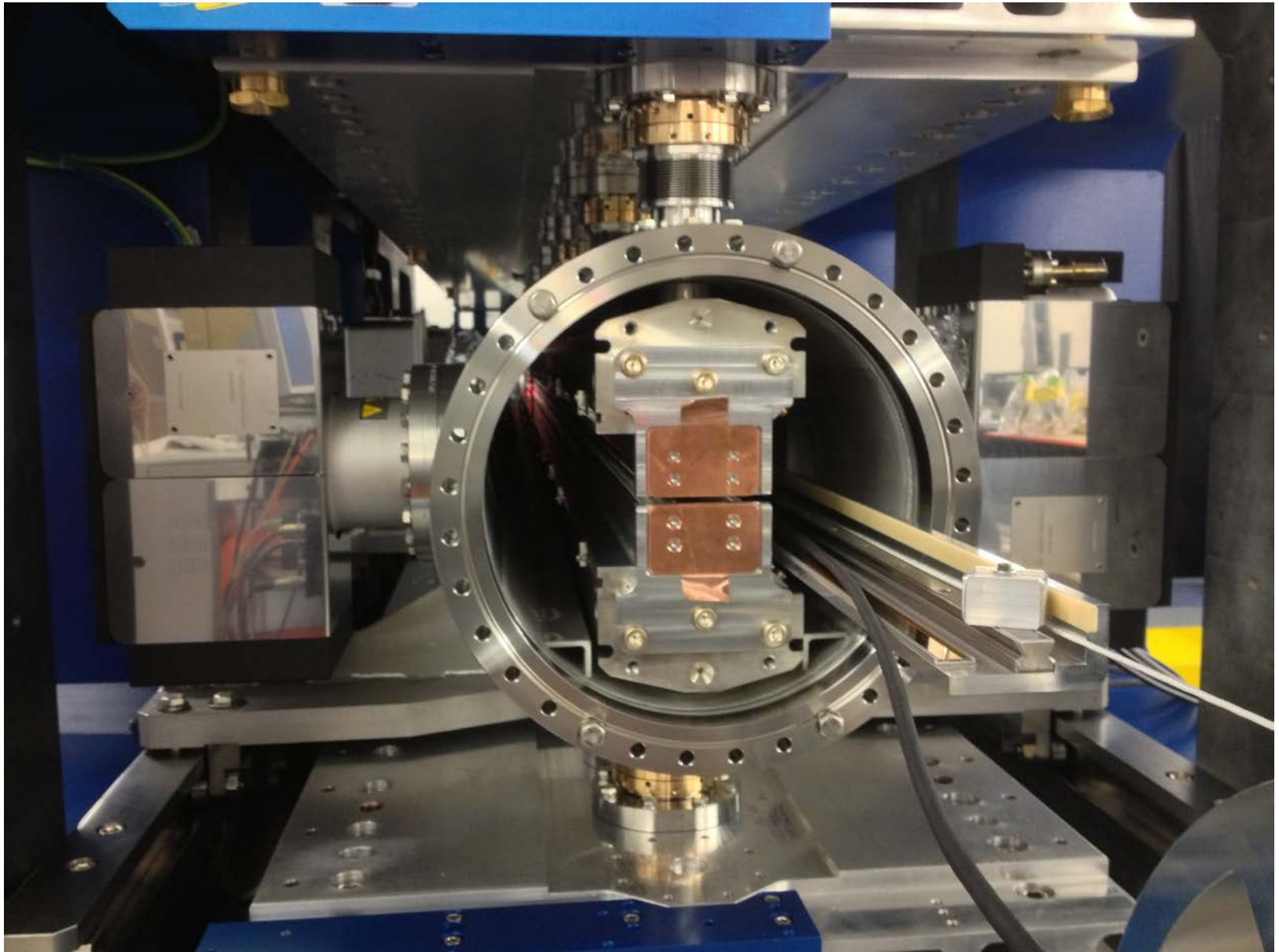
Aramis In-vacuum undulator



Aramis In-vacuum undulator

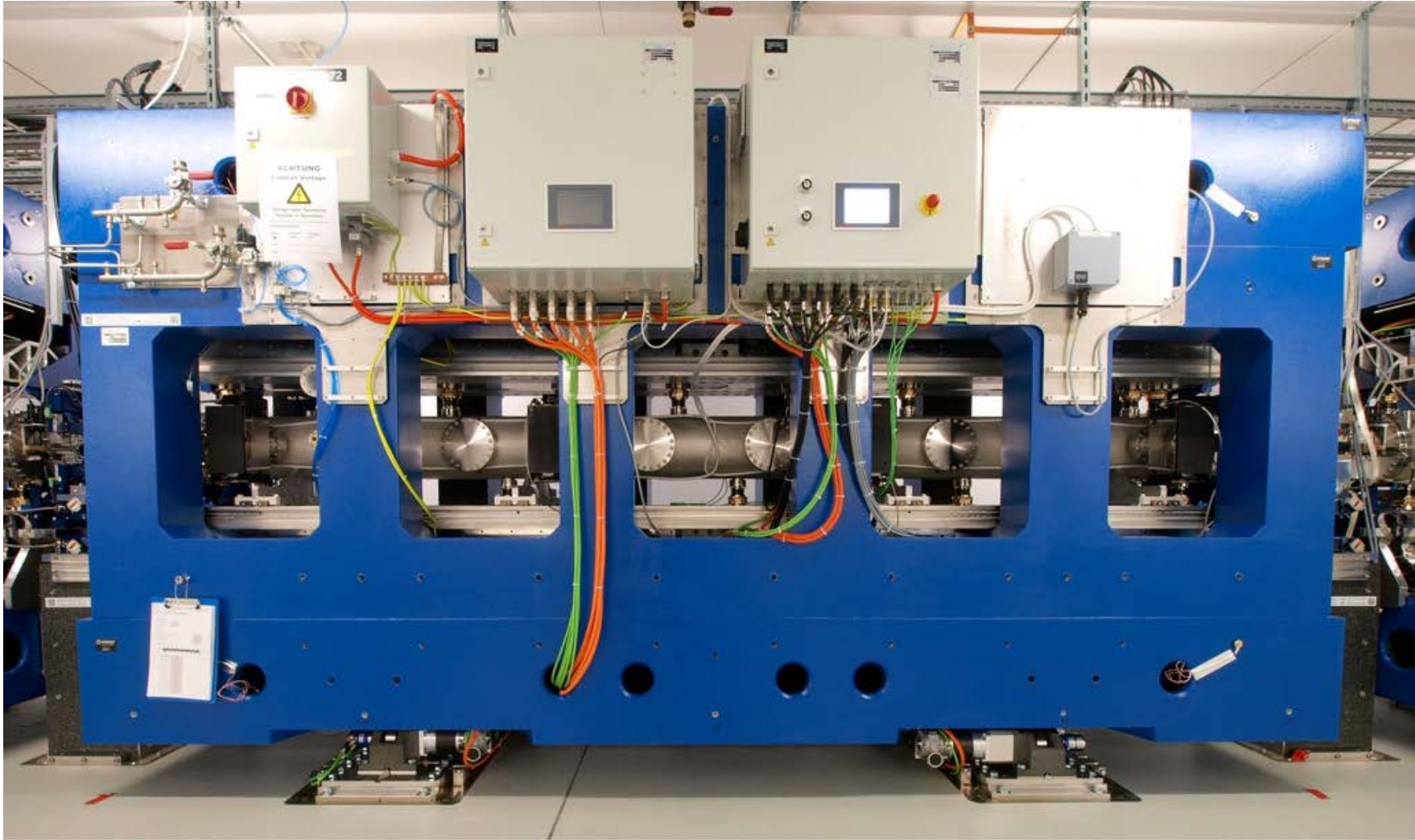


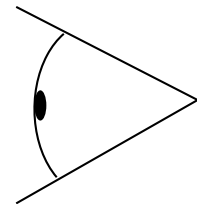
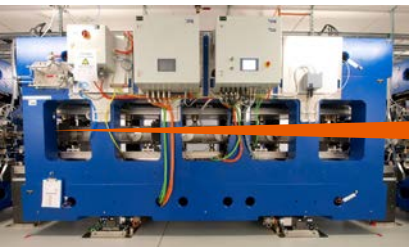
Aramis In-vacuum undulator



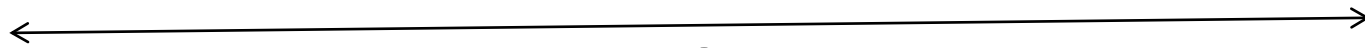


Aramis In-vacuum undulators





observer



150 m

Undulator Fundamental Relation

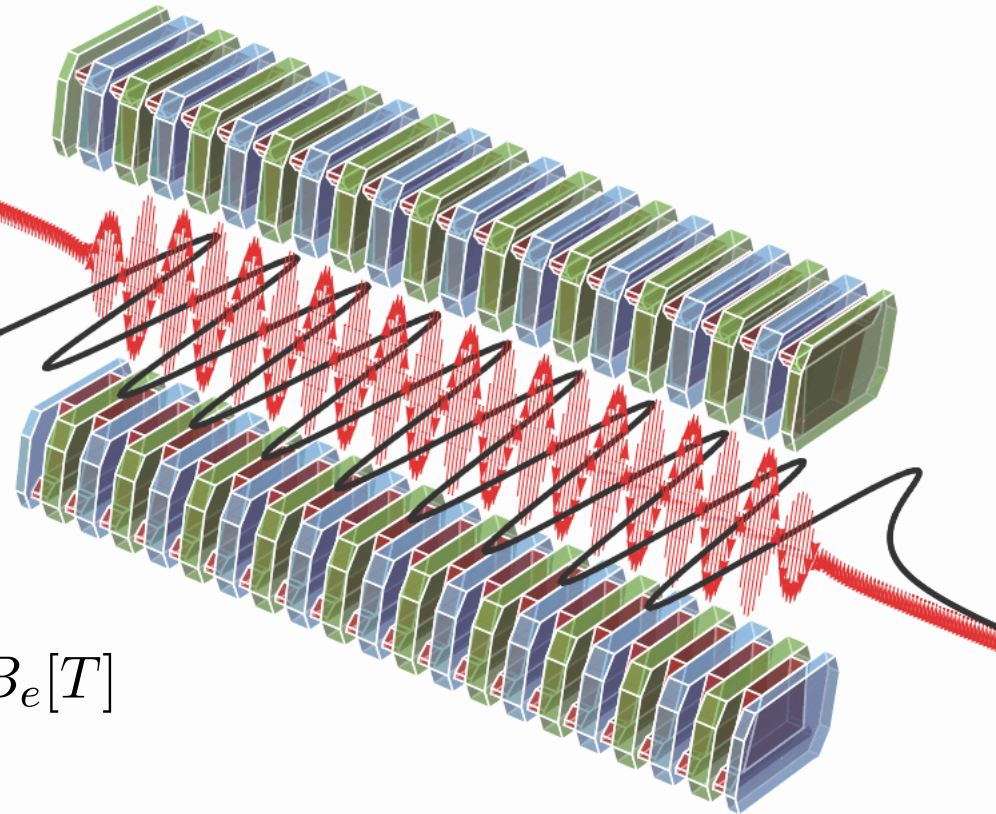
$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} \right)$$

λ_u period length

γ Lorentz factor

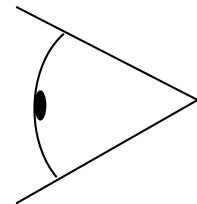
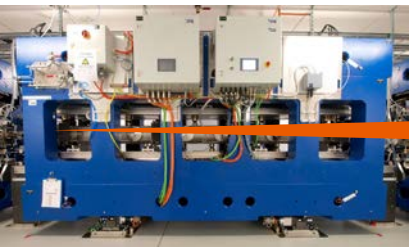
$$K = \frac{e}{2\pi m c} \lambda_u B_e$$

$$\begin{aligned} &\approx 0.9336 \cdot \lambda_u [cm] \cdot B_e [T] \\ &\approx \lambda_u [cm] \cdot B_e [T] \end{aligned}$$

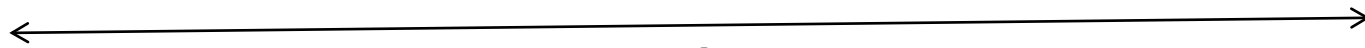


$$\lambda_n = \frac{\lambda_u}{2n\gamma} \left(1 + \frac{K^2}{2} + \theta^2 \gamma^2 \right)$$

θ Observation angle

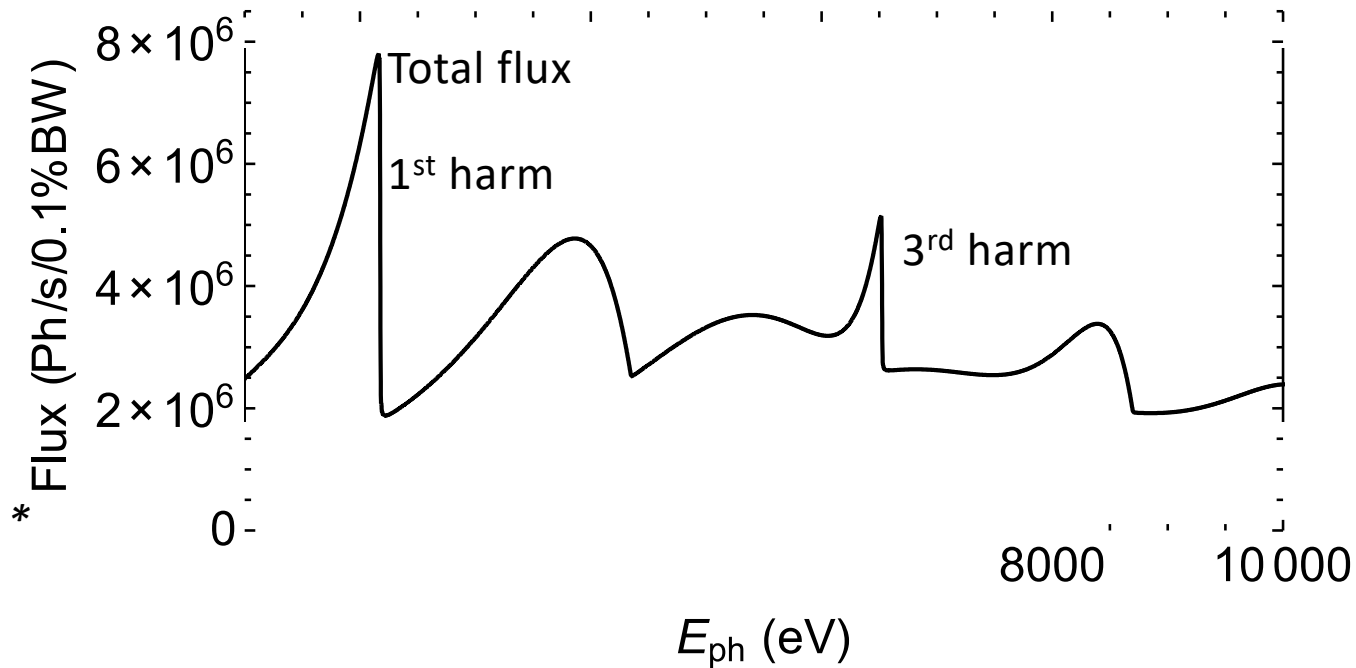


observer



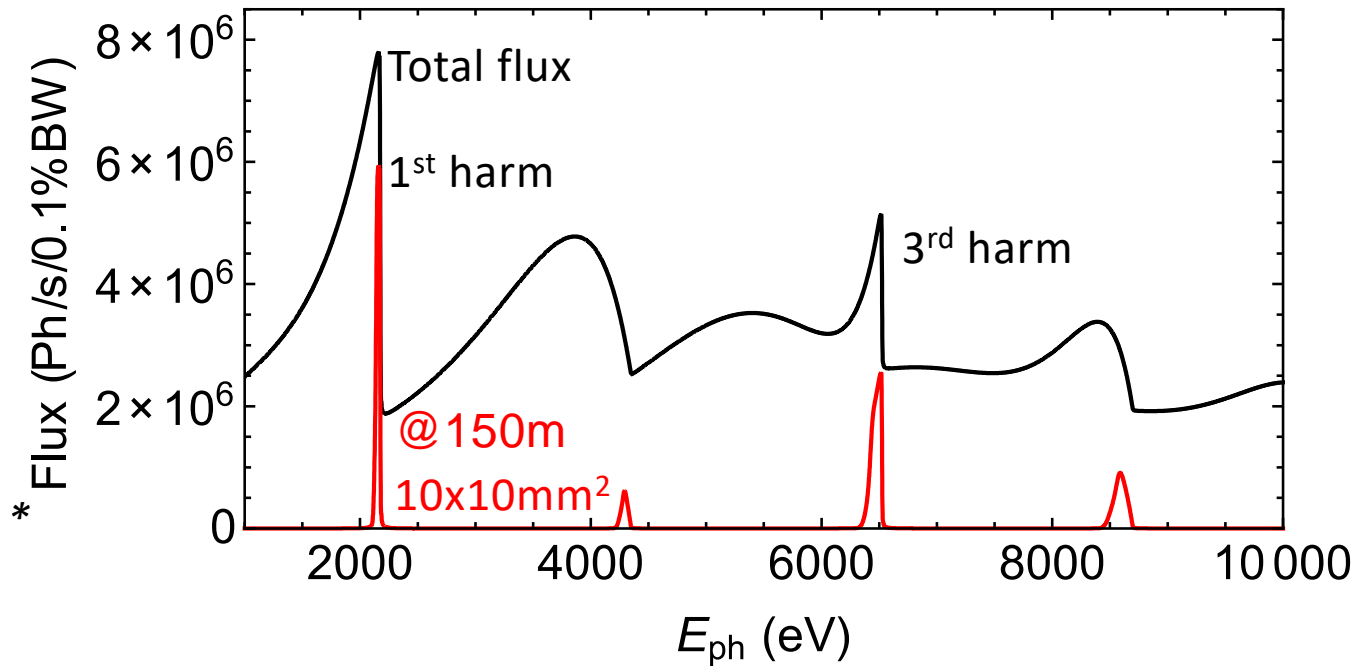
150 m

$$\lambda_n = \frac{\lambda_u}{2n\gamma} \left(1 + \frac{K^2}{2} + \theta^2 \gamma^2 \right)$$



*All calculations made with 1Hz repetition rate $\rightarrow 1/s =$ per shot
 Charge = 200pC

$$\lambda_n = \frac{\lambda_u}{2n\gamma} \left(1 + \frac{K^2}{2} + \theta^2 \gamma^2 \right)$$



*All calculations made with 1Hz repetition rate $\rightarrow 1/s =$ per shot

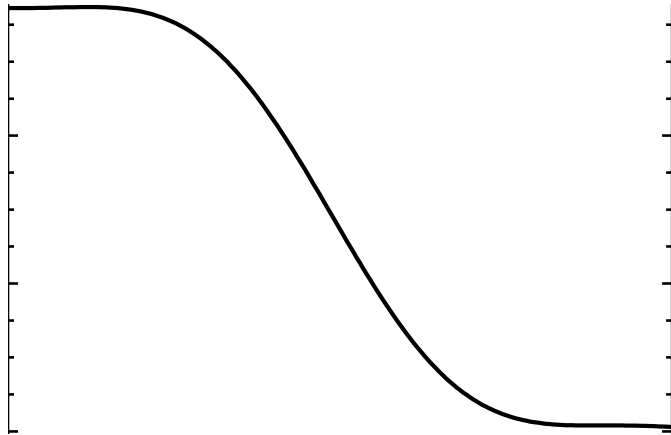
Charge = 200pC



$E=3.0\text{GeV}$ & $K=1.8$ – 1st harmonic

@150m

Total flux

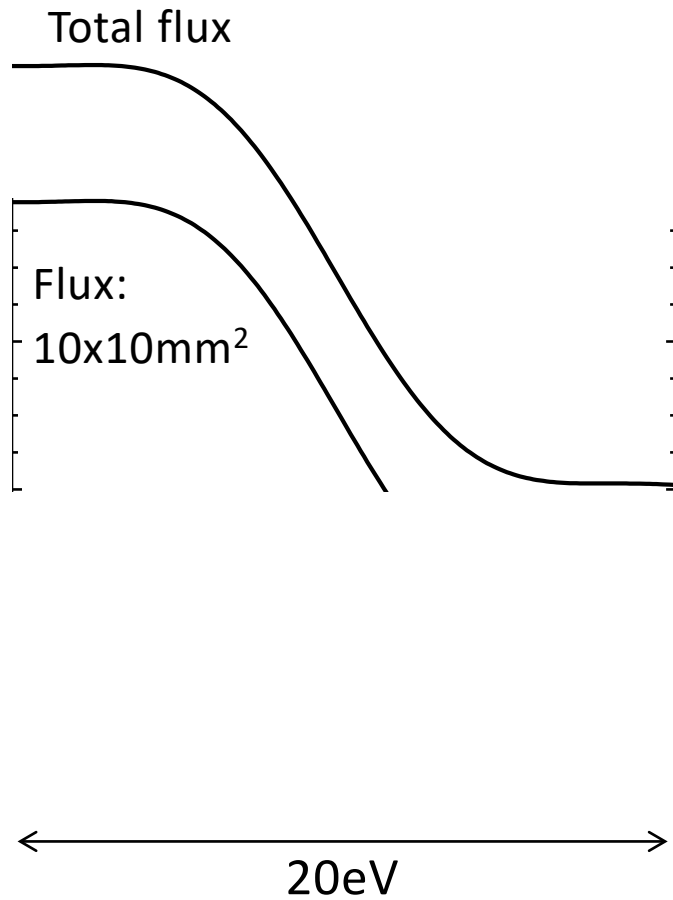


20eV



$E=3.0\text{GeV}$ & $K=1.8$ – 1st harmonic

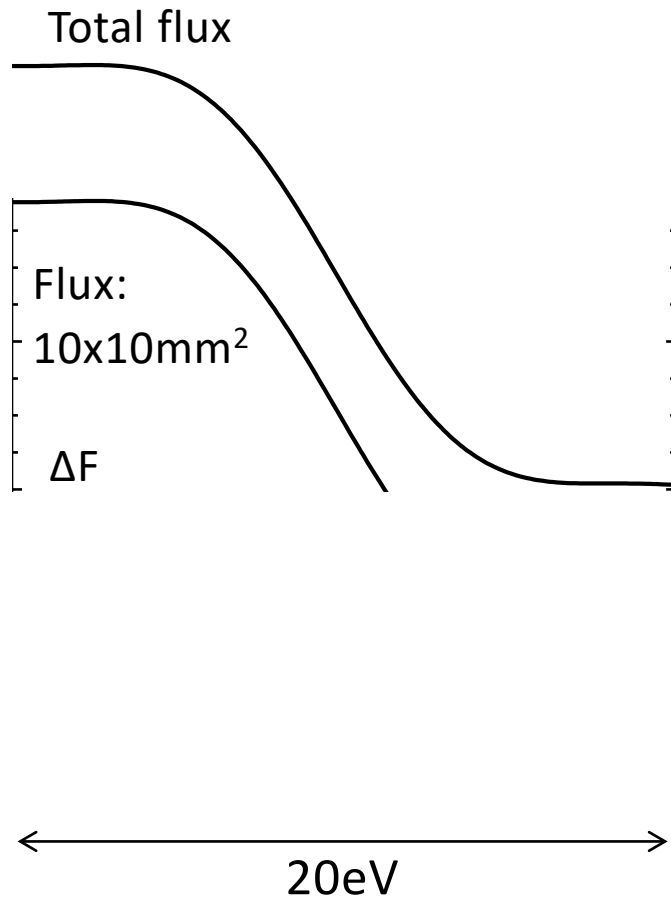
@150m



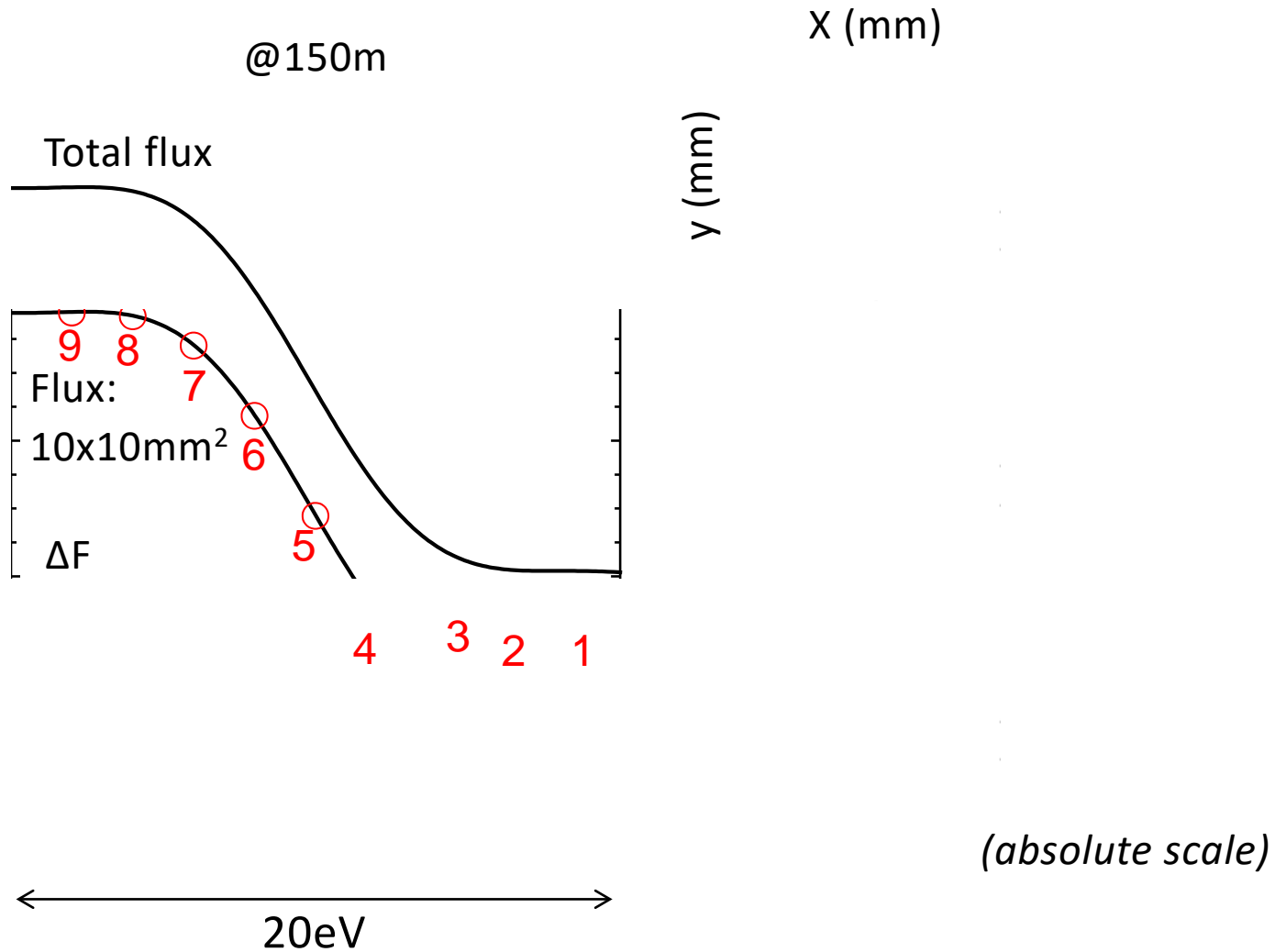


E=3.0GeV & K=1.8 – 1st harmonic

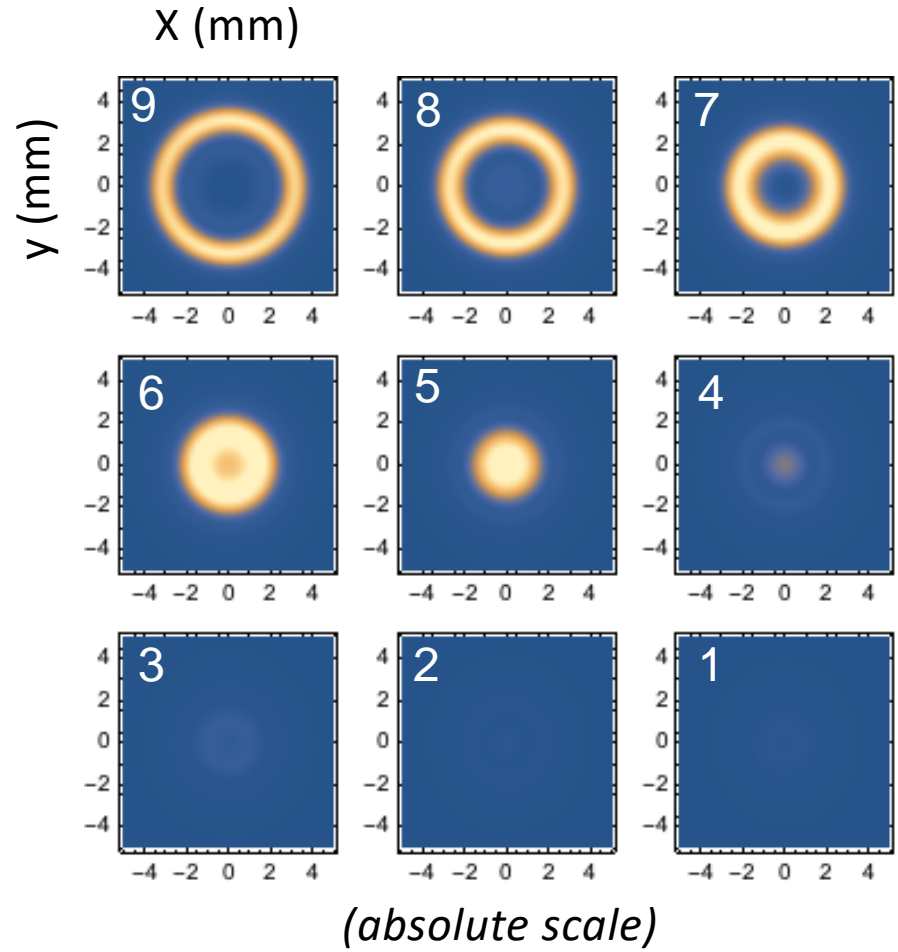
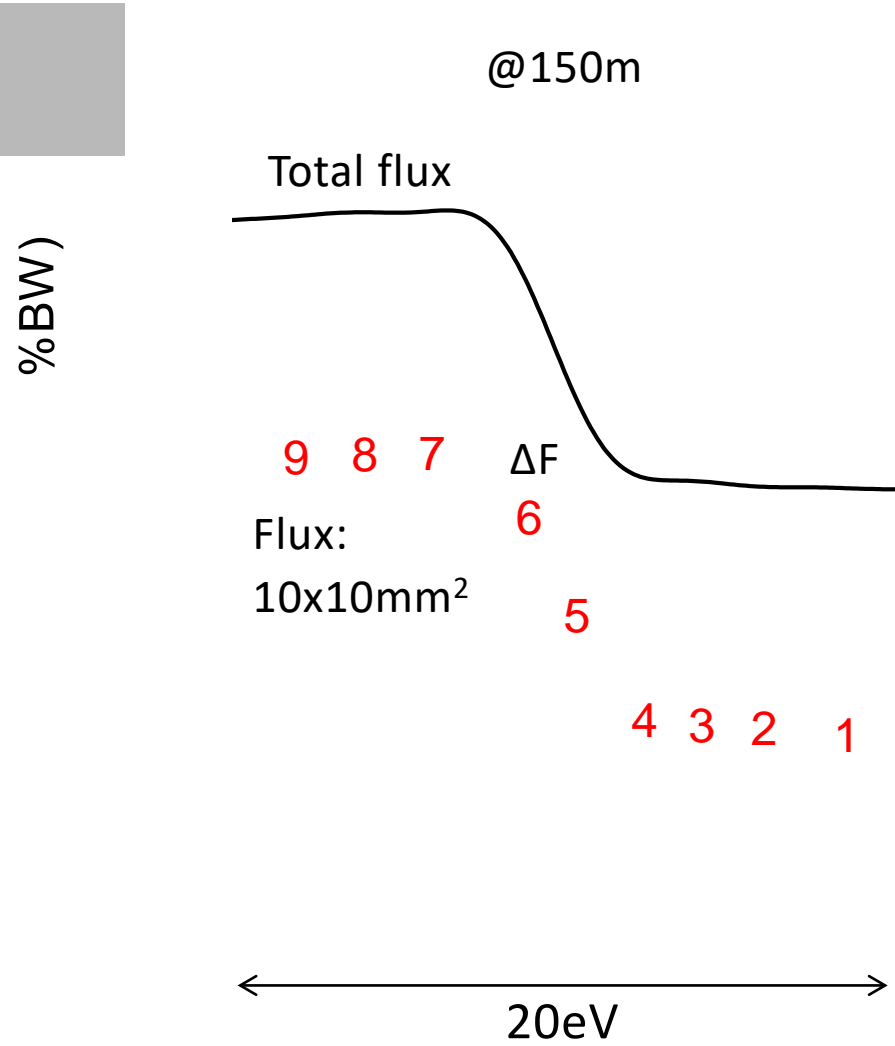
@150m



E=3.0GeV & K=1.8 – 1st harmonic

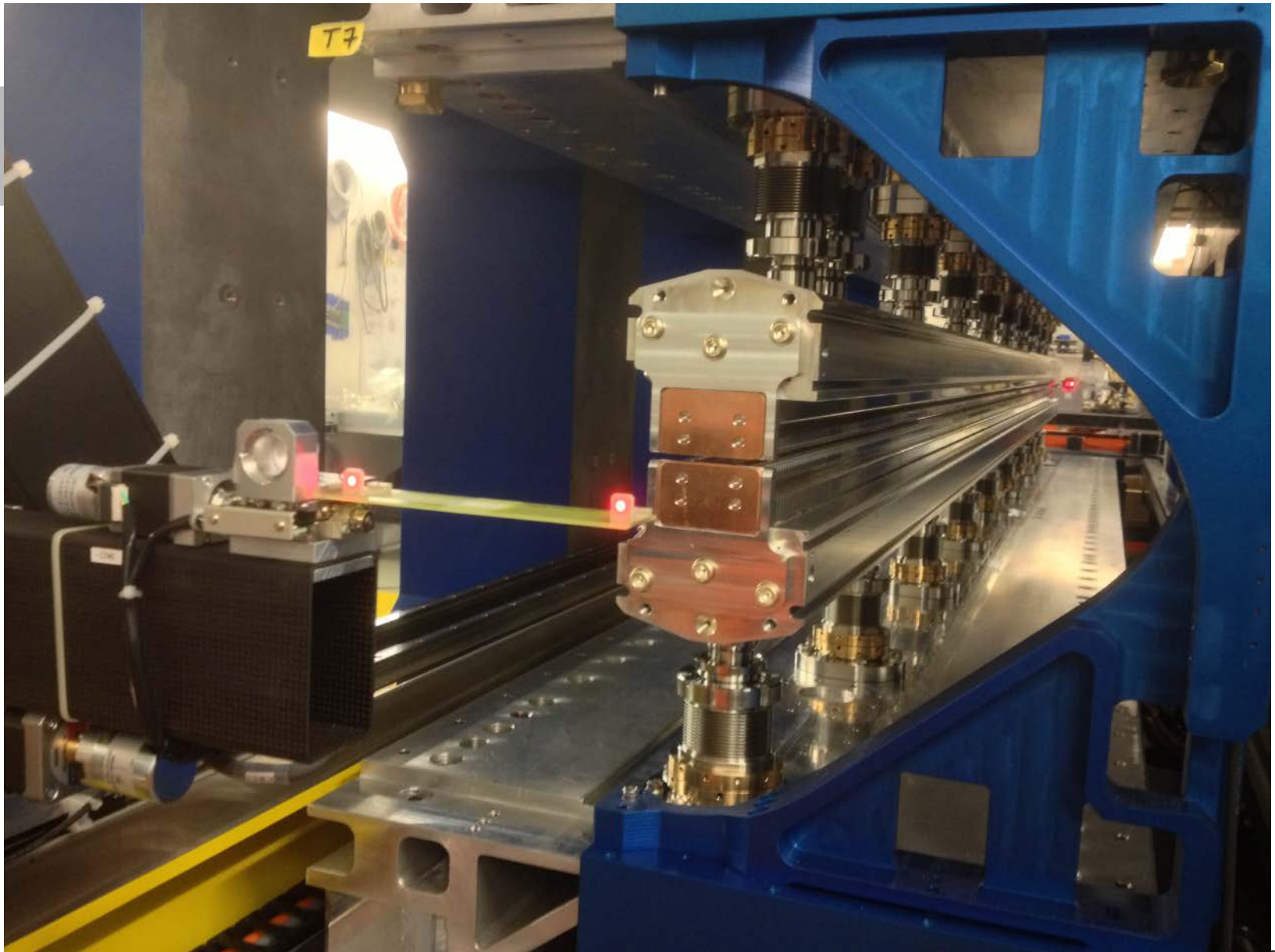


E=2.0GeV & K=1.8 – 3rd harmonic

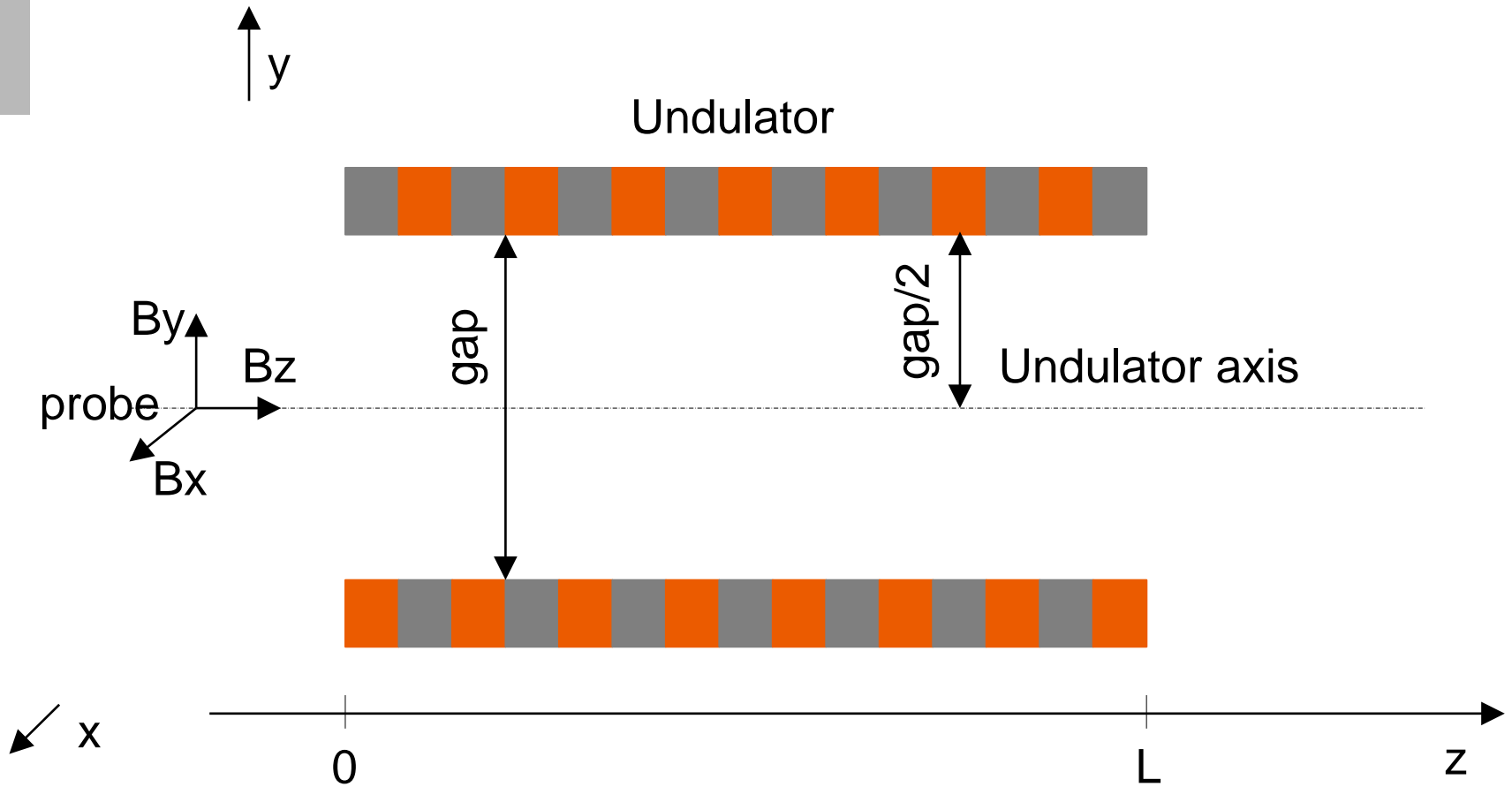


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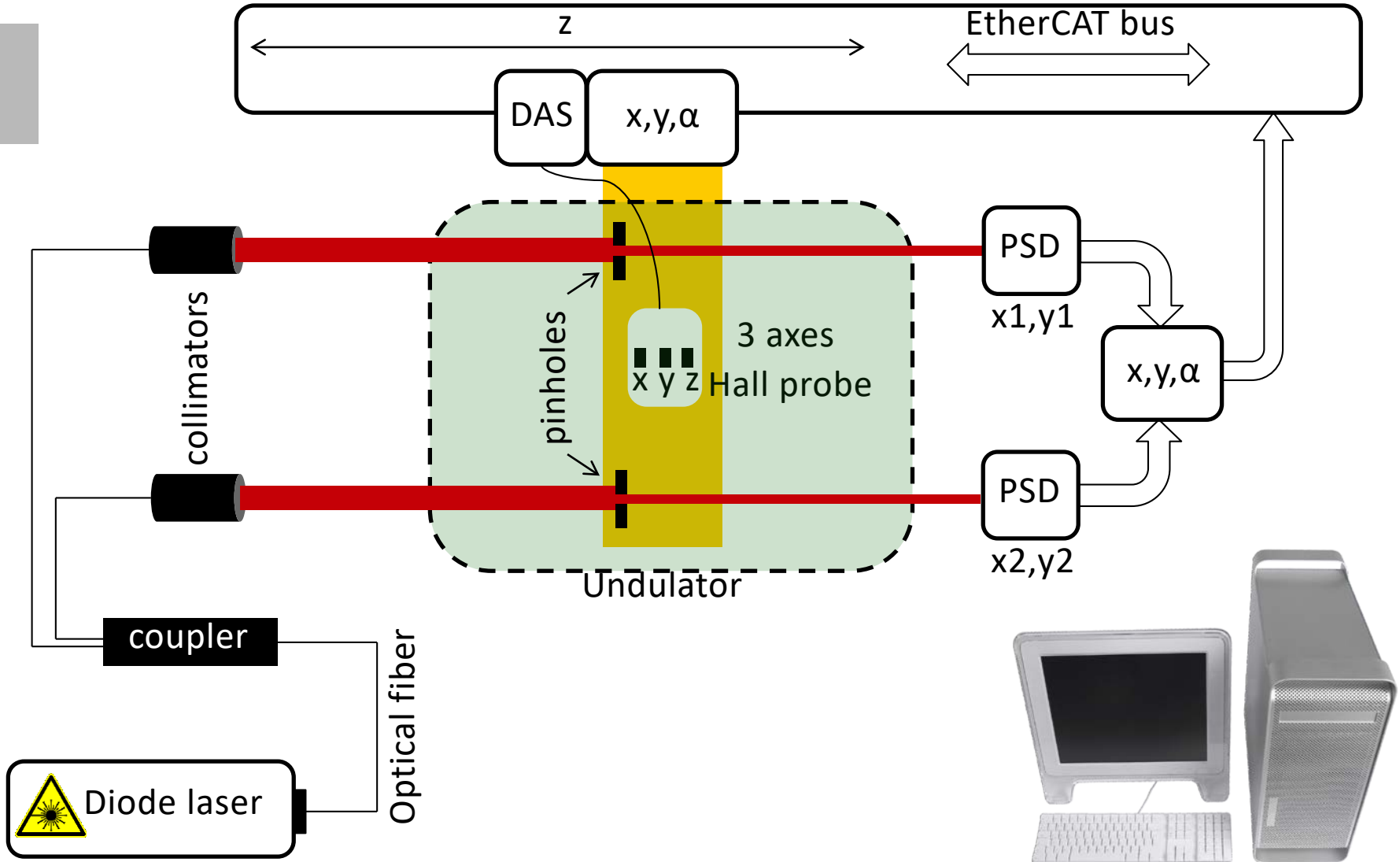
Measuring bench



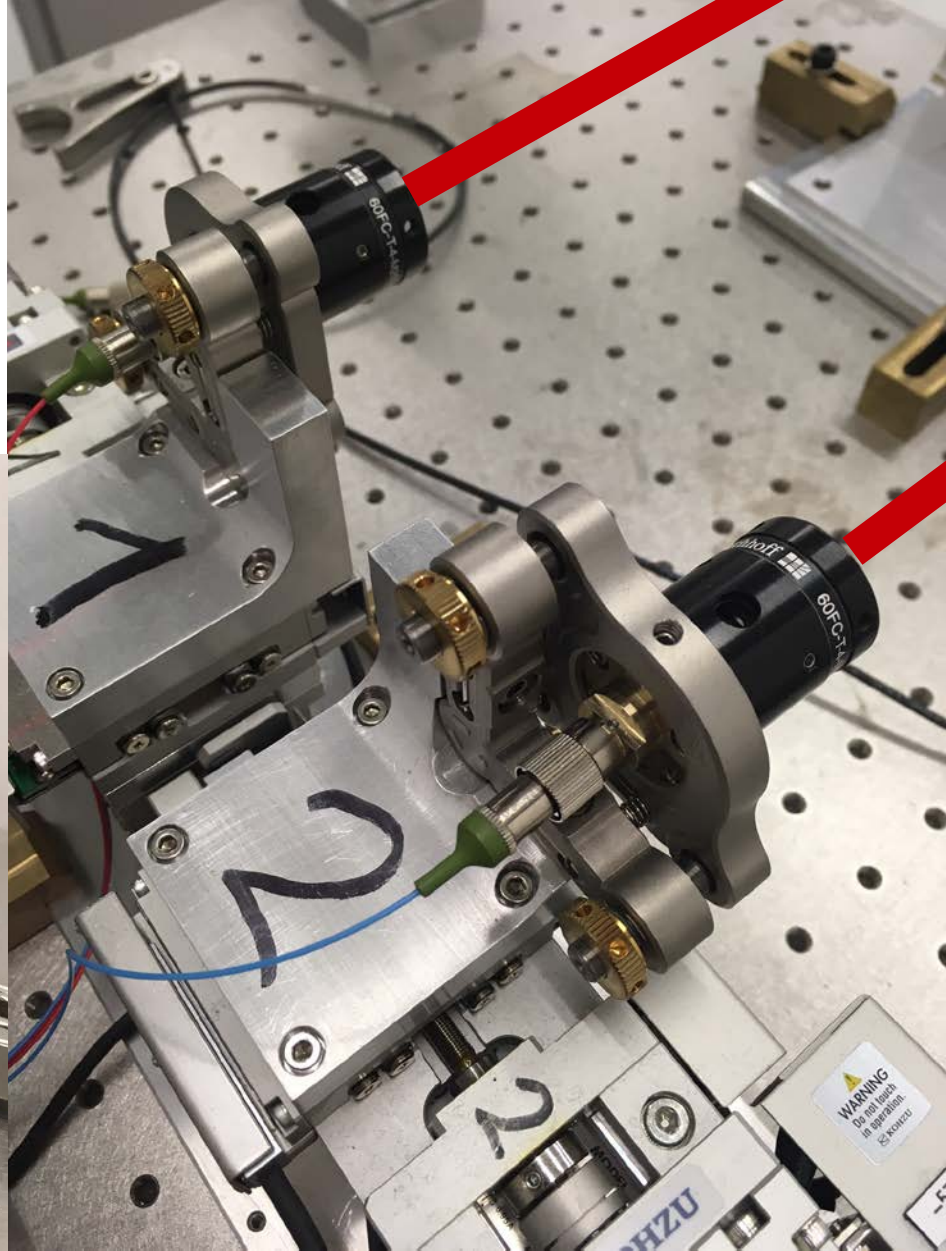
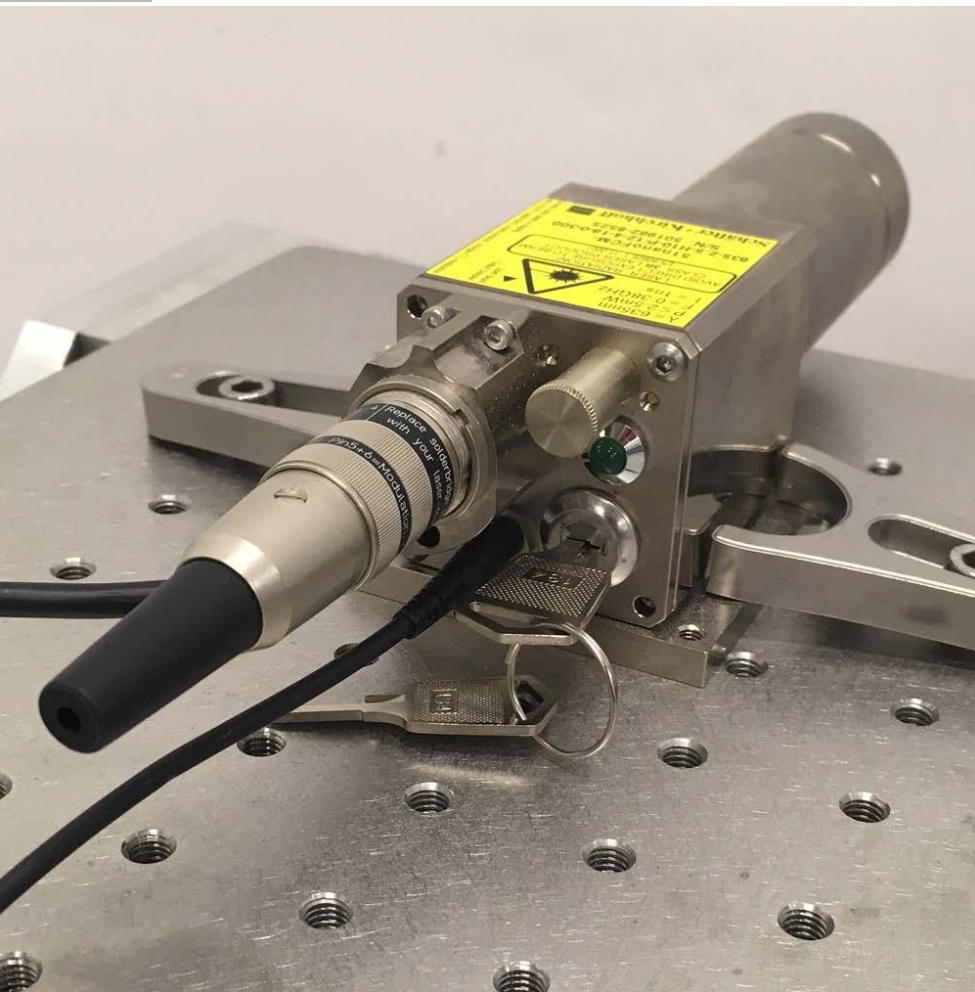
Measuring bench



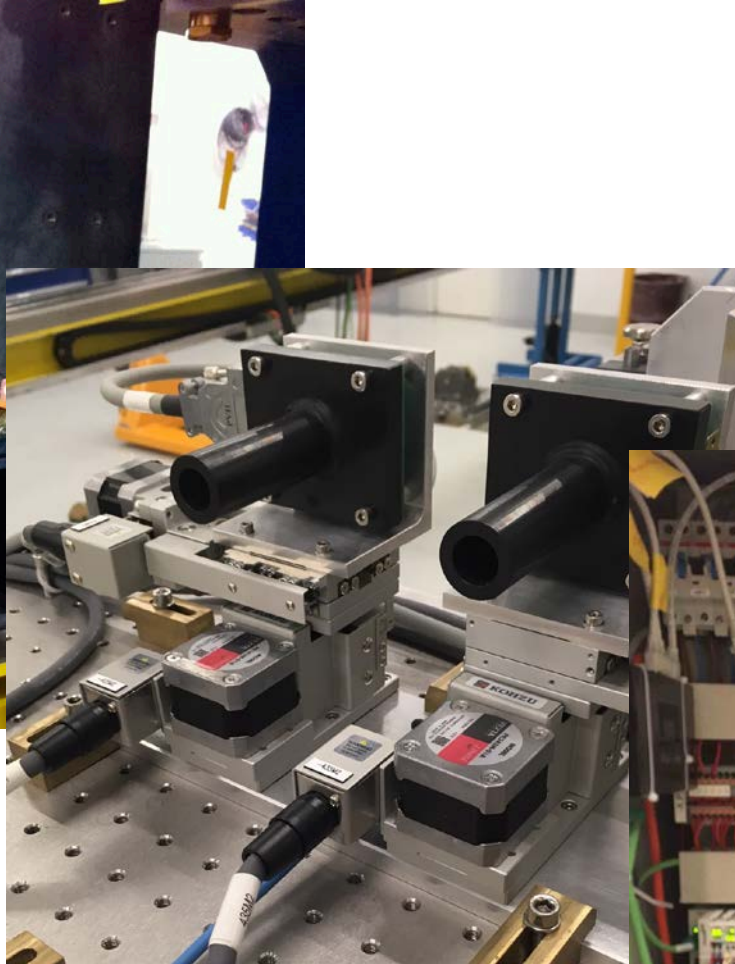
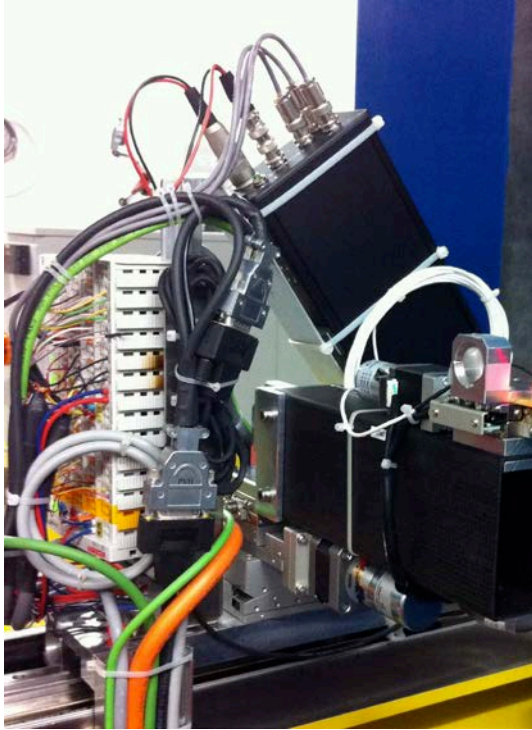
Measuring bench



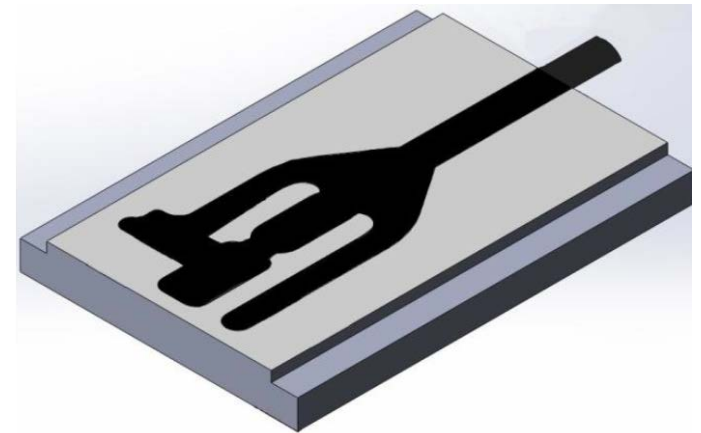
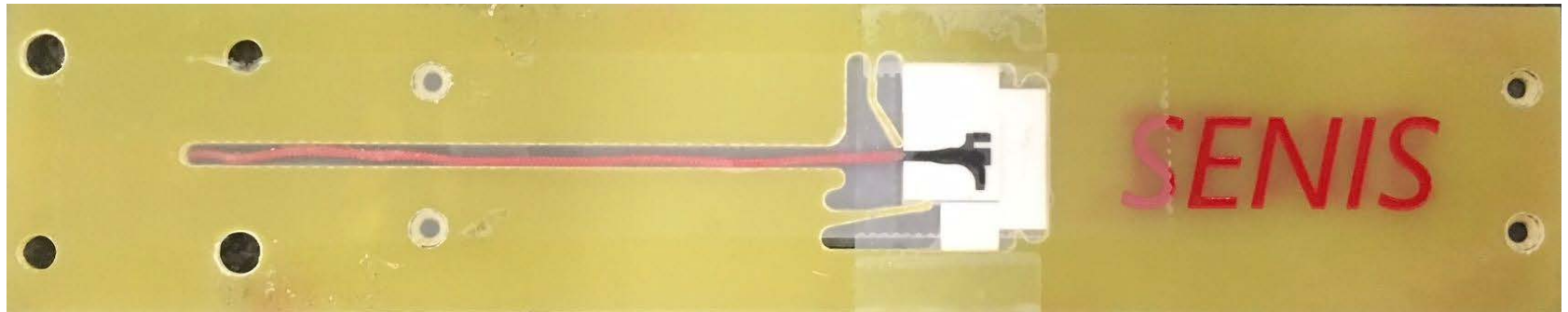
Measuring bench



Measuring bench



Measuring bench



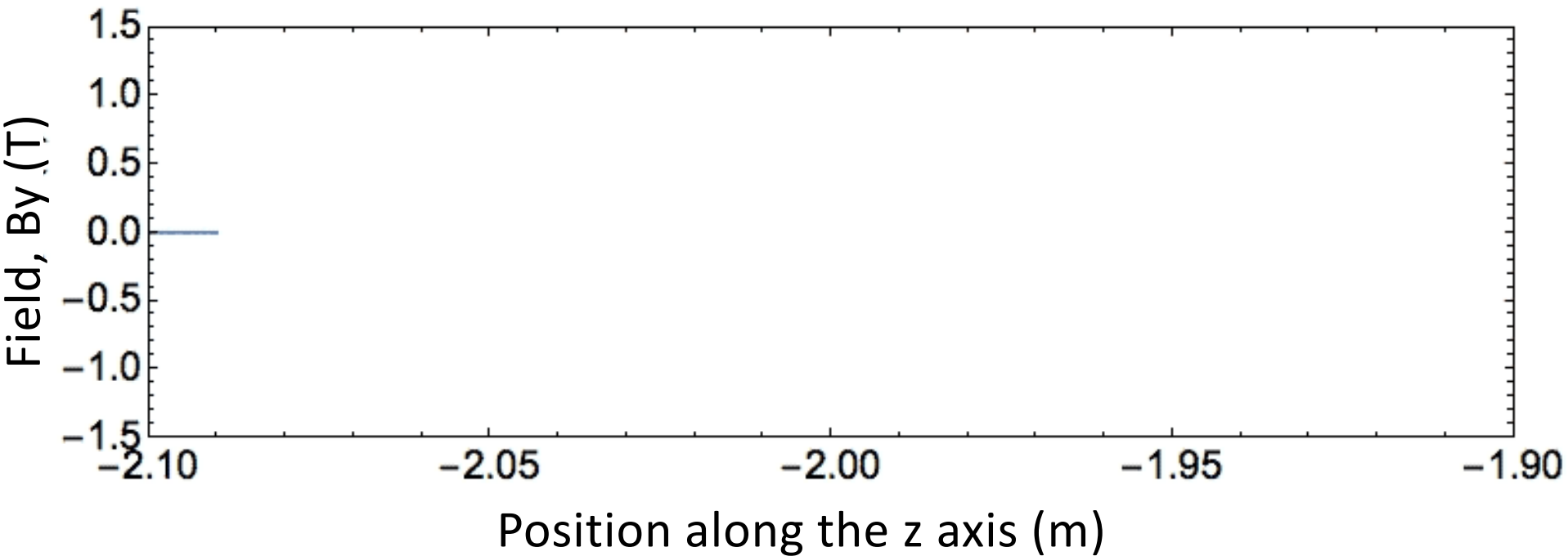
Dimensions: 1.4x10.5x15.0mm³

Mutual orthogonality: $<2^\circ$

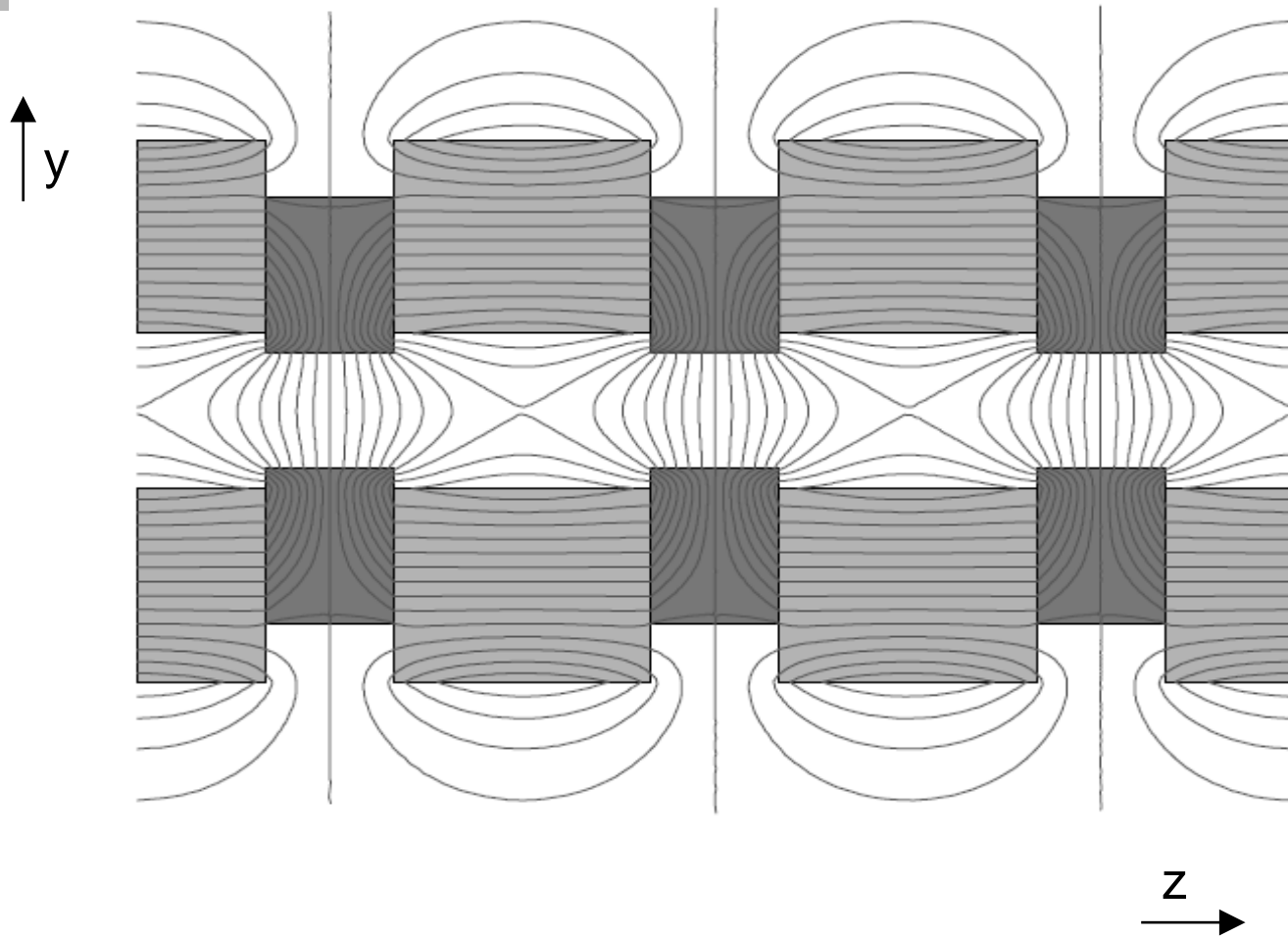
Angular accuracy with respect to the reference surface: $\pm 2^\circ$

The three probes are all at the same height of 0.7 (middle of the probe) and horizontal position, while they are spaced longitudinally by 2mm

Measurement example – Raw data



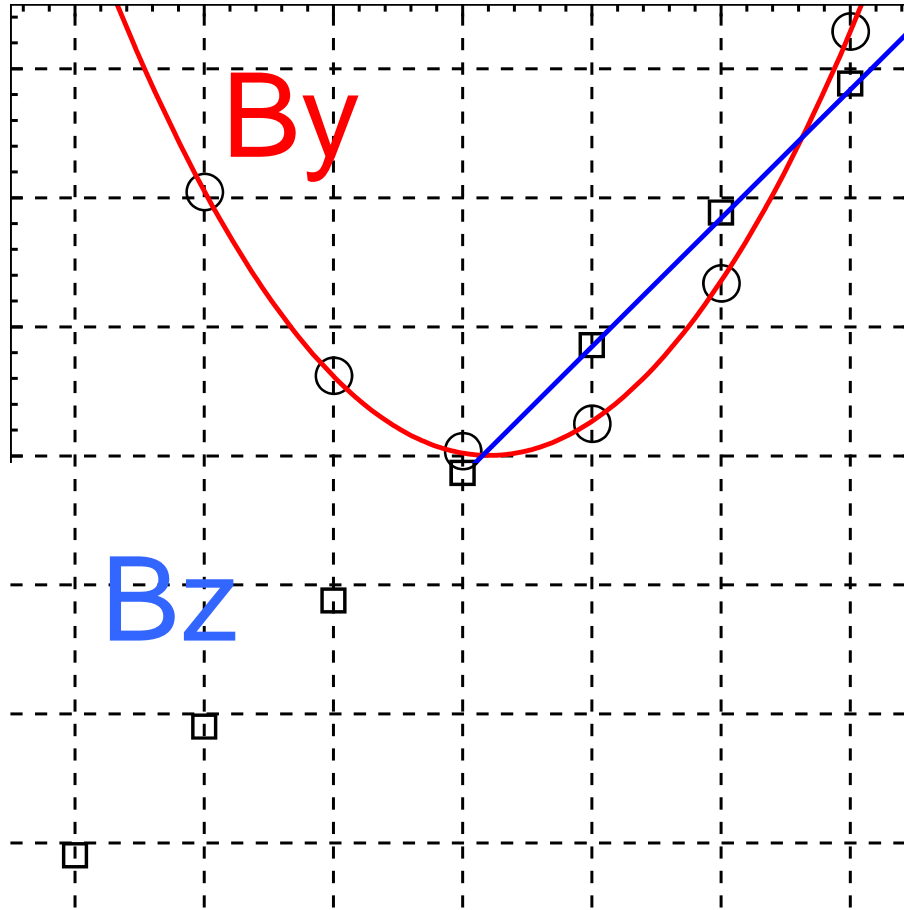
axis definition: $\frac{\partial B_y}{\partial y} = 0$ or $B_z = 0$



Alignment

Prototype

□ Height error from Bs (mm)

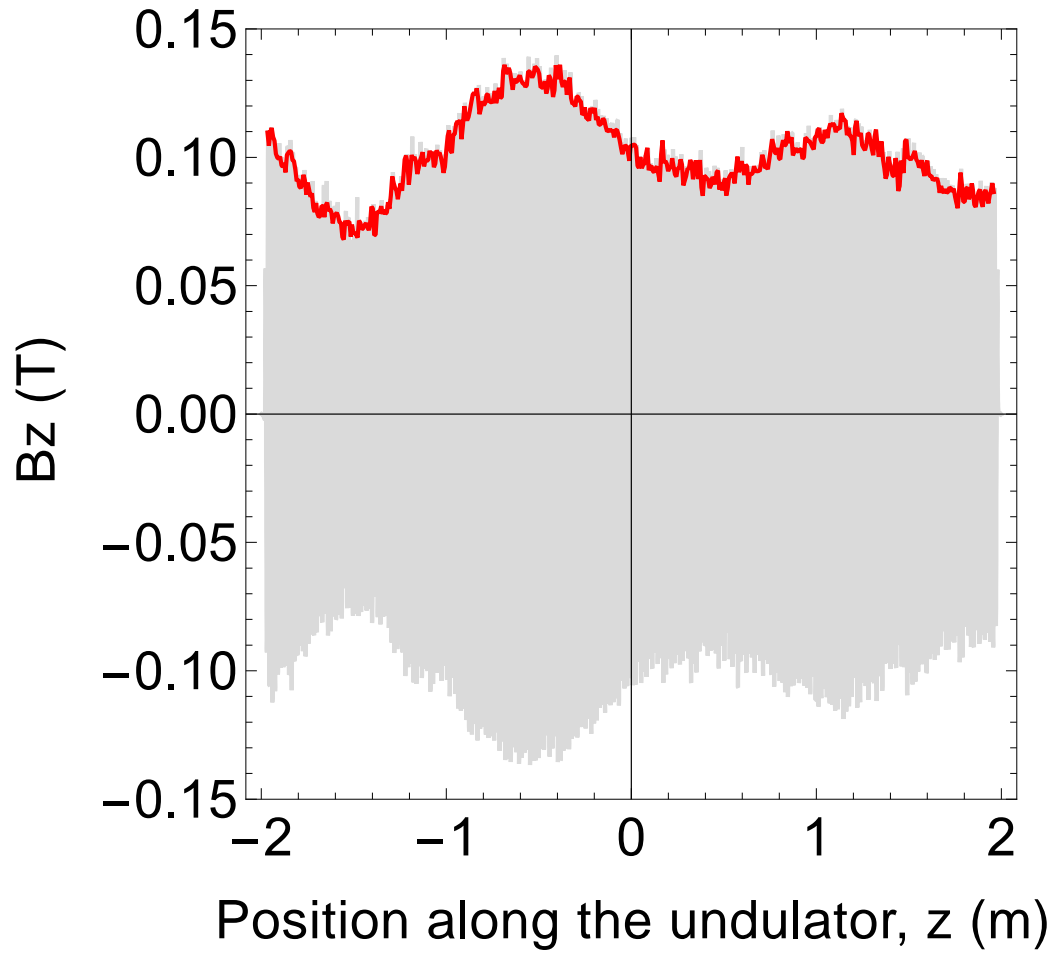


$$dBy/dh=0$$

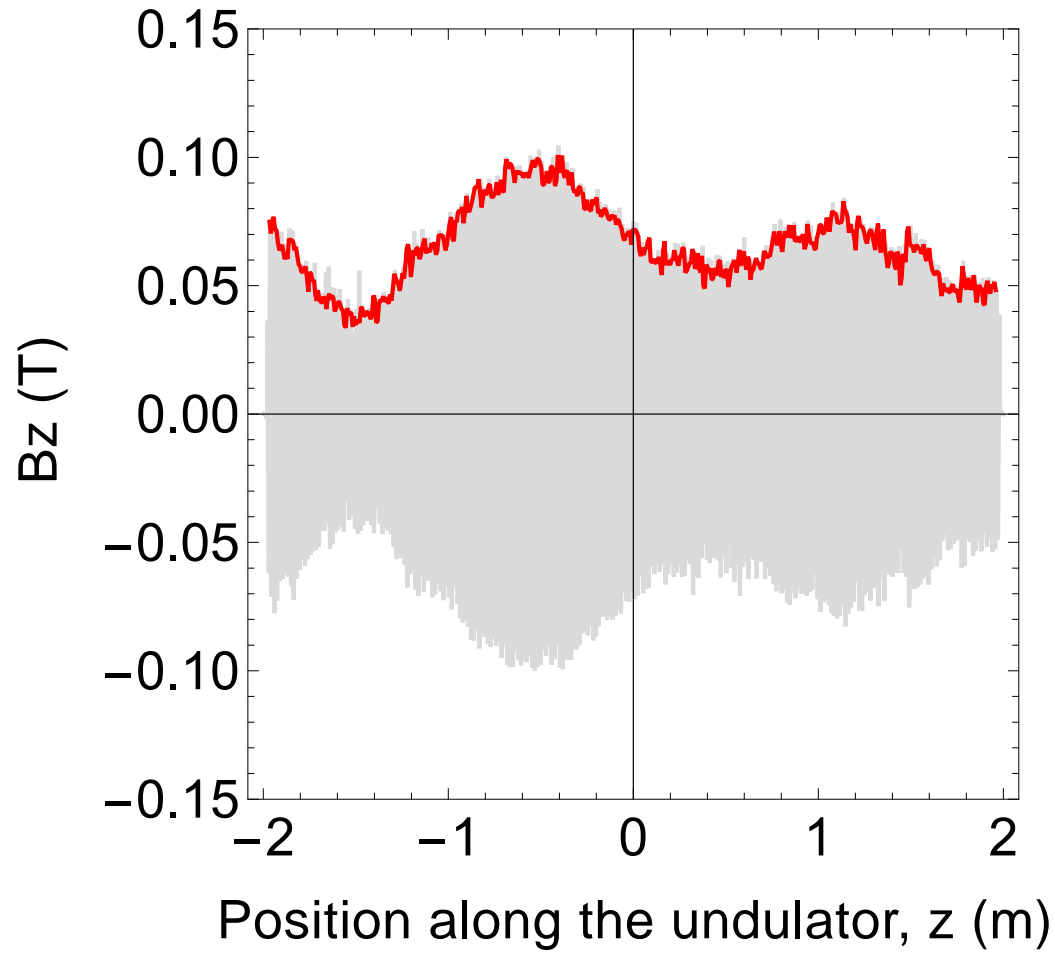
$$\circ \quad Bz=0$$

t movers (mm)

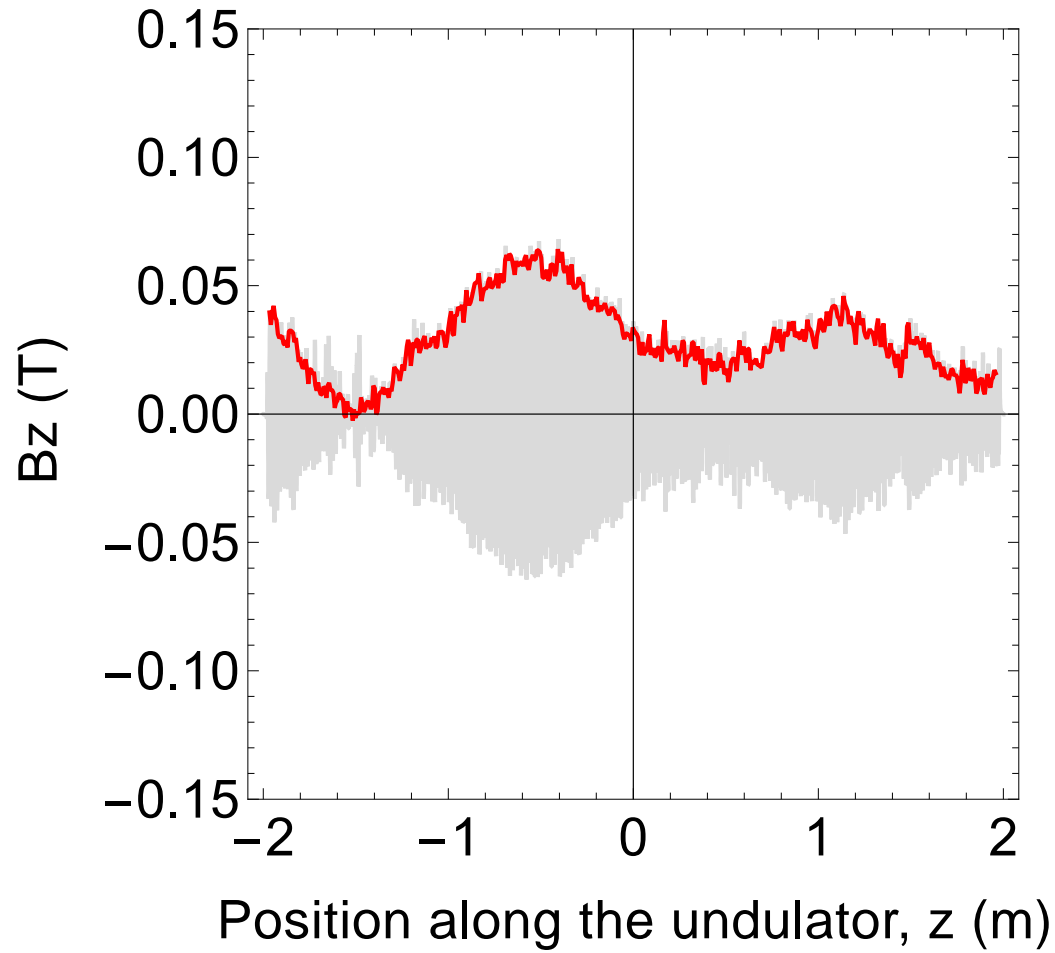
Alignment



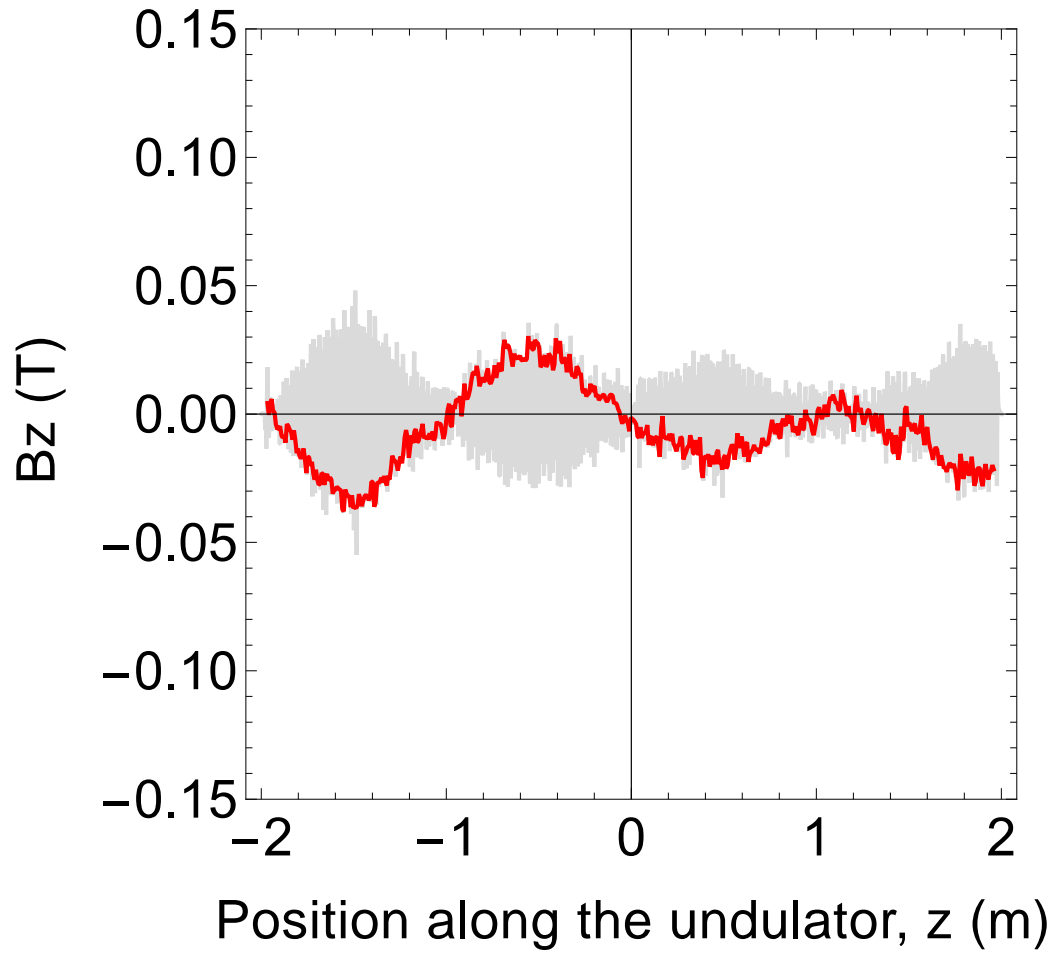
Alignment



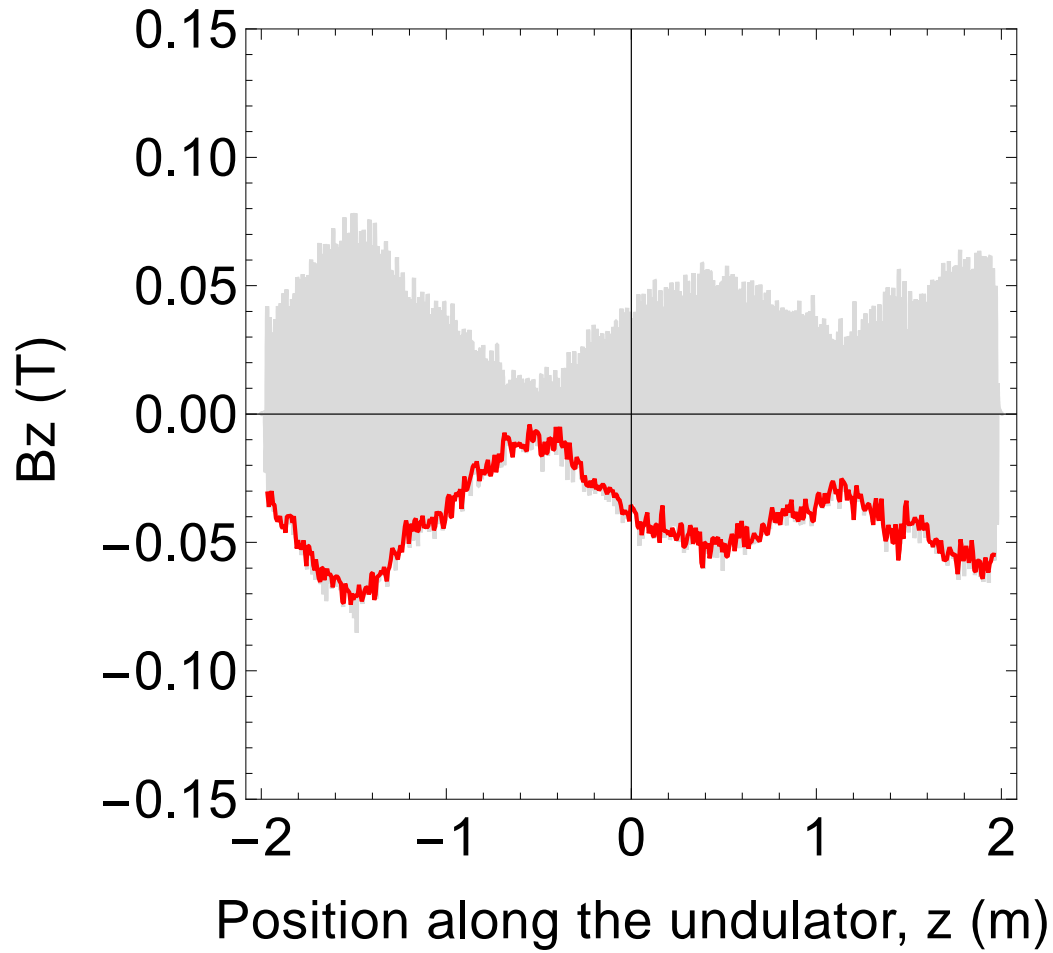
Alignment



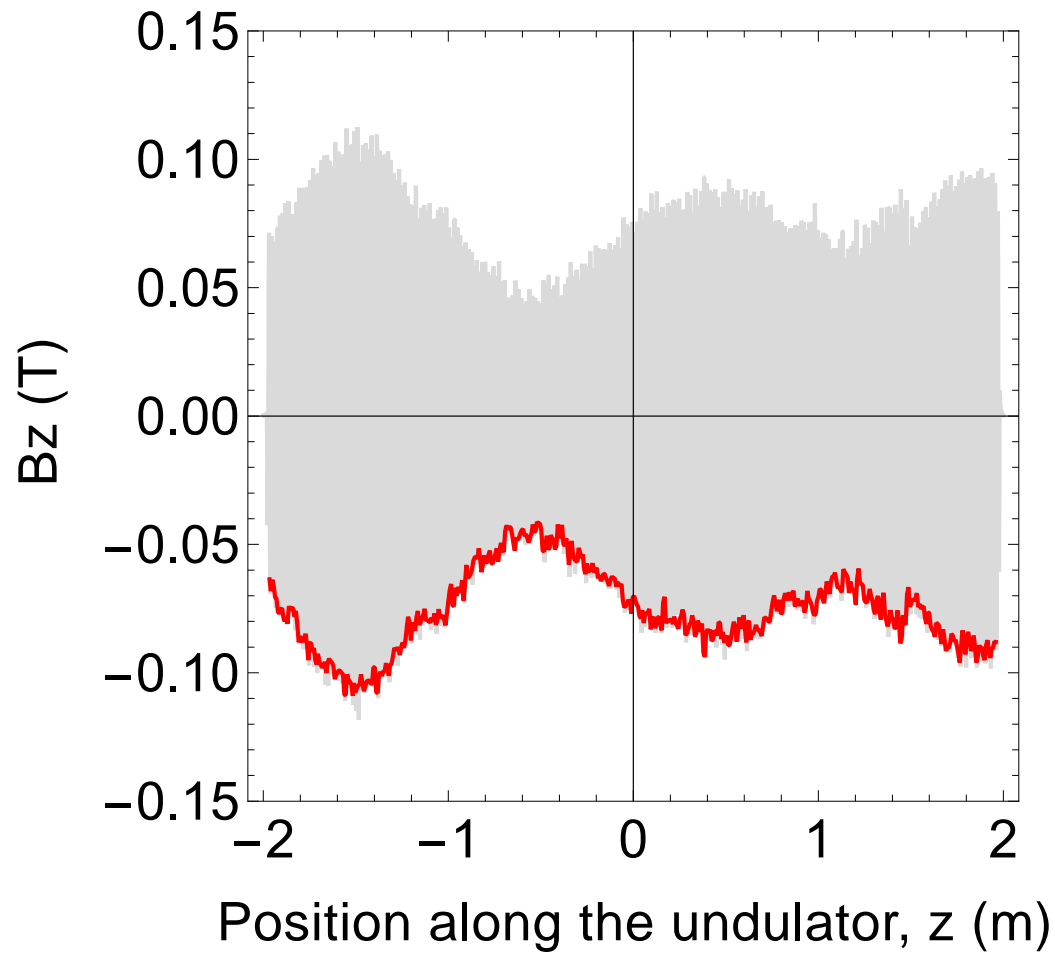
Alignment



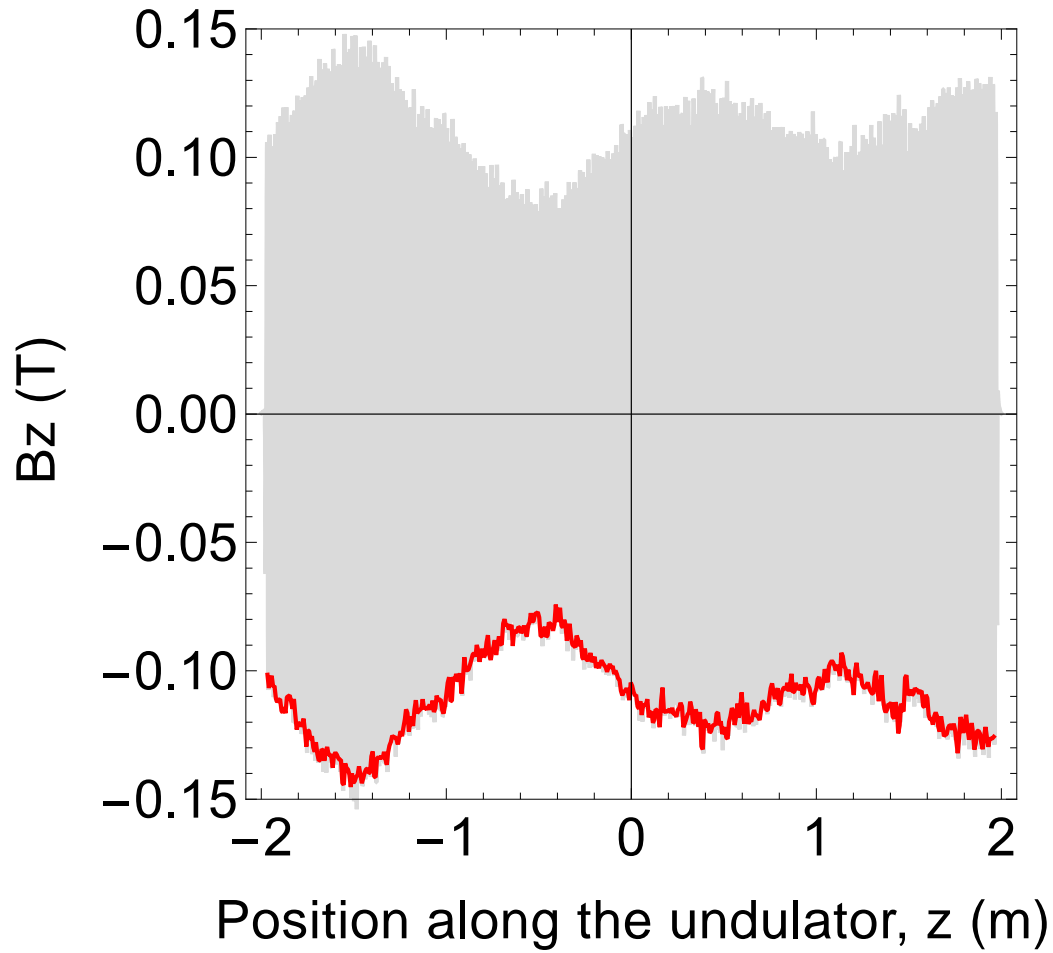
Alignment



Alignment



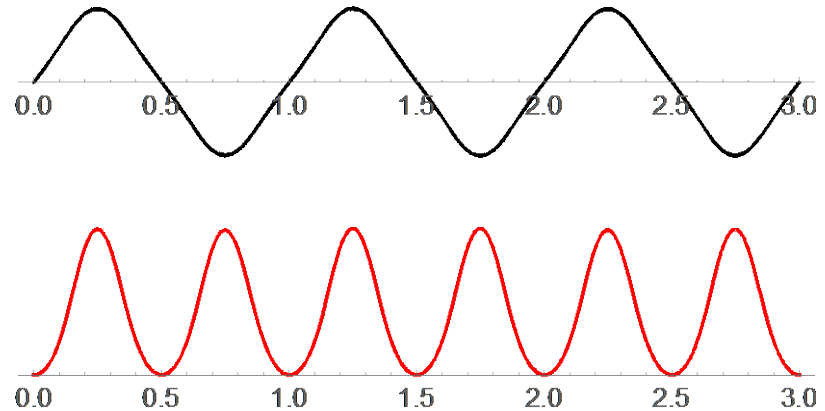
Alignment




Correction of the integrals

$\tilde{B}_\xi(z)$ the magnetic field component, x or y

$$B_\xi(z) = \tilde{B}_\xi(z) + \alpha \tilde{B}_\xi^2(z)$$



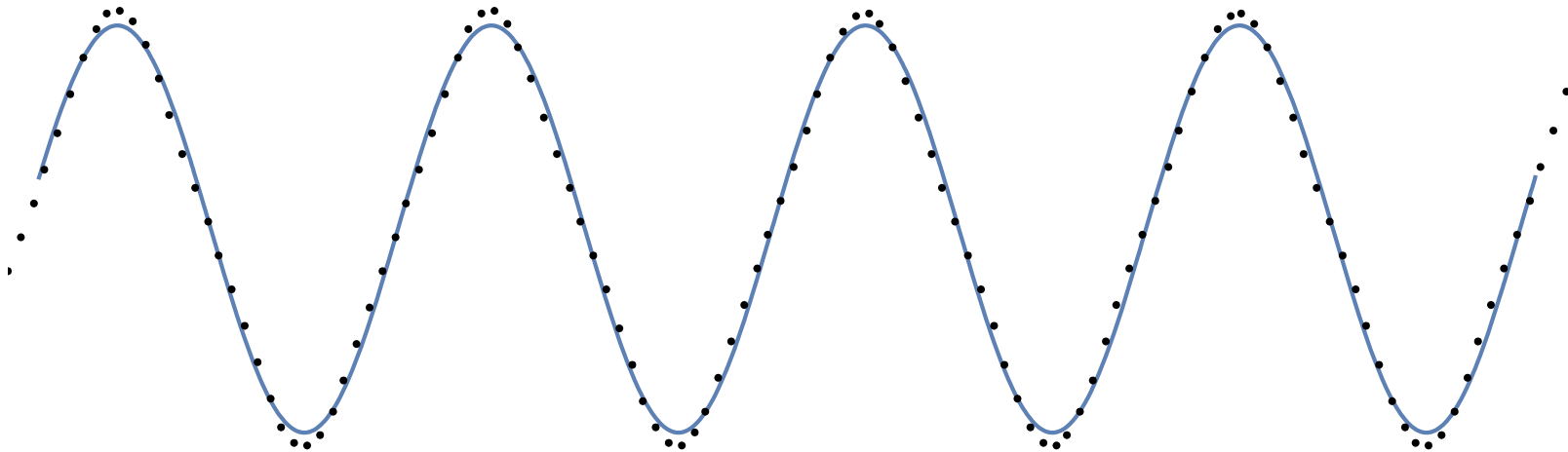
$$I_\xi = \int_{s_0}^{s_1} \tilde{B}_\xi(s) ds + \alpha \int_{s_0}^{s_1} \tilde{B}_\xi^2(s) ds$$

 This is the field integral, in x or y,
 measured with an independent and more
 accurate system: **MOVING WIRE**

Measurement of the K

$$K = \frac{e}{2\pi mc} \lambda_u B_e$$

$$B_e^2 = \sum_{n=1,3,5,\dots} \left(\frac{\hat{B}_n}{n} \right)^2$$

1st harmonic

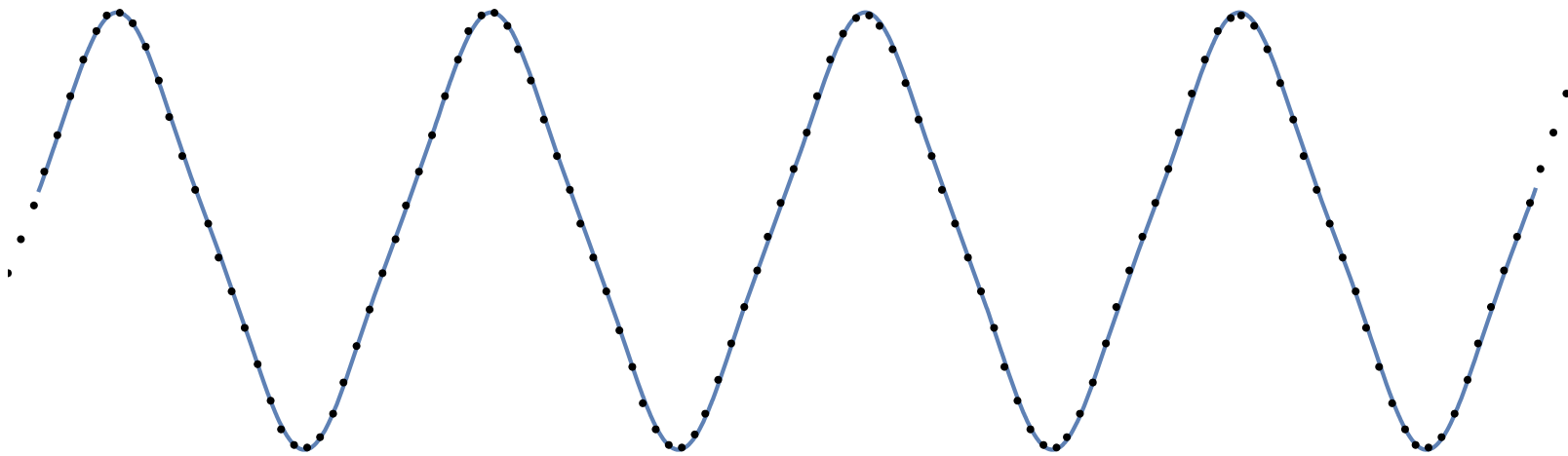
K=1.82870

Measurement of the K

$$K = \frac{e}{2\pi mc} \lambda_u B_e$$

$$B_e^2 = \sum_{n=1,3,5,\dots} \left(\frac{\hat{B}_n}{n} \right)^2$$

1st + 3rd harmonic



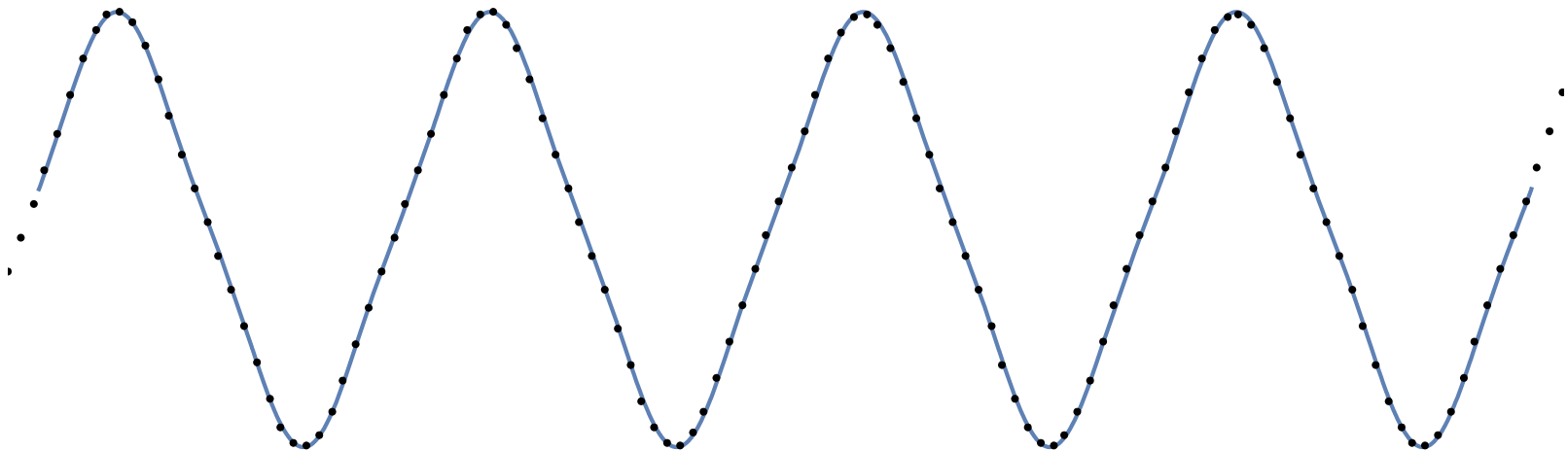
K=1.82930

Measurement of the K

$$K = \frac{e}{2\pi mc} \lambda_u B_e$$

$$B_e^2 = \sum_{n=1,3,5,\dots} \left(\frac{\hat{B}_n}{n} \right)^2$$

1st + 3rd + 5th harmonic



K=1.82930

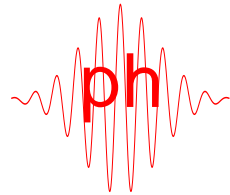
Measurement of the Phase

$$\phi(z) = \frac{1}{2\lambda} \left(\frac{z}{\gamma^2} + \int_0^z \dot{x}^2(z') dz' \right)$$

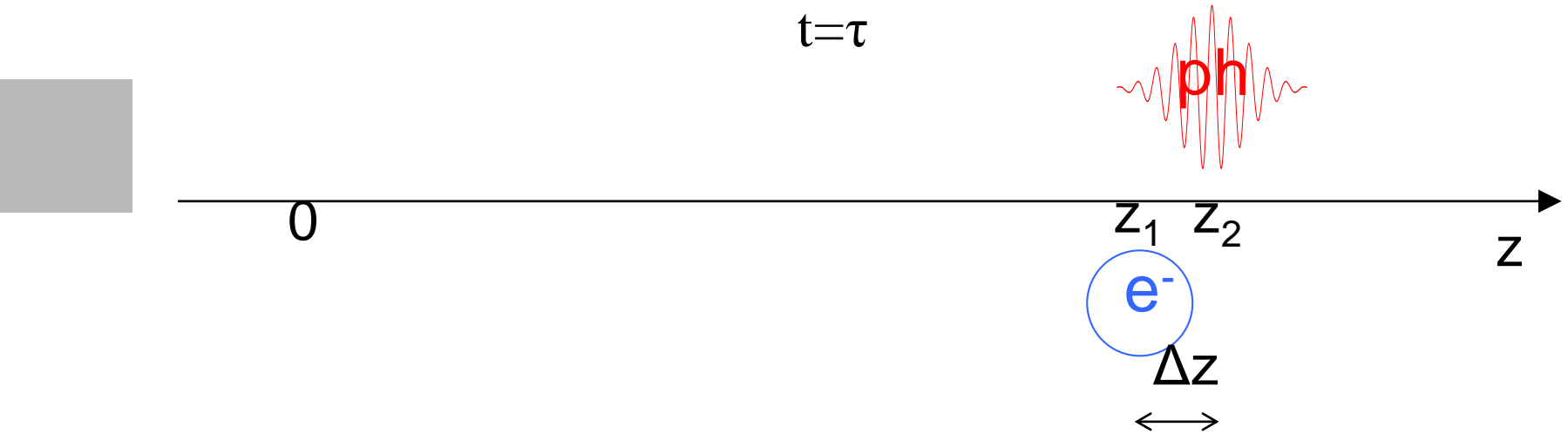
$$\dot{x}(z) = \frac{e}{\gamma mc} \int_0^z B(z') dz'$$



Measurement of the Phase

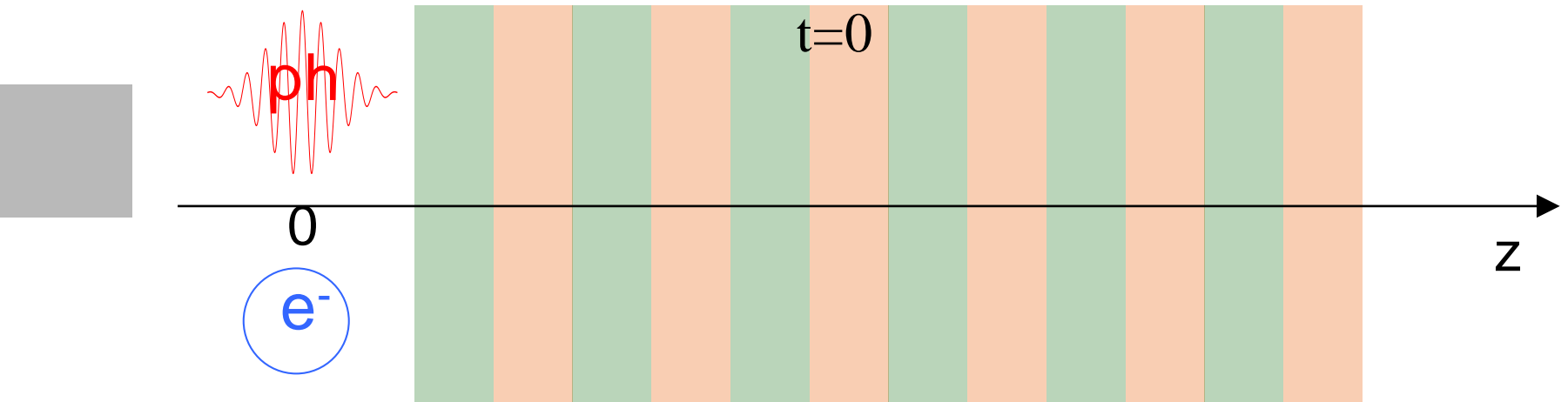
 $t=0$ 

Measurement of the Phase



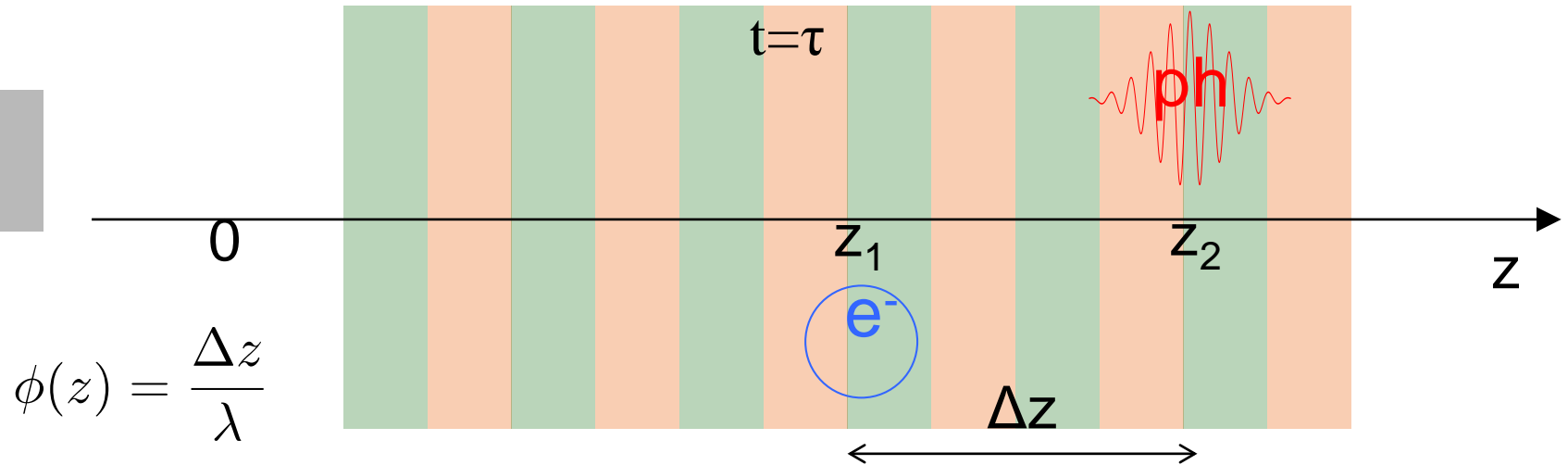
Measurement of the Phase

Undulator field



Measurement of the Phase

Undulator field



$$\phi(z) = \frac{\Delta z}{\lambda}$$

$$dt = \frac{dz}{v_z}$$

$$\tau = \int_0^{z_1} \frac{dz}{v}$$

$$\int_0^{z_1} \left(\frac{1}{v} - \frac{1}{c} \right) dz = \int_{z_1}^{z_1 + \Delta z} \frac{dz}{c}$$

$$\Delta z = \int_0^{z_1} \frac{c}{v} dz - z_1$$

$$\Delta z = \int_0^z \frac{1}{\beta_z(z')} dz' - z$$

Measurement of the Phase

$$\Delta z = \int_0^z \frac{1}{\beta_z(z')} dz' - z$$

$$\beta_z^2 = \beta^2 - \beta_x^2$$

$$\frac{1}{\beta_z} = \frac{1}{\beta} \left[1 - \left(\frac{\beta_x}{\beta} \right)^2 \right]^{-\frac{1}{2}} \approx \frac{1}{\beta} \left[1 + \frac{1}{2} \left(\frac{\beta_x}{\beta} \right)^2 \right]$$

$$\Delta z = \left(\frac{1}{\beta} - 1 \right) z + \frac{1}{2} \frac{1}{\beta^3} \int_0^z \beta_x^2(z') dz'$$

$$\rightarrow \frac{1}{2\gamma^2}$$

$$\phi(z) = \frac{1}{2\lambda} \left(\frac{z}{\gamma^2} + \int_0^z \dot{x}^2(z') dz' \right)$$

$$\beta_x \approx \frac{dx}{dz} = \dot{x} = \frac{e}{\gamma mc} \int_0^z B_y(z') dz'$$

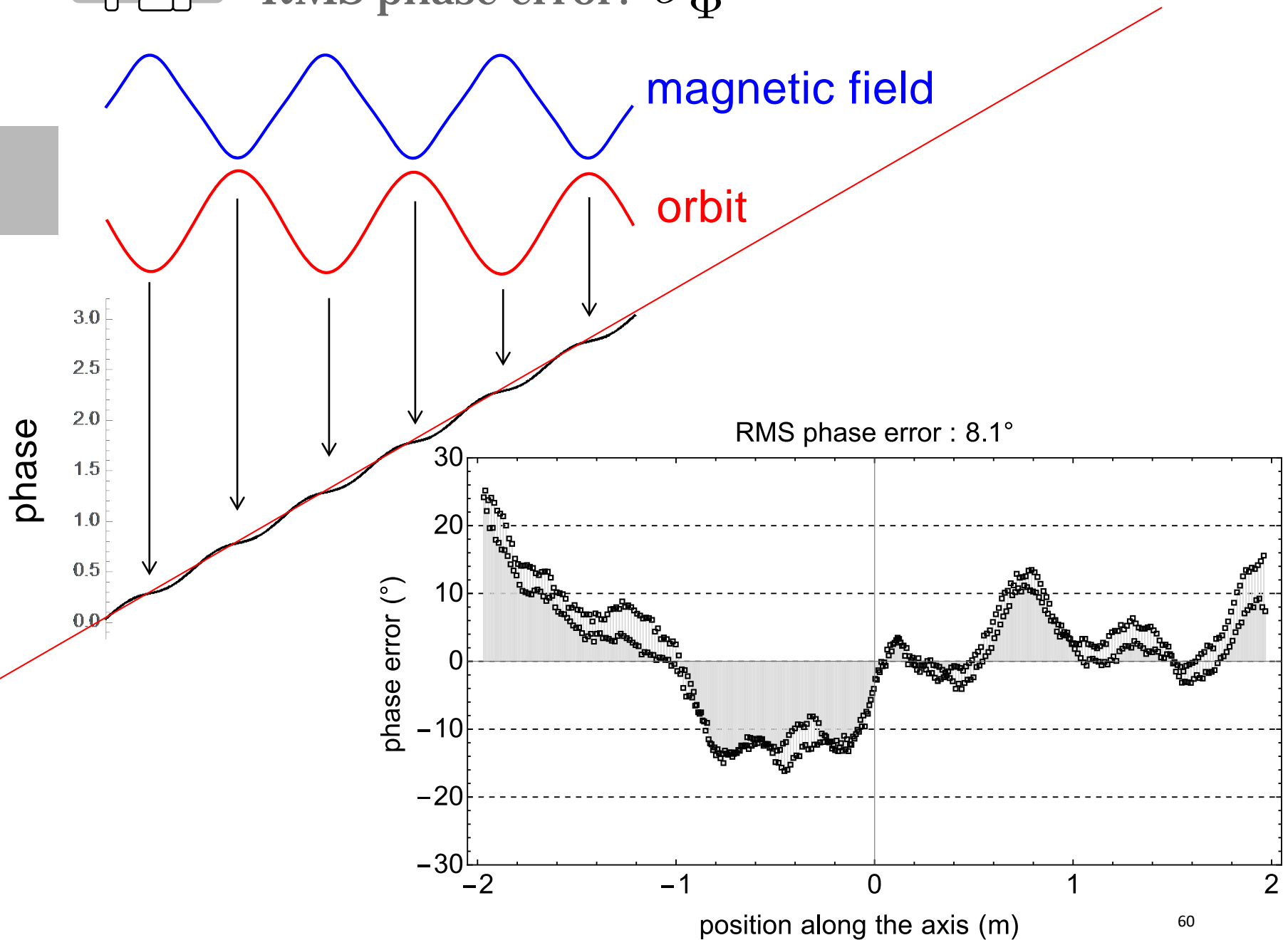
$$\phi(z) = \frac{1}{2\lambda} \left(\frac{z}{\gamma^2} + \int_0^z \dot{x}^2(z') dz' \right)$$

$$\dot{x}(z) = \frac{e}{\gamma mc} \int_0^z B(z') dz'$$

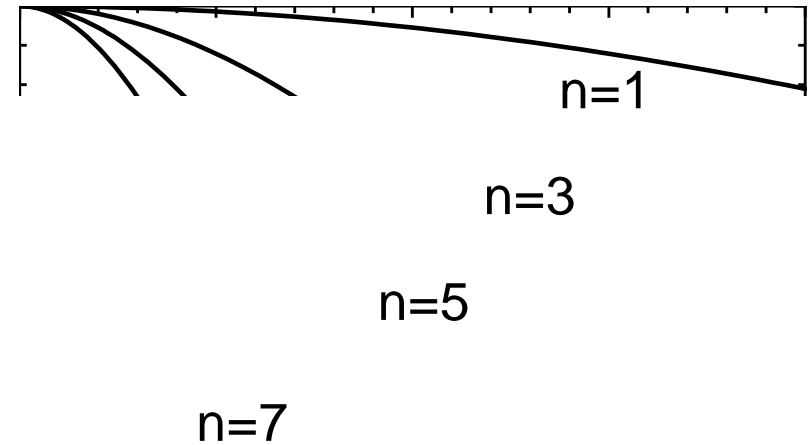
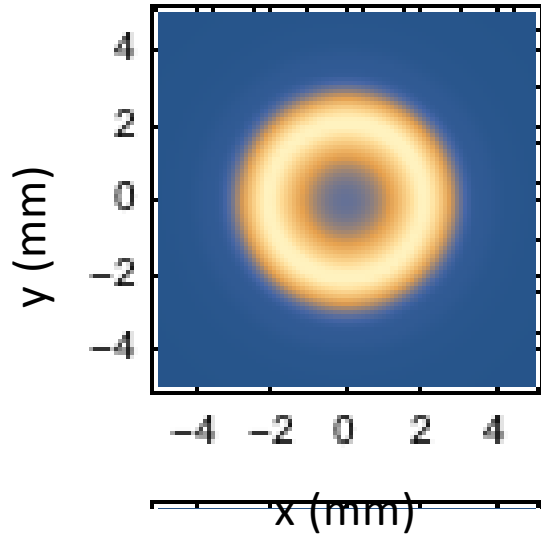
$$\phi(z) = \frac{1}{\lambda_u \left(1 + \frac{1}{2} K^2 \right)} \left(z + \left(\frac{e}{mc} \right)^2 \int_0^z I^2(z') dz' \right)$$

$$I(z) = \int_0^z B(z') dz'$$

RMS phase error: σ_{Φ}^2



RMS phase error: σ_{Φ}^2



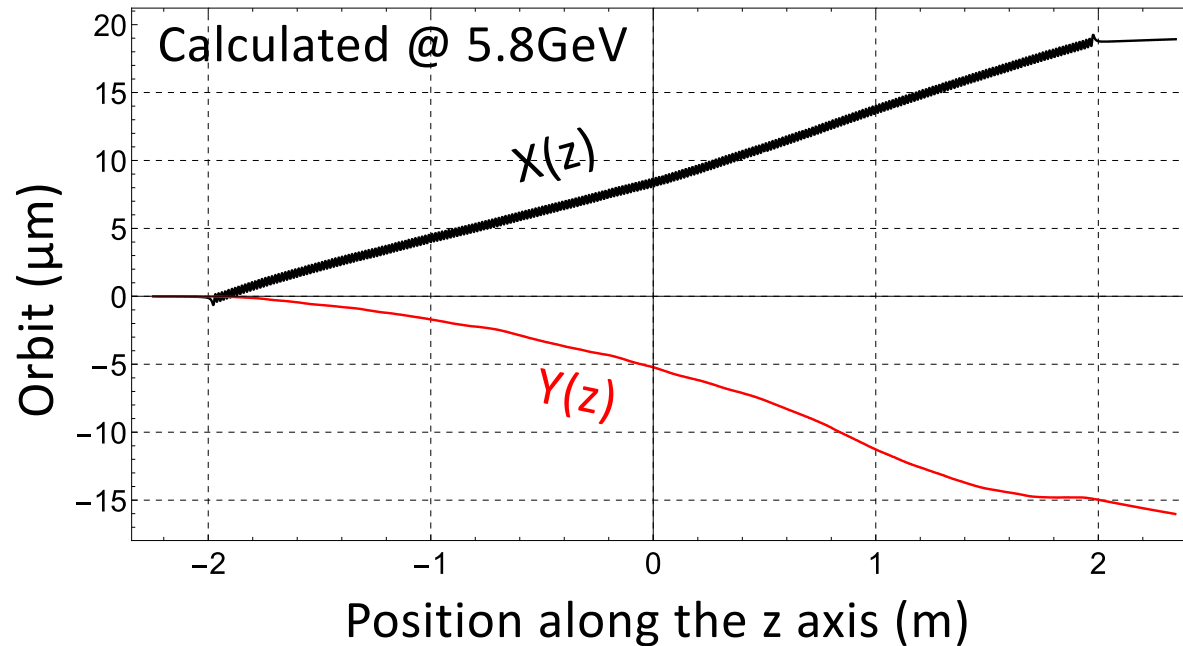
$$R \approx e^{-n^2 \sigma_{\Phi}^2}$$

R is the relative intensity

n is the harmonic number

Measurement of the Orbit distortion

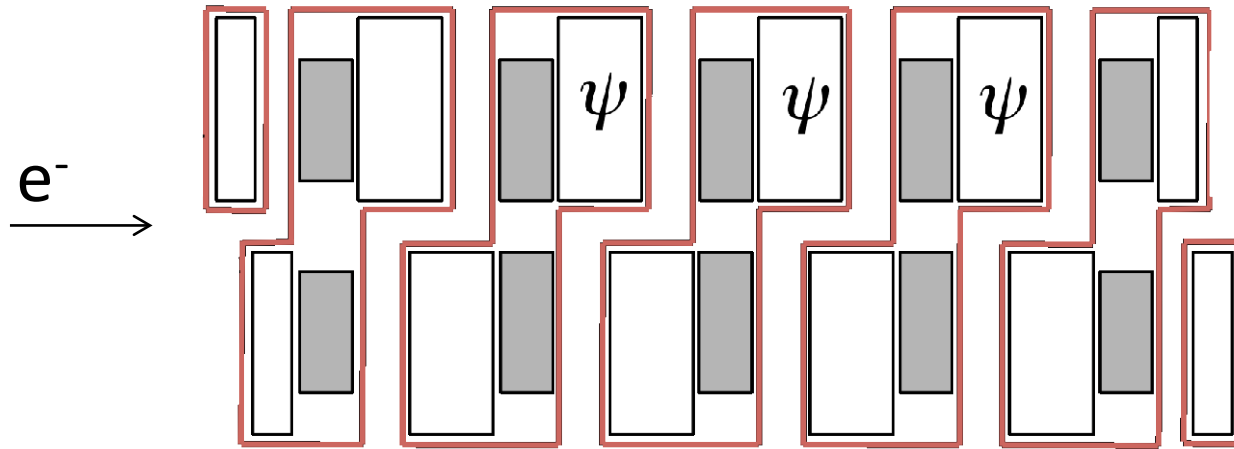
$$x/y(z) = \frac{e}{\gamma mc} \int_{-\infty}^z \int_{-\infty}^{z'} B_{y/x}(z'') dz'' dz'$$



$$\xi(z) = \begin{cases} 0 & z < z_i \\ \kappa_i(z - z_i) + \frac{1}{2} E_c (z - z_i)^2 & z_i < z < z_o \\ \kappa_i(z - z_i) + 4E_c z + \kappa_o(z - z_o) & z > z_o \end{cases}$$

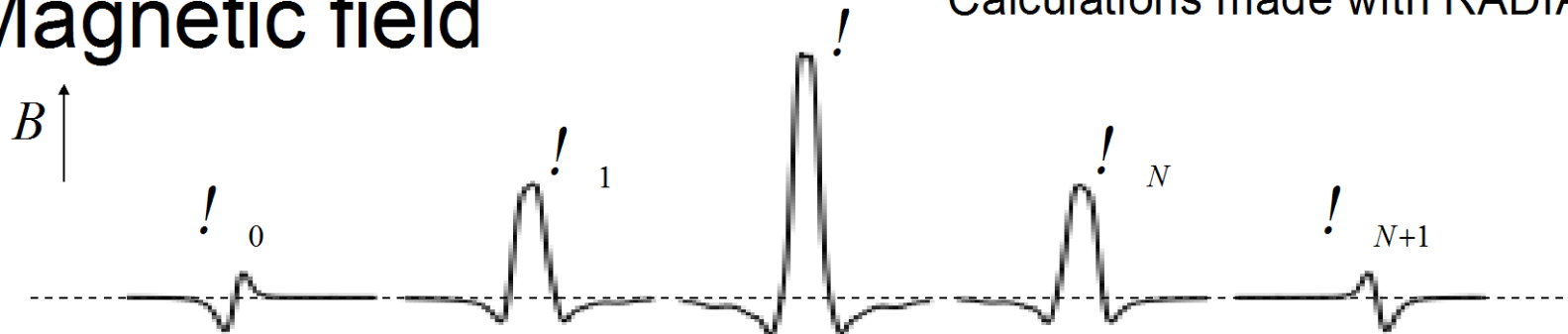
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Optimization: field



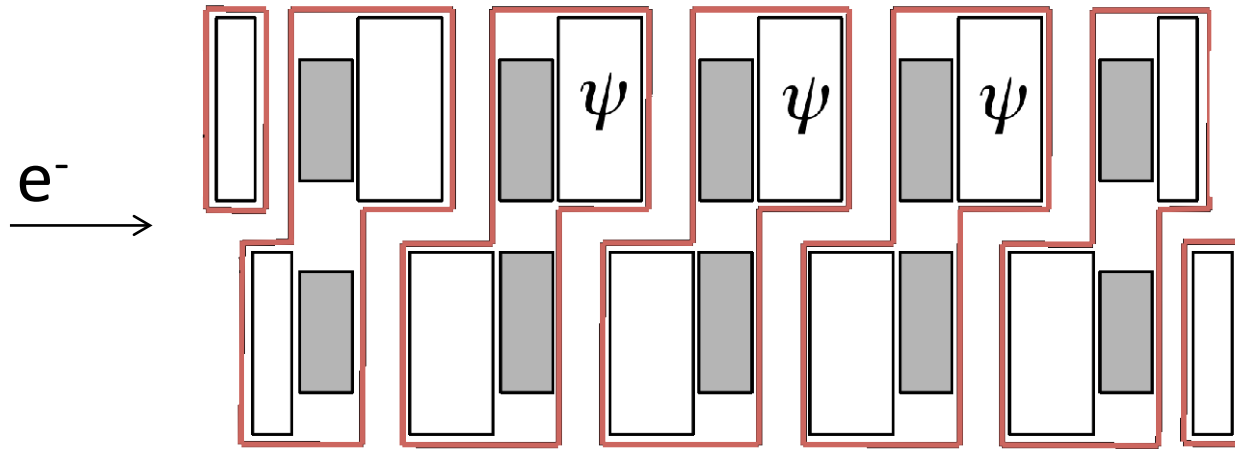
Magnetic field

Calculations made with RADIA

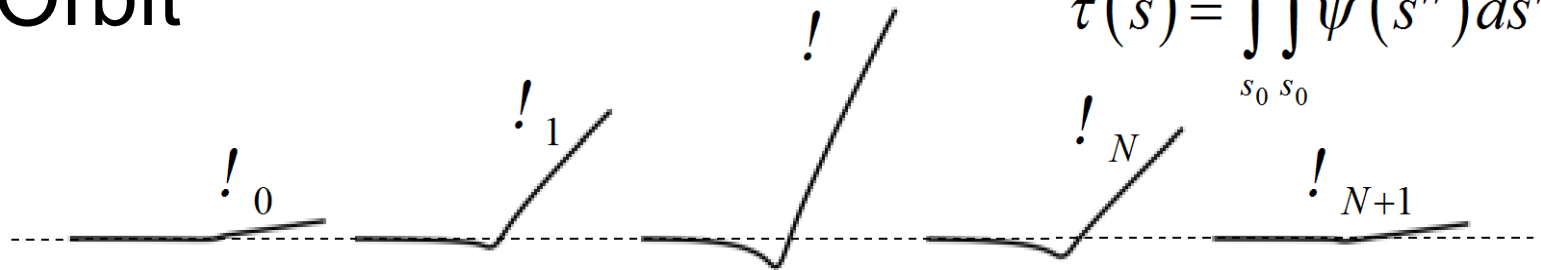


$$\Delta B(s) = \Psi_e(s) + \sum_{n=2}^{N-1} (-1)^n b_n \psi(s - s_n)$$

Optimization: Orbit



Orbit



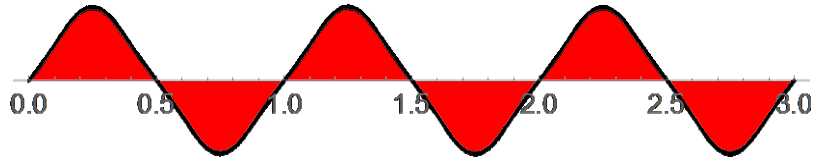
$$\tau(s) = \int_{s_0}^s \int_{s_0}^{s'} \psi(s'') ds''$$

$$\Delta T(s) = \tau_e(s) + \sum_{n=2}^{N-1} (-1)^n b_n \tau(s - s_n)$$

Measurements

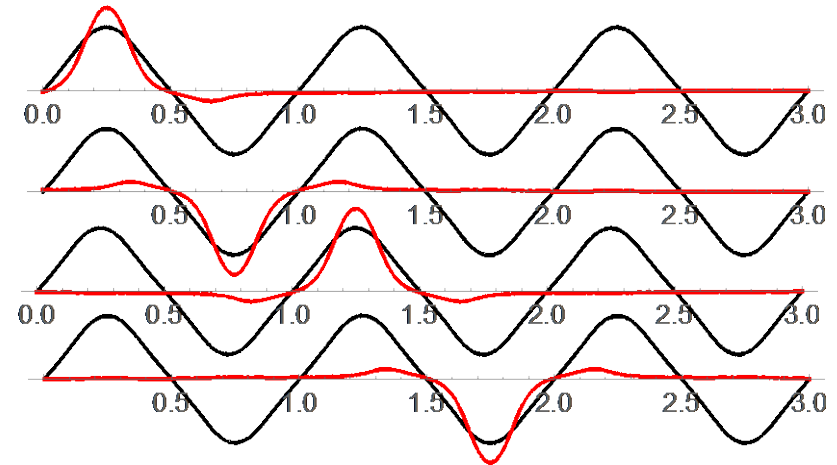
$$k_n = \left| \int_{z_n}^{z_{n+1}} B_y(z) dz \right|$$

$$\delta k_n = k_n - \langle k_n \rangle$$



$$p_{n,m} = \frac{1}{\delta h} \int_{z_n}^{z_{n+1}} \delta B_y(z - \bar{z}_m) dz$$

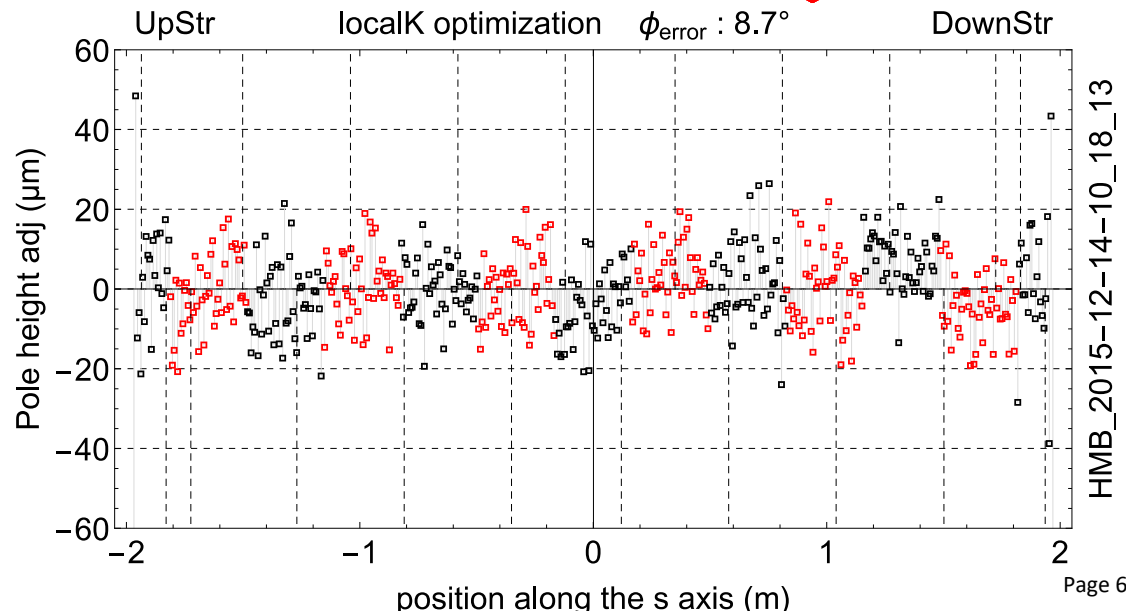
$$\bar{z}_m = \frac{1}{2} (z_m + z_{m+1})$$



Optimisation

$$\delta \mathbf{k} - \mathbf{P}(g) \delta \mathbf{h} = 0$$

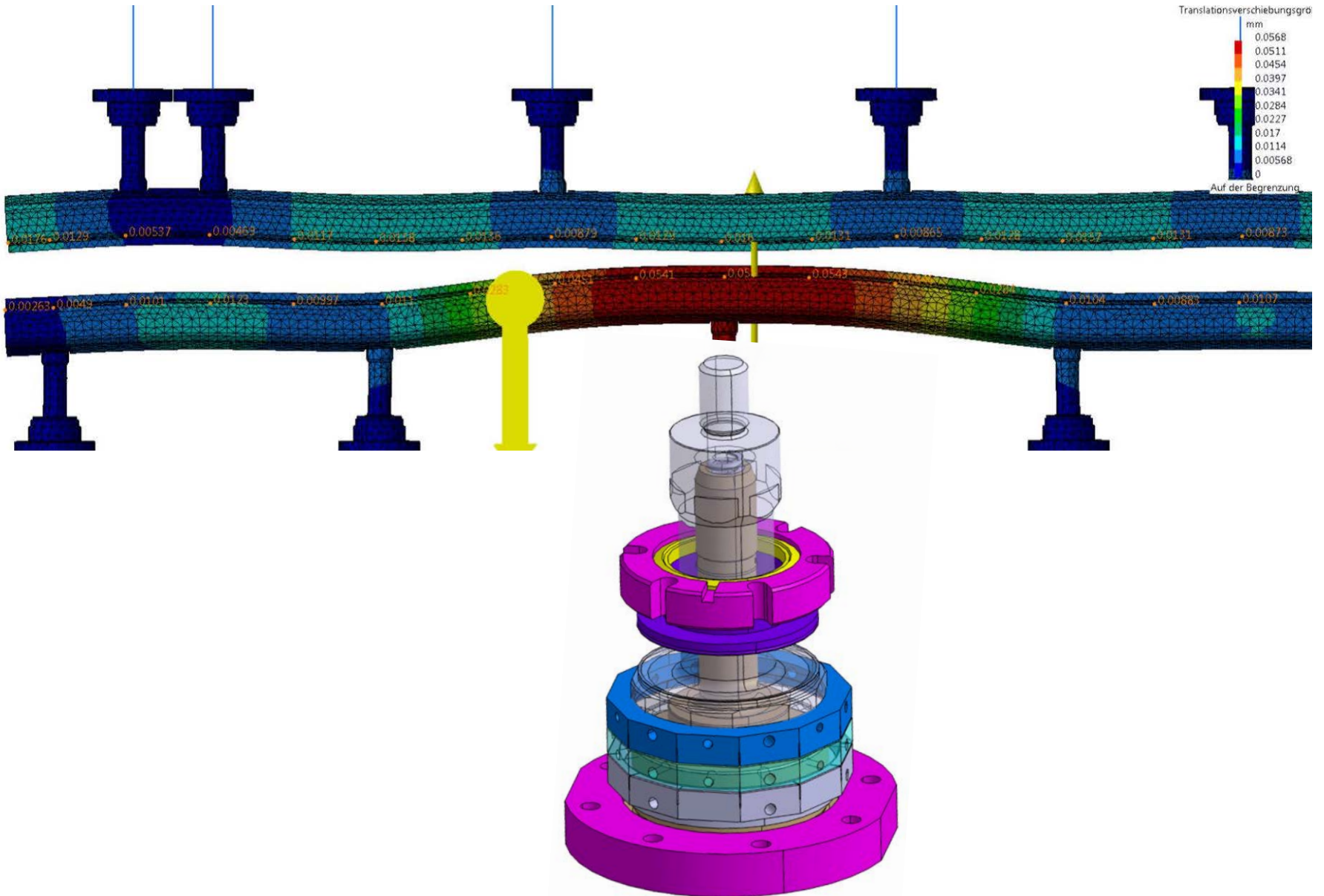
$$\delta \mathbf{h} = \mathbf{P}^{-1} \delta \mathbf{k}$$



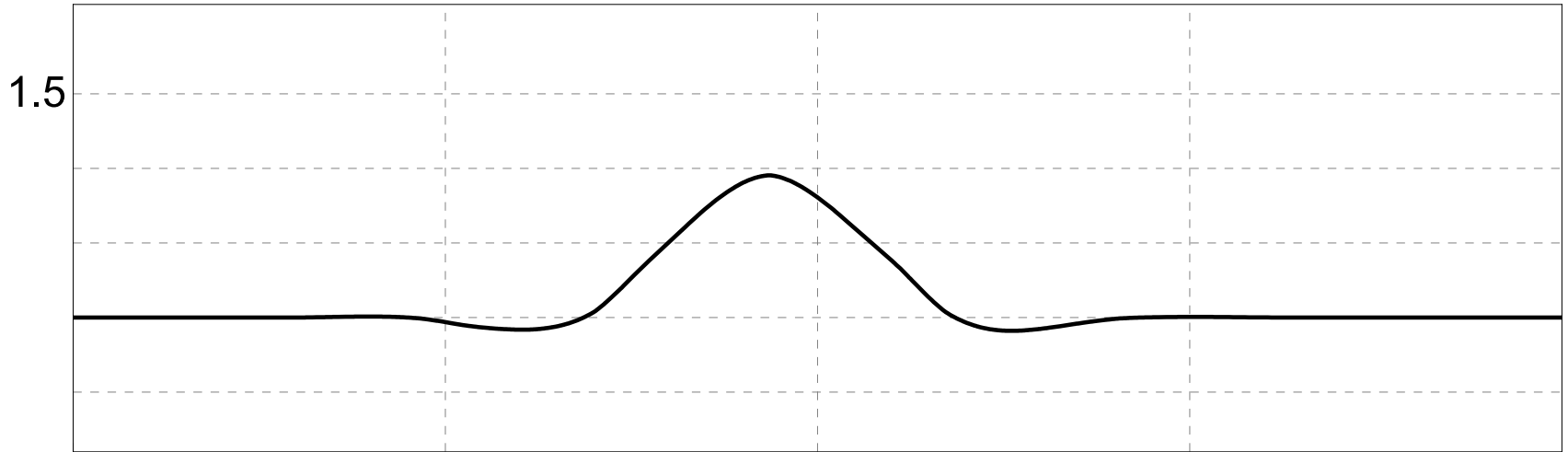
Columns optimisation



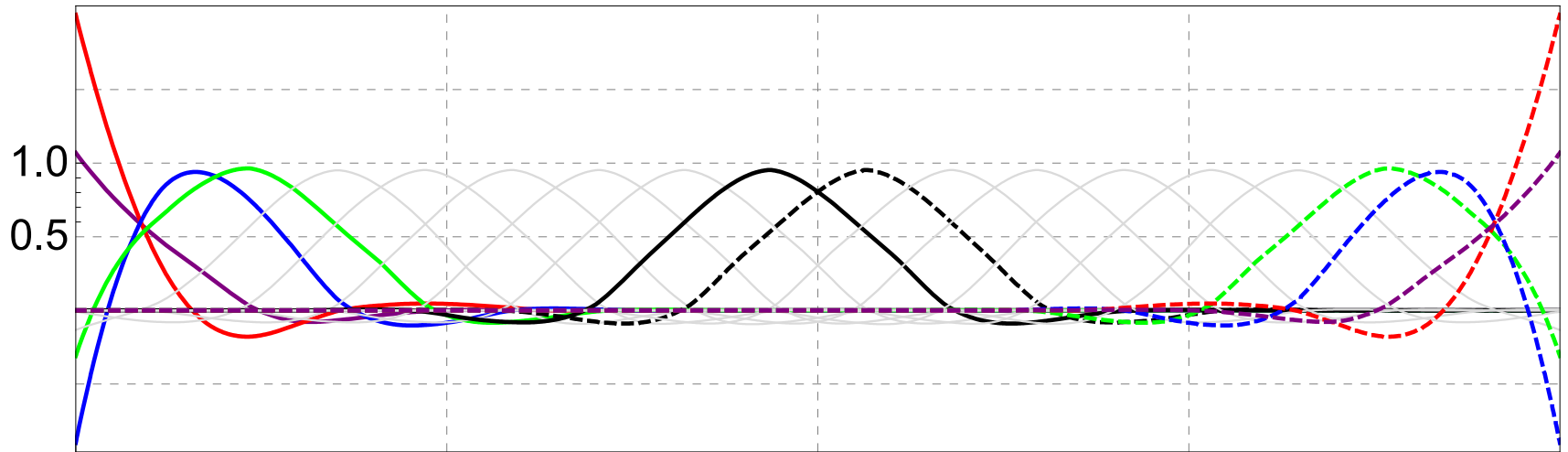
Columns optimisation



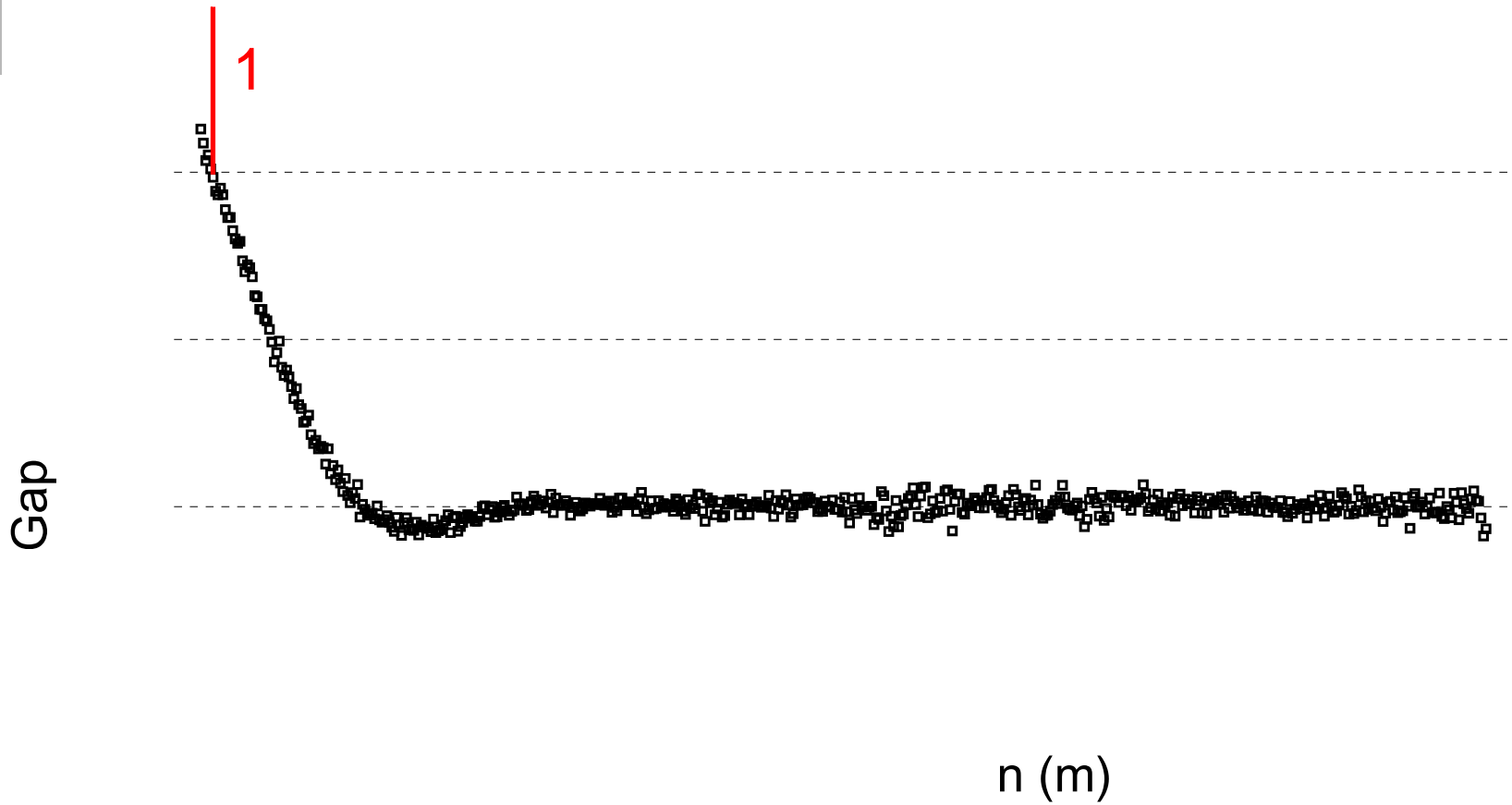
Columns optimisation



Columns optimisation



Columns optimisation



Columns optimisation



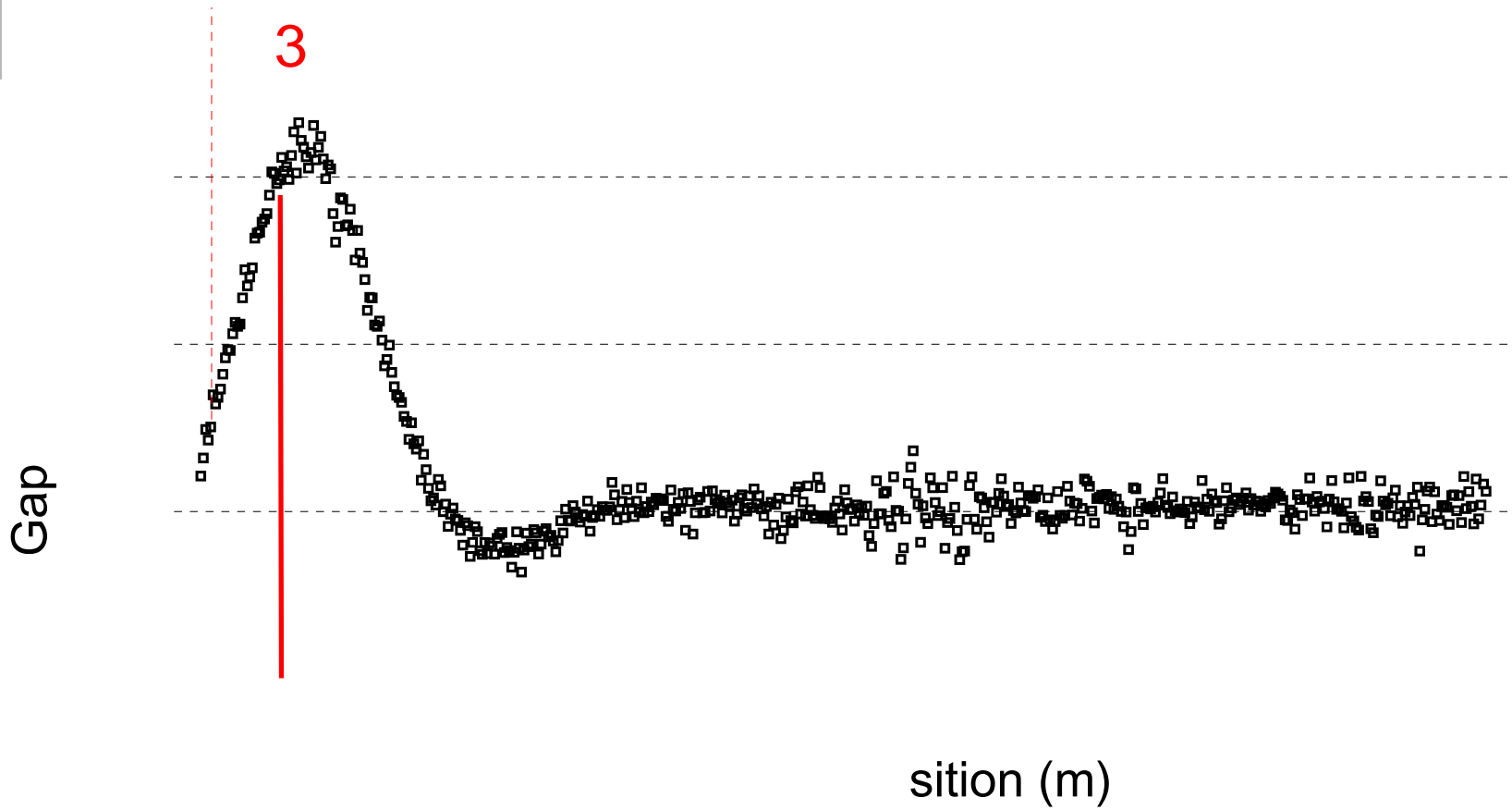
2

Gap

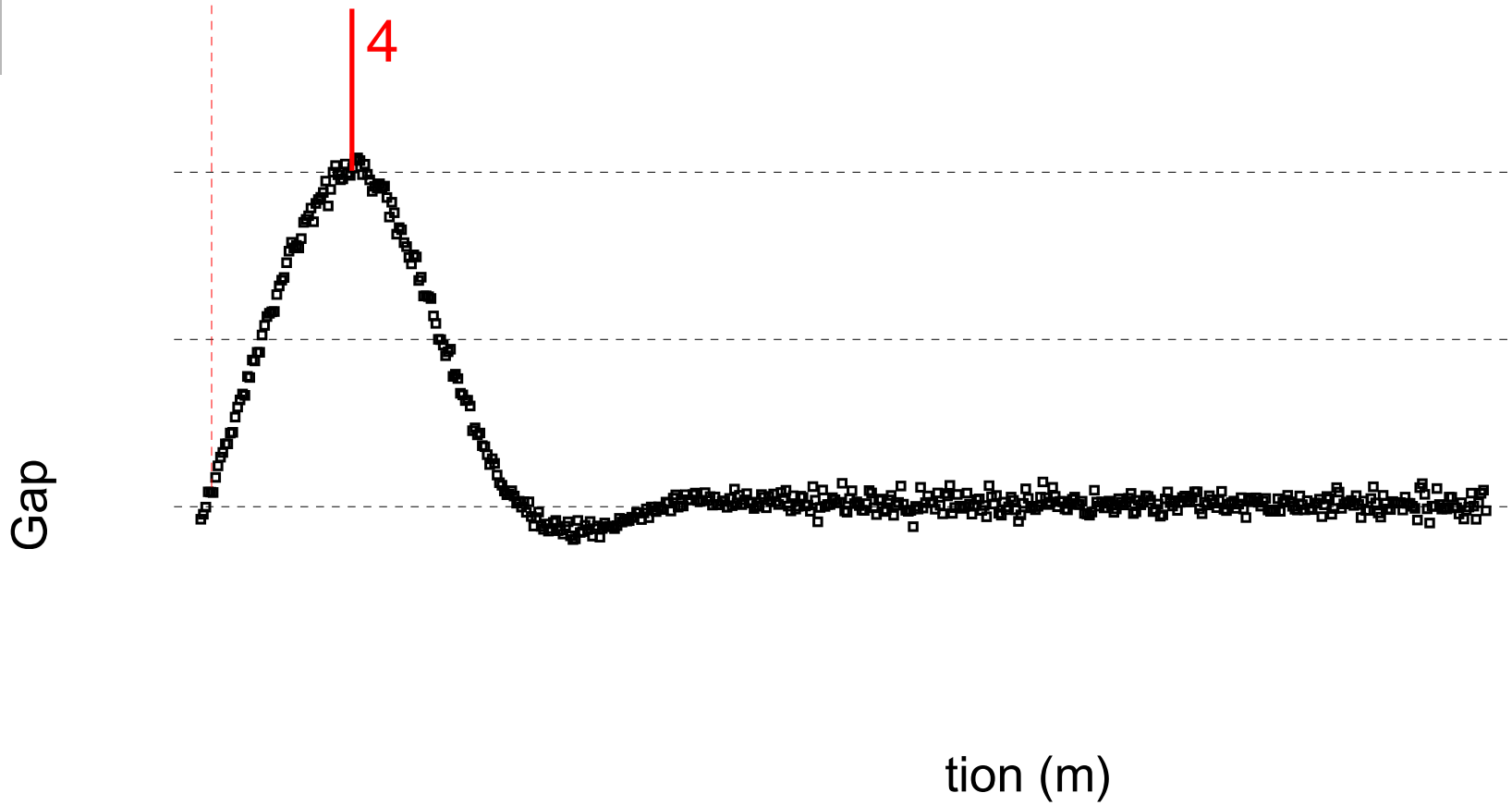


tion (m)

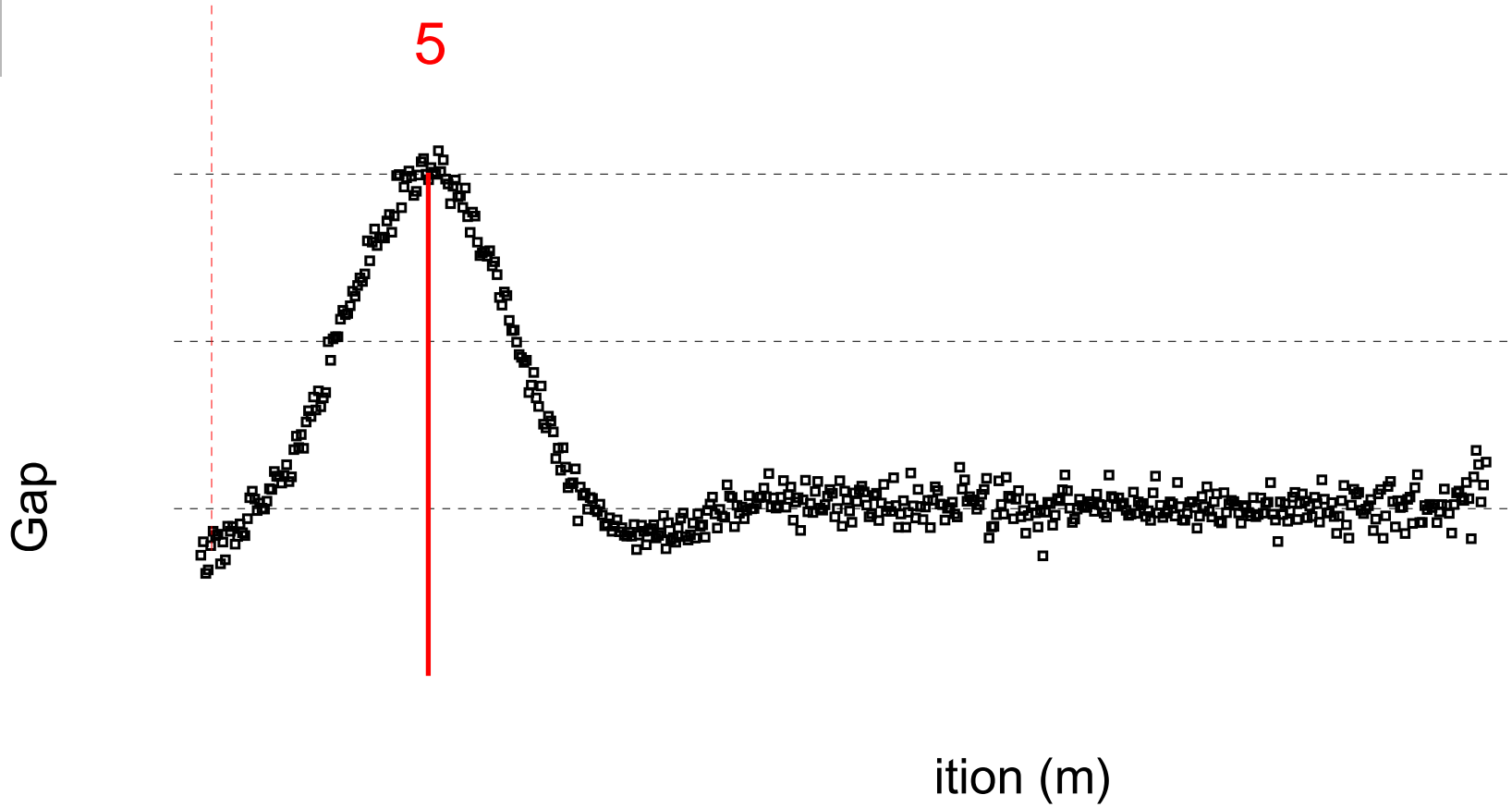
Columns optimisation



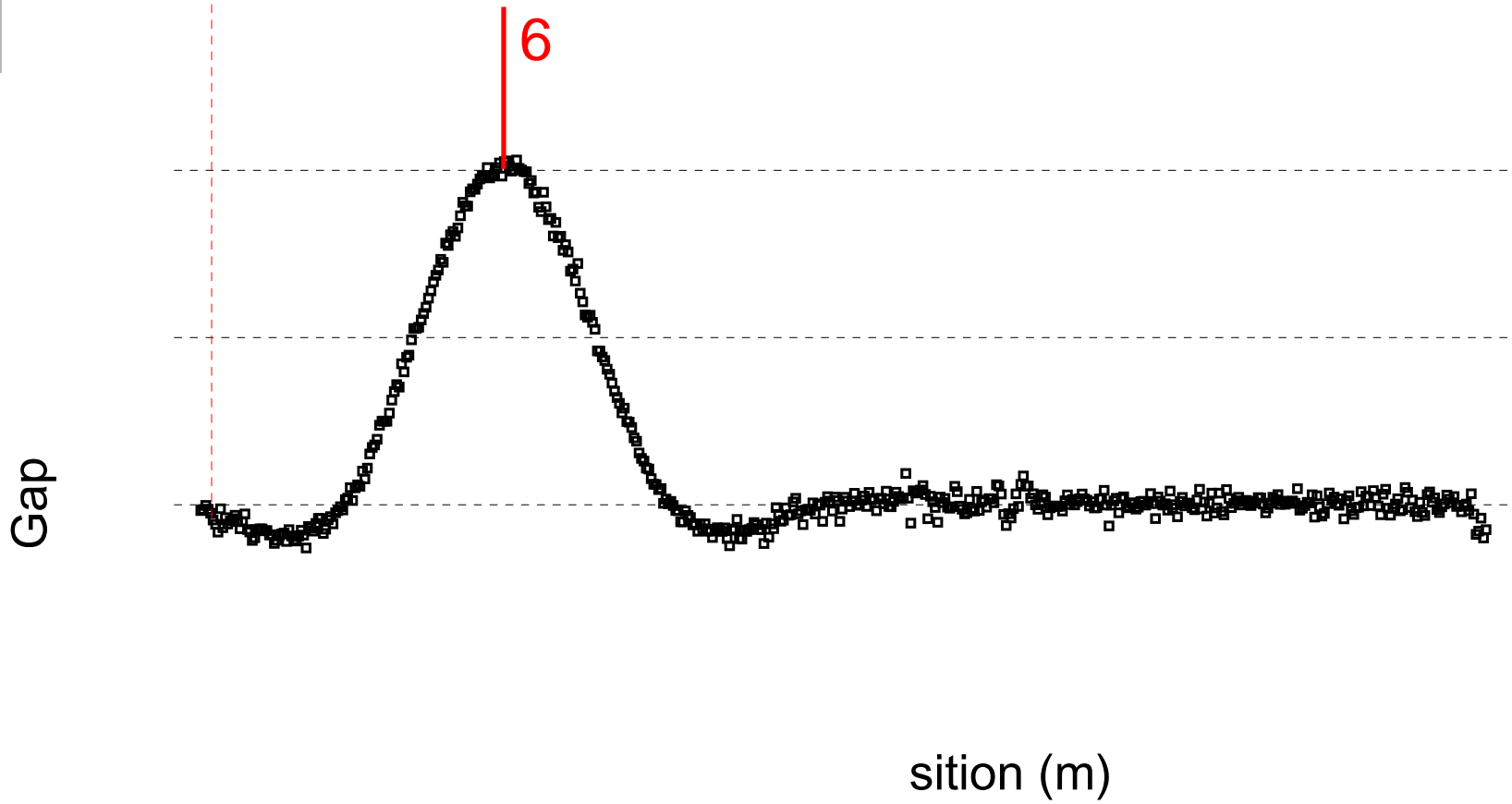
Columns optimisation



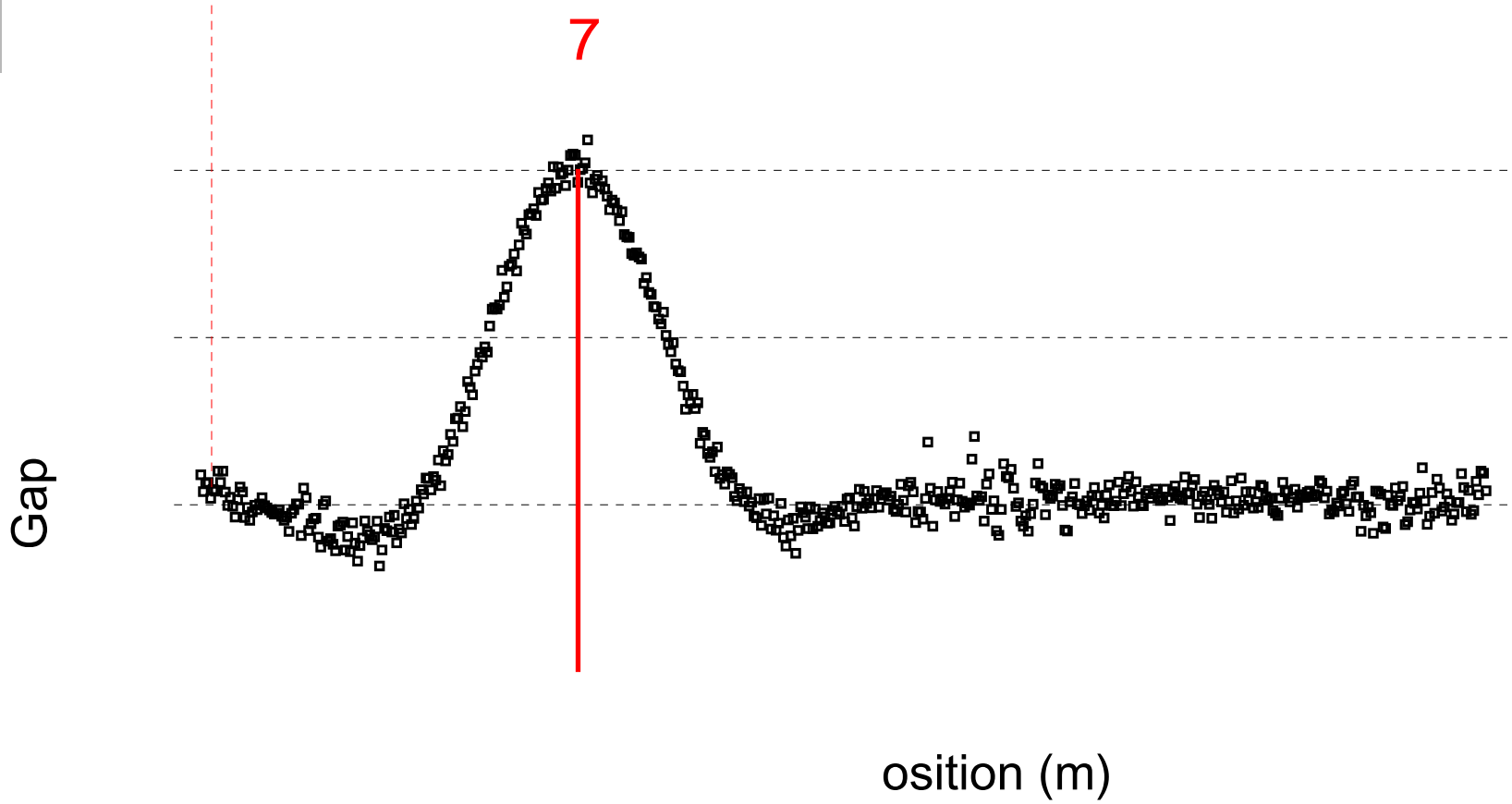
Columns optimisation



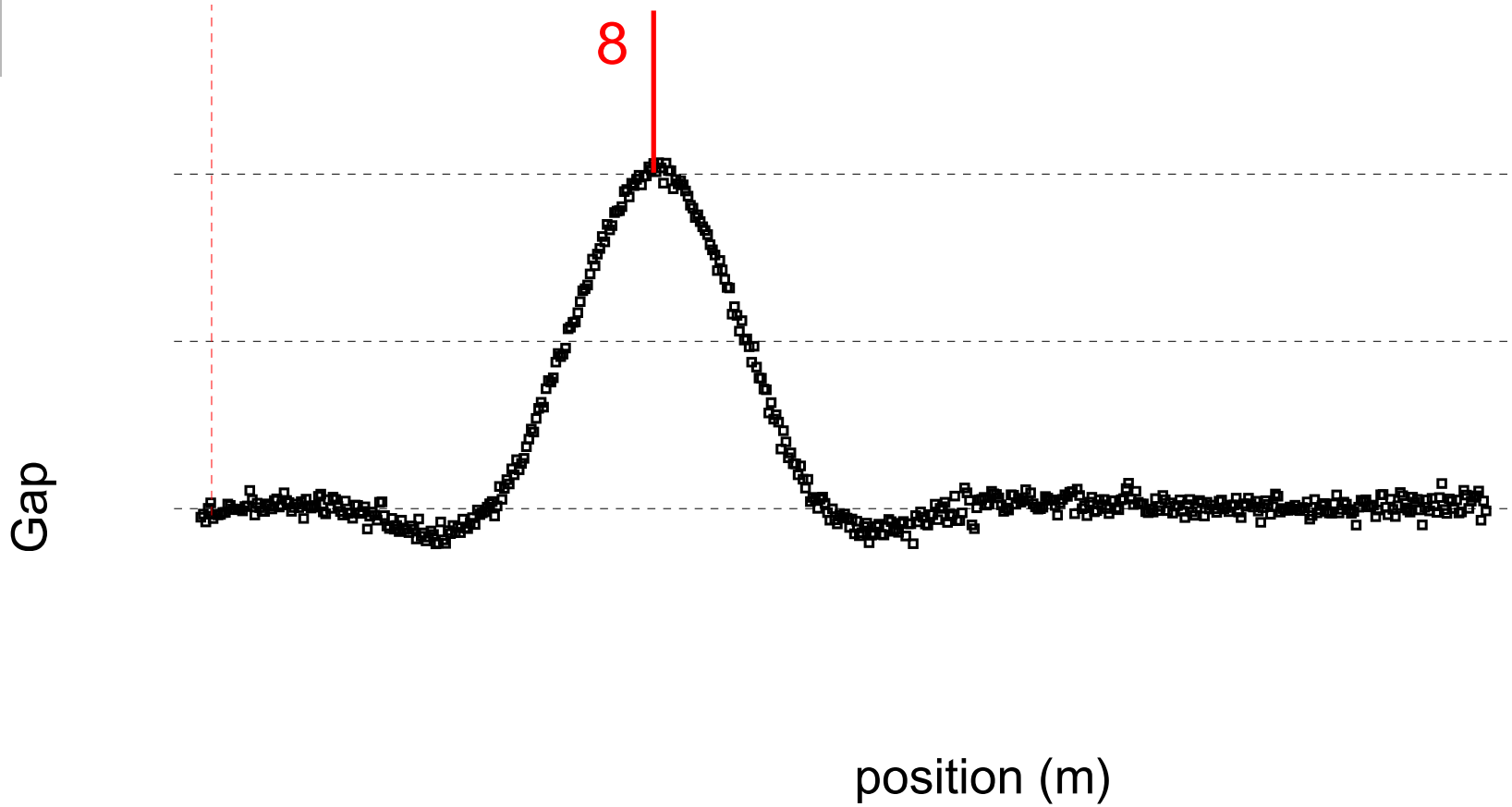
Columns optimisation



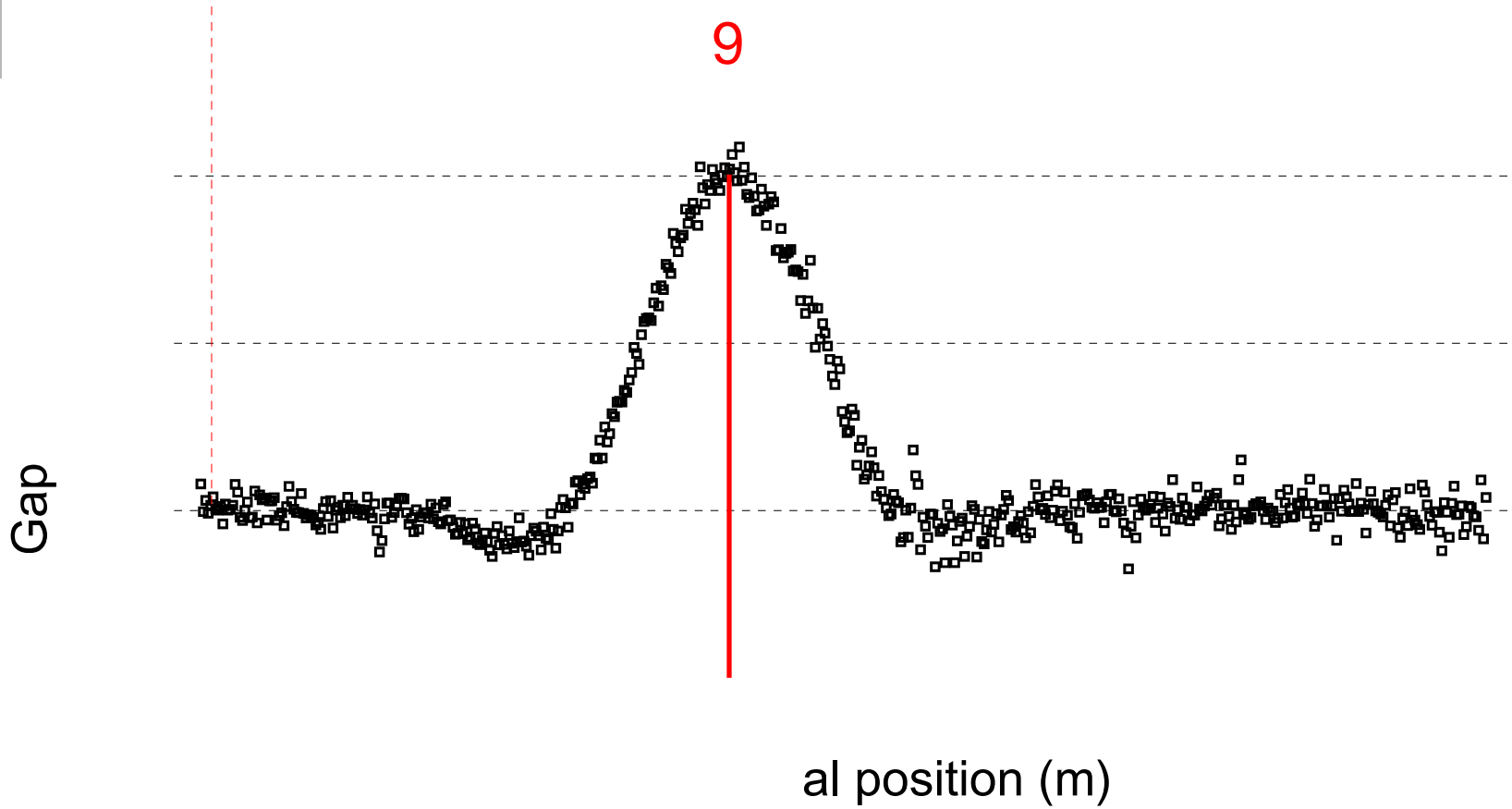
Columns optimisation



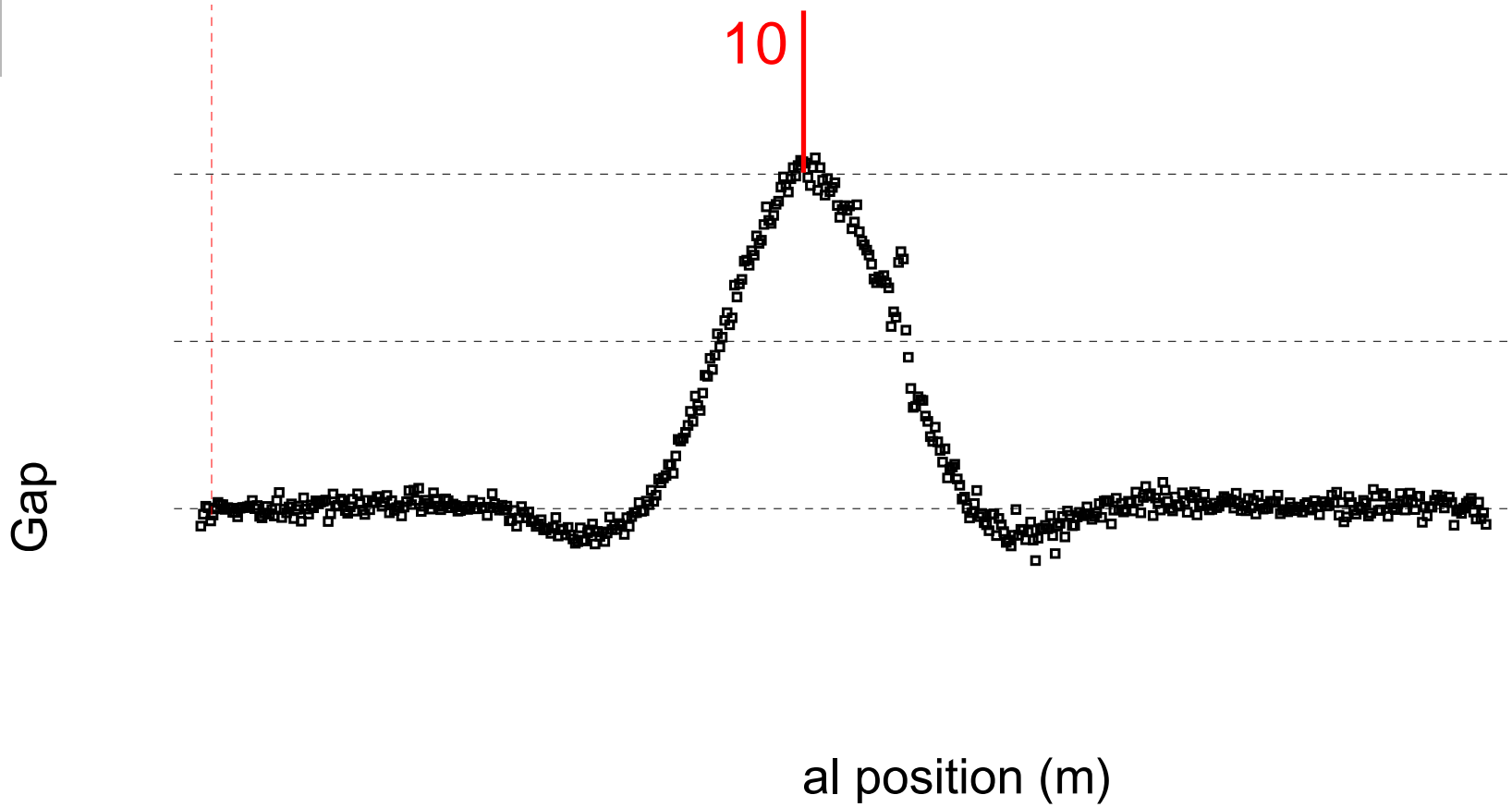
Columns optimisation



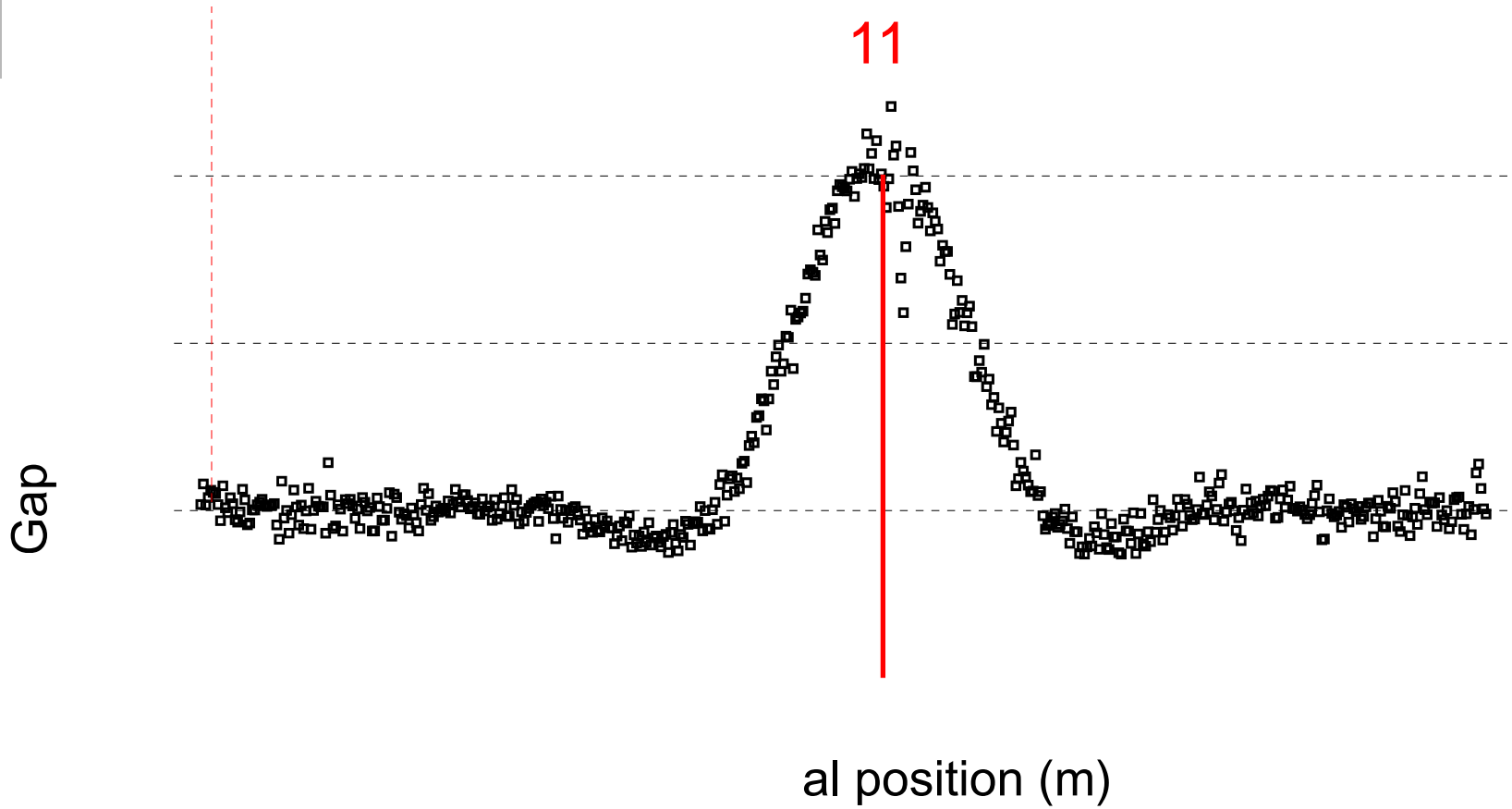
Columns optimisation



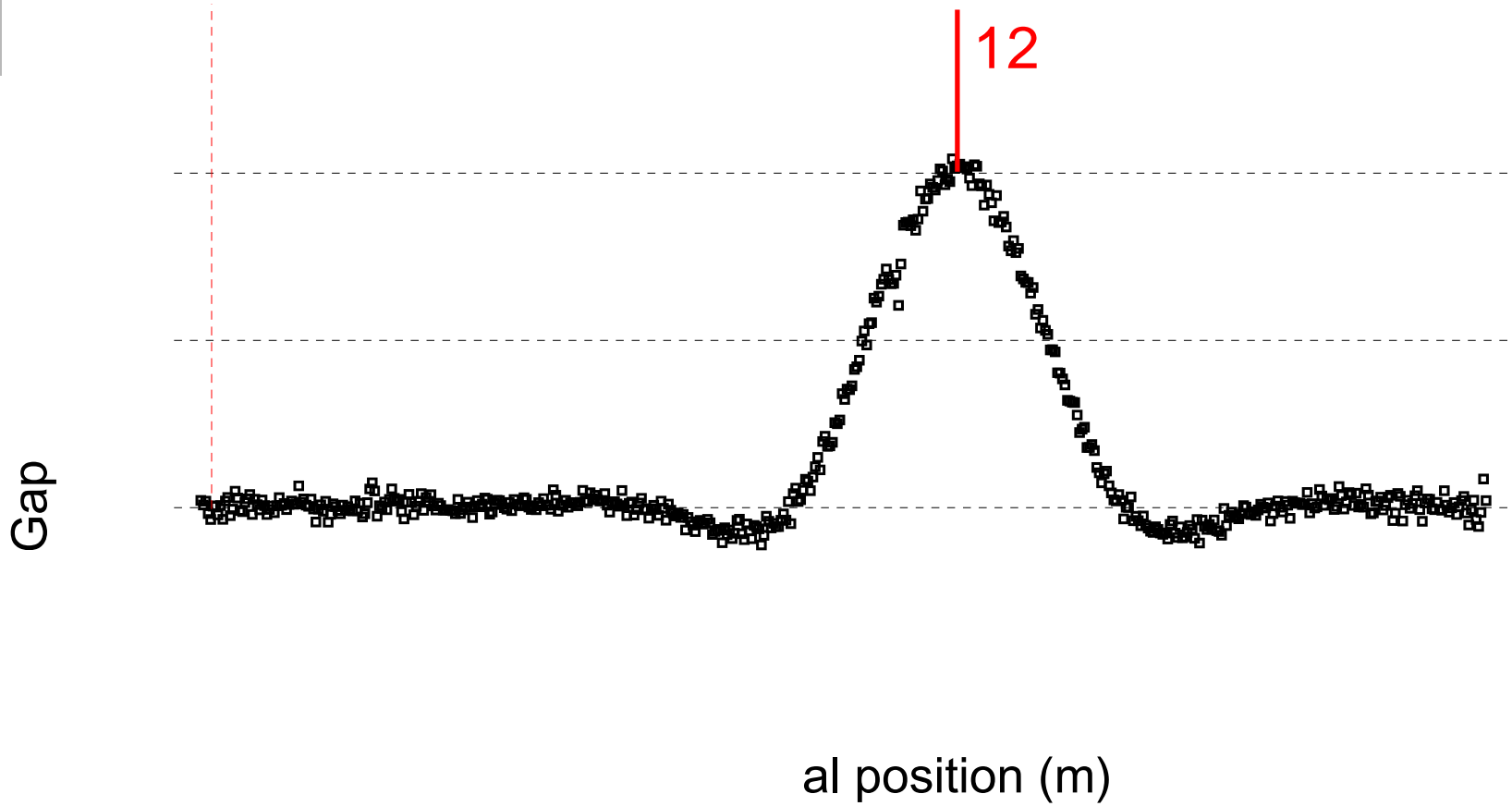
Columns optimisation



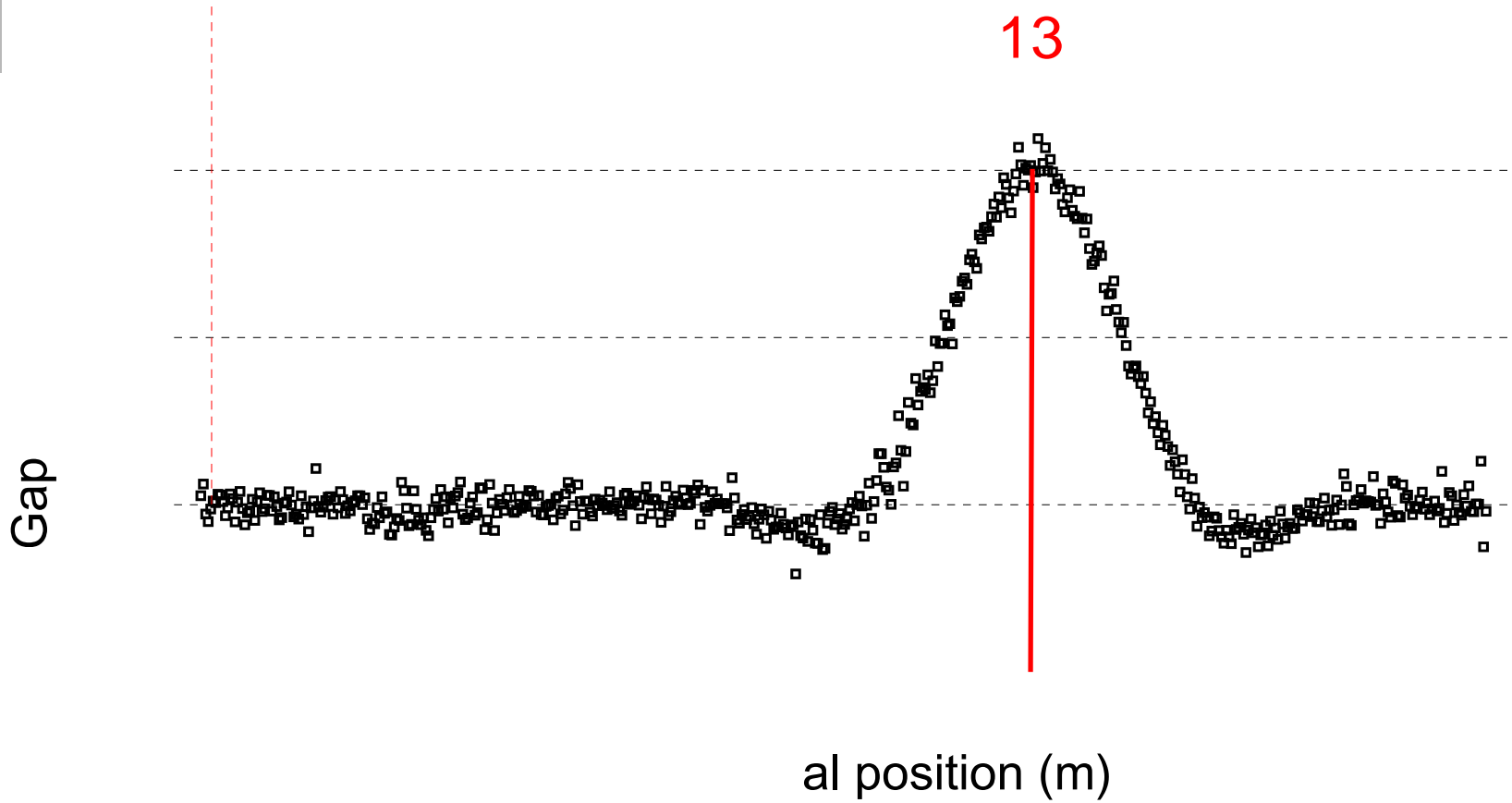
Columns optimisation



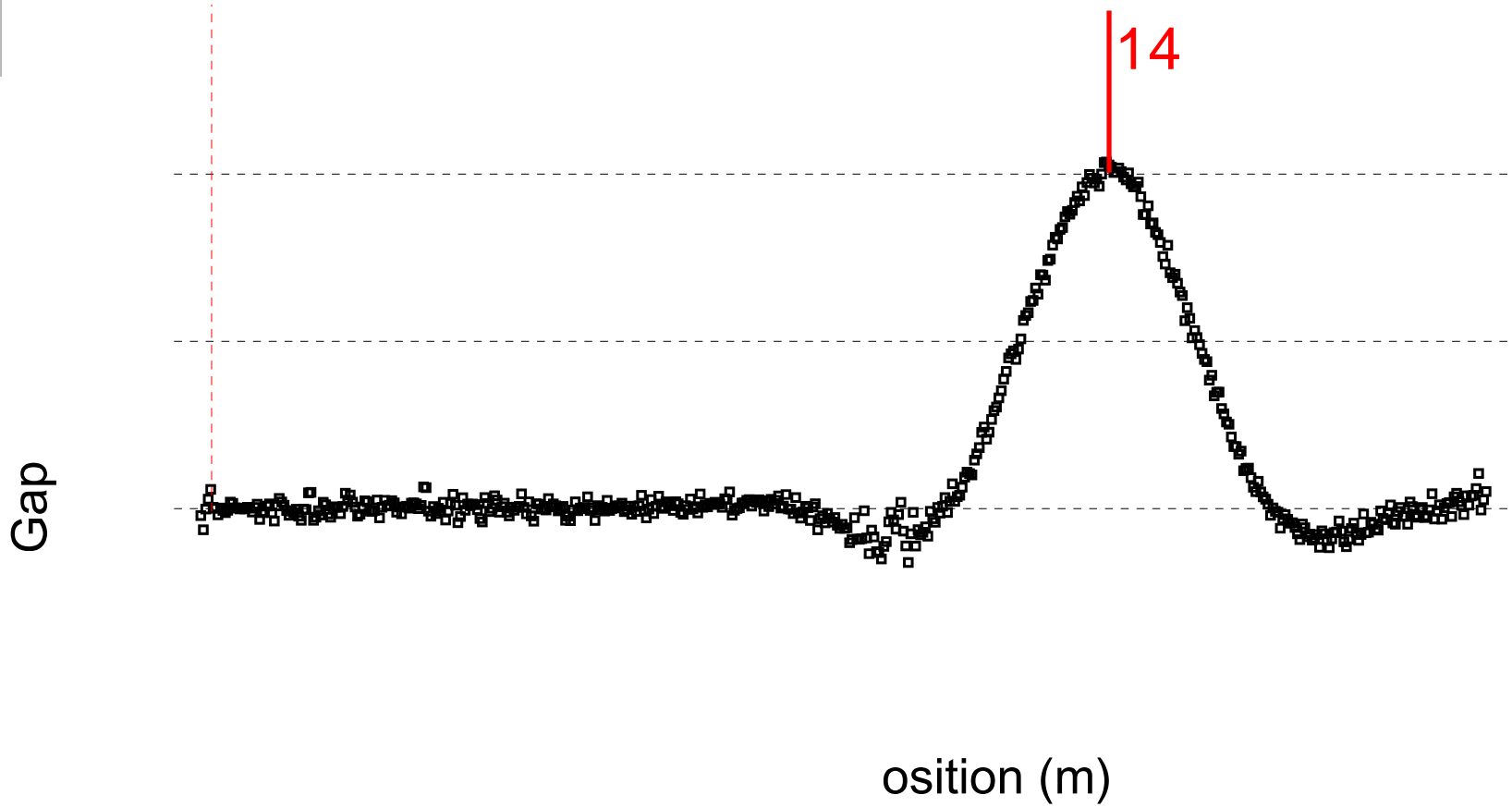
Columns optimisation



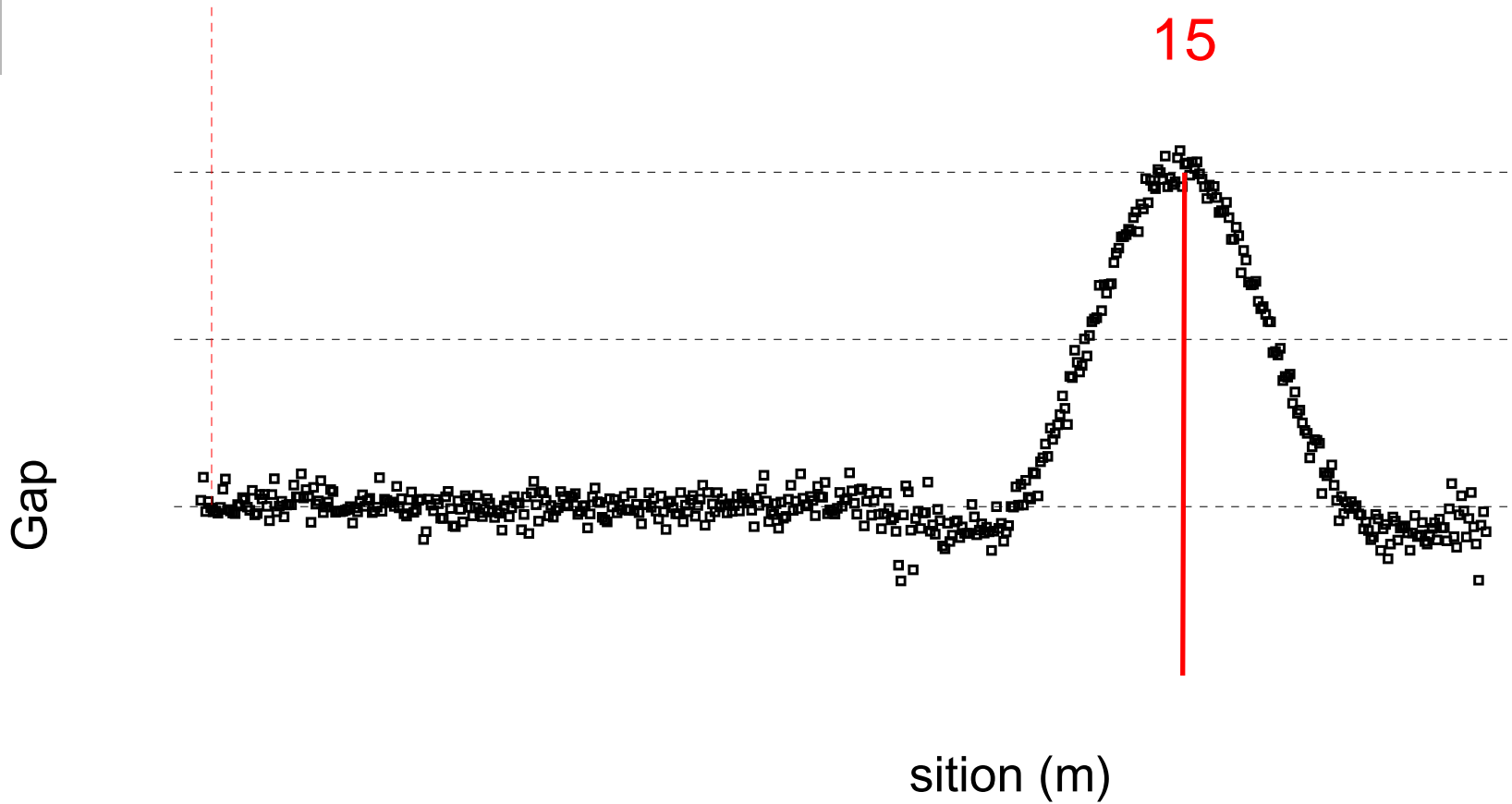
Columns optimisation



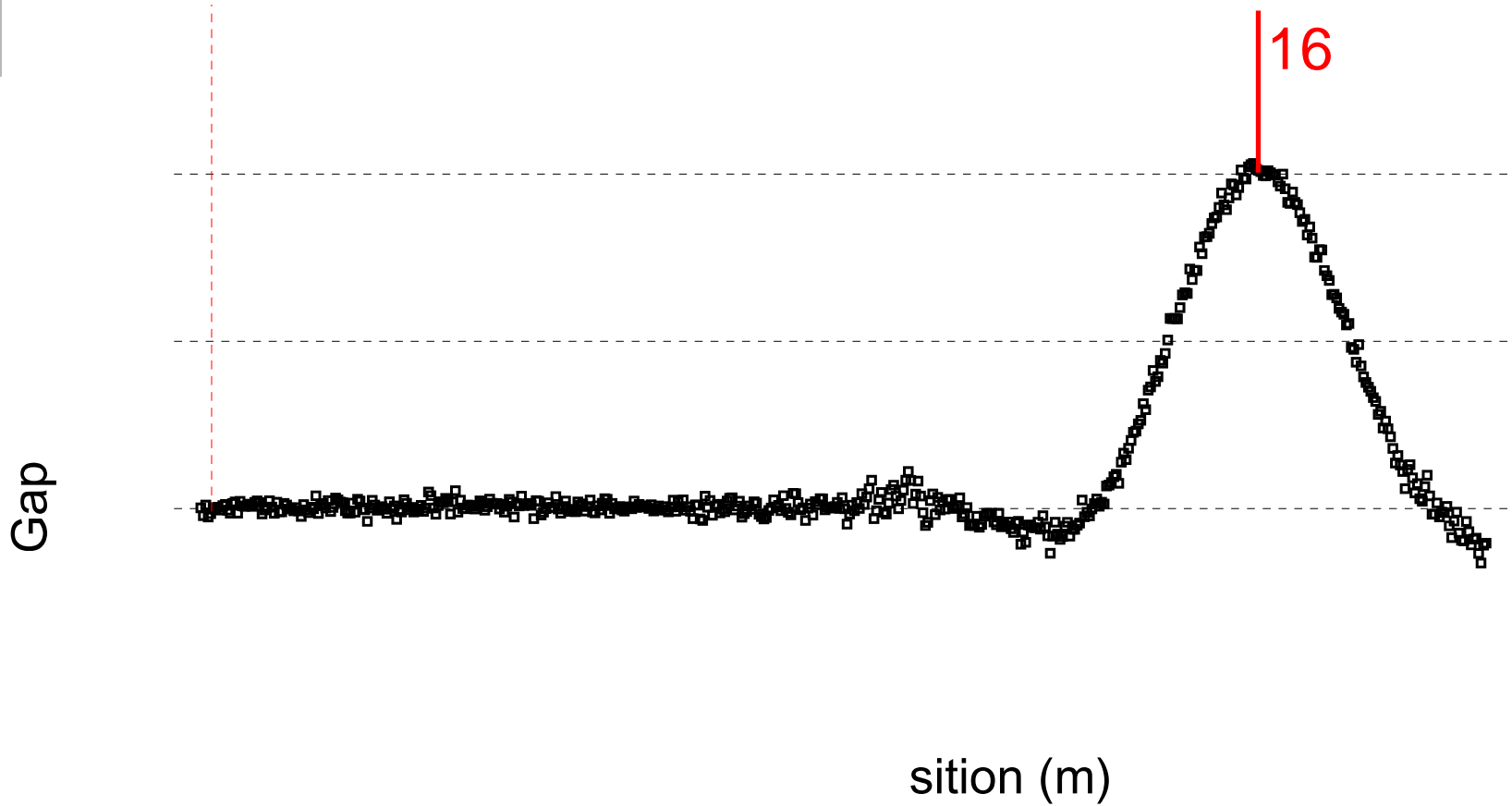
Columns optimisation



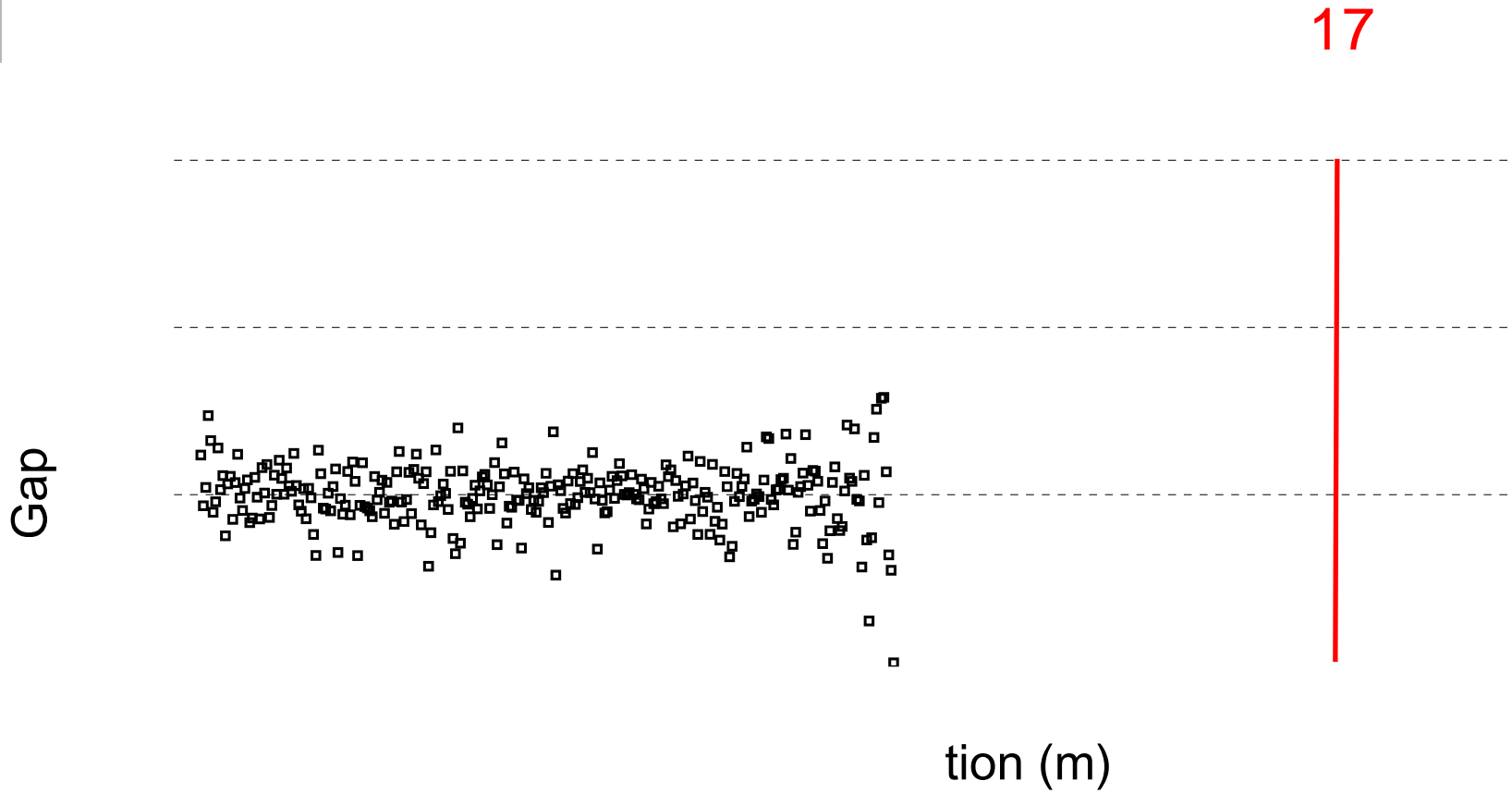
Columns optimisation



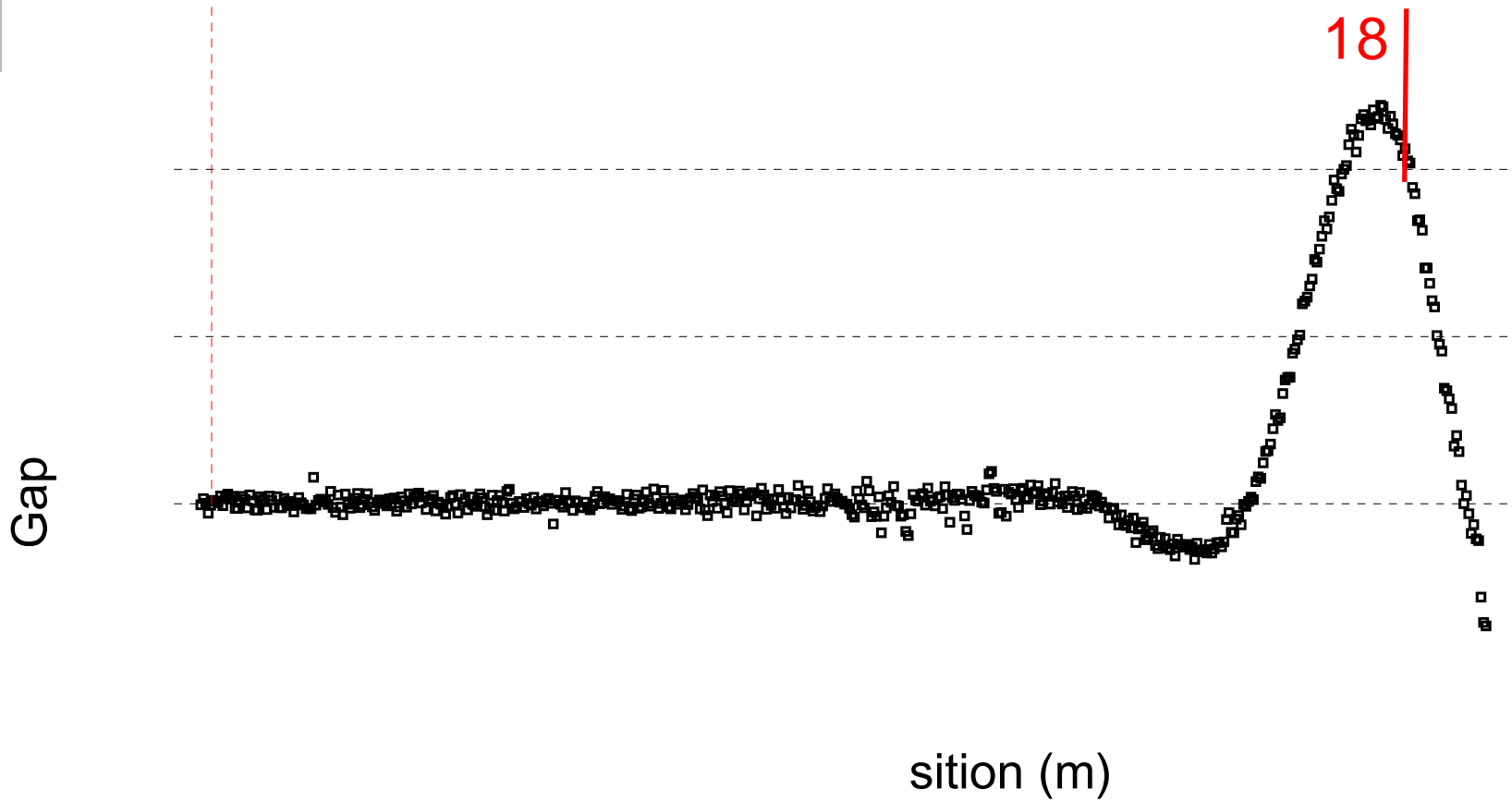
Columns optimisation



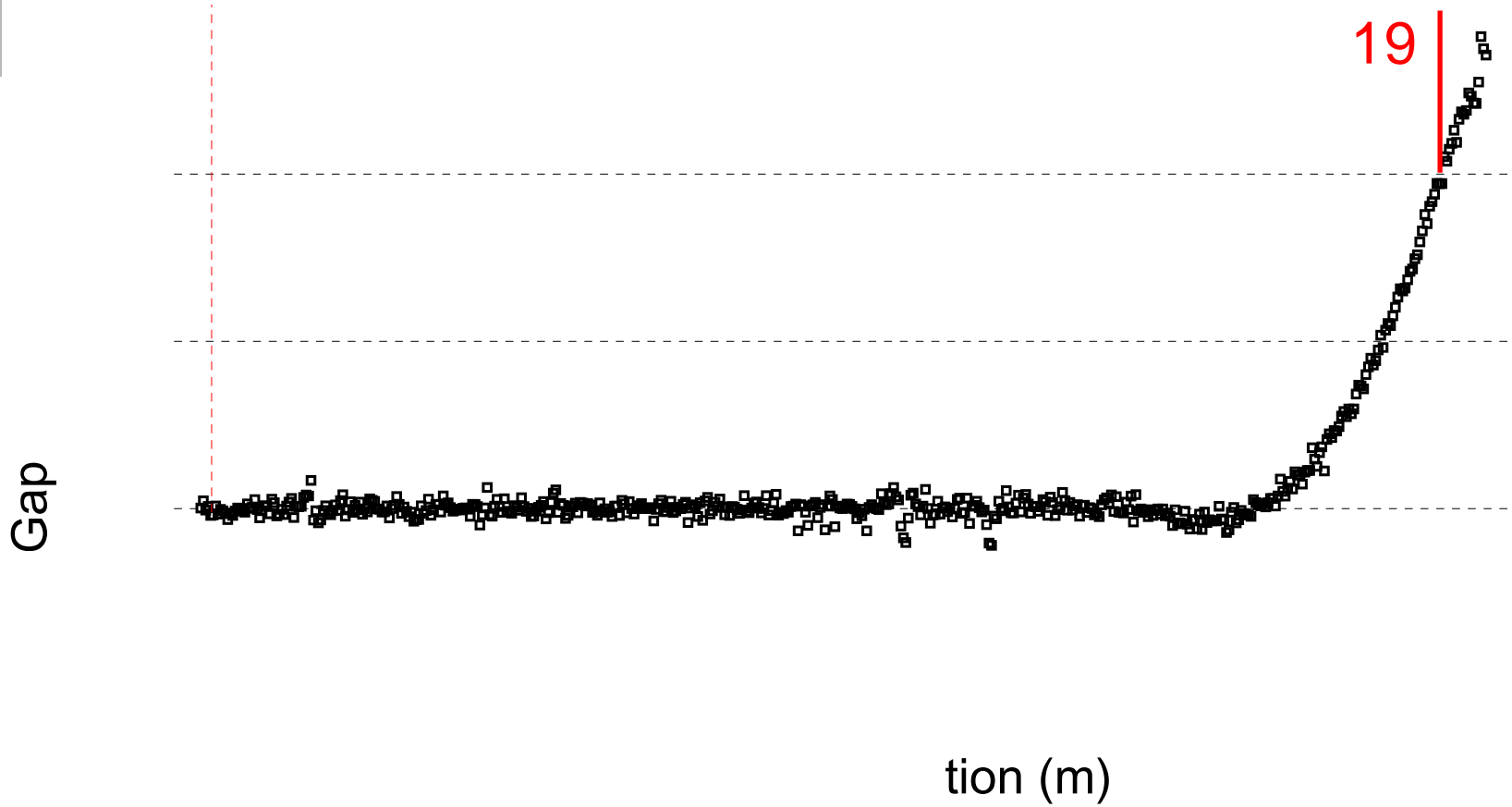
Columns optimisation



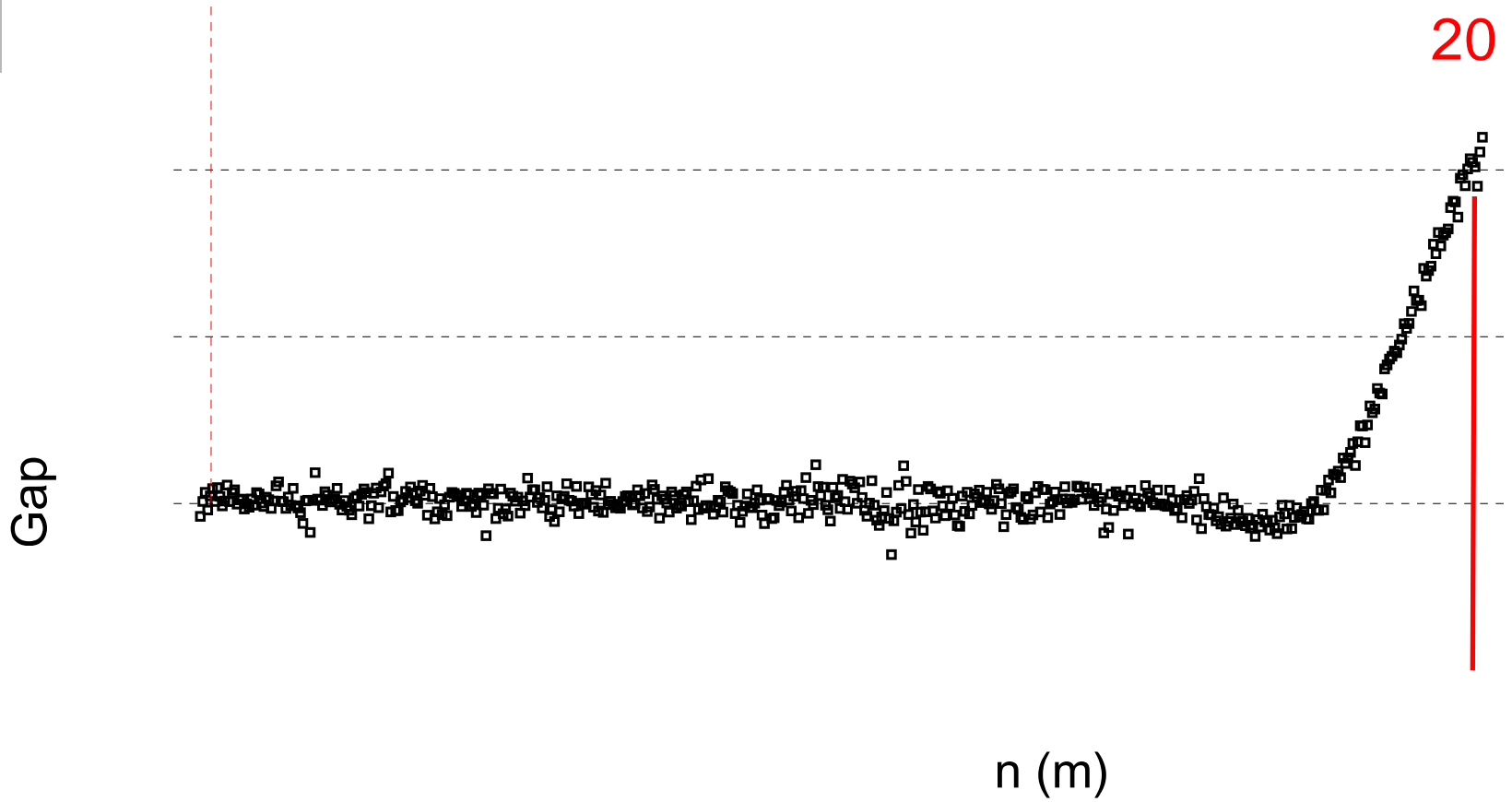
Columns optimisation



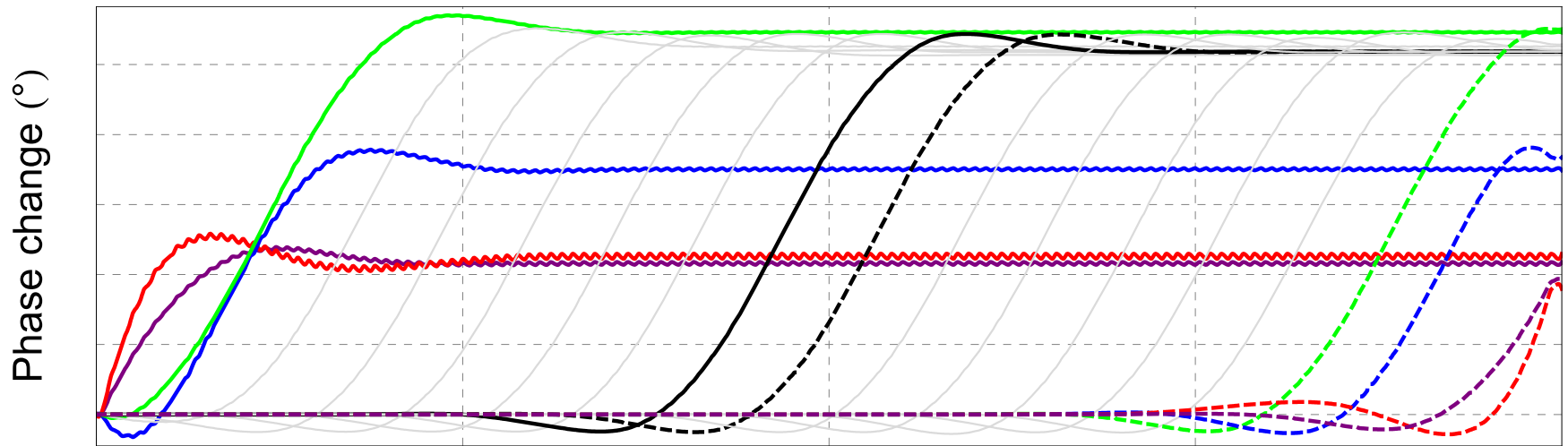
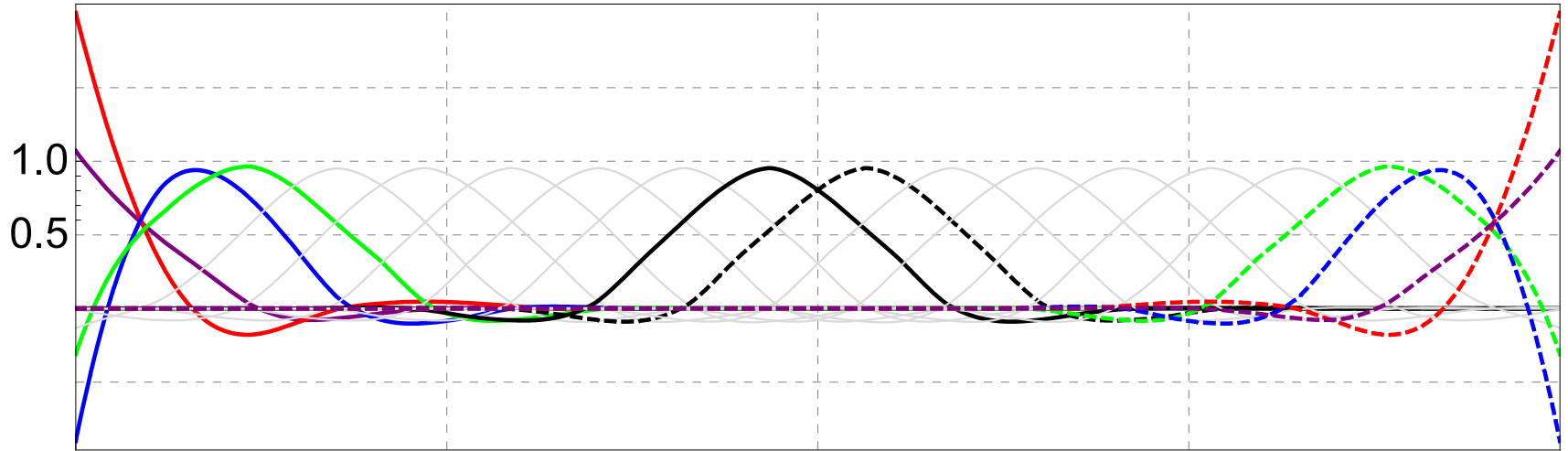
Columns optimisation



Columns optimisation



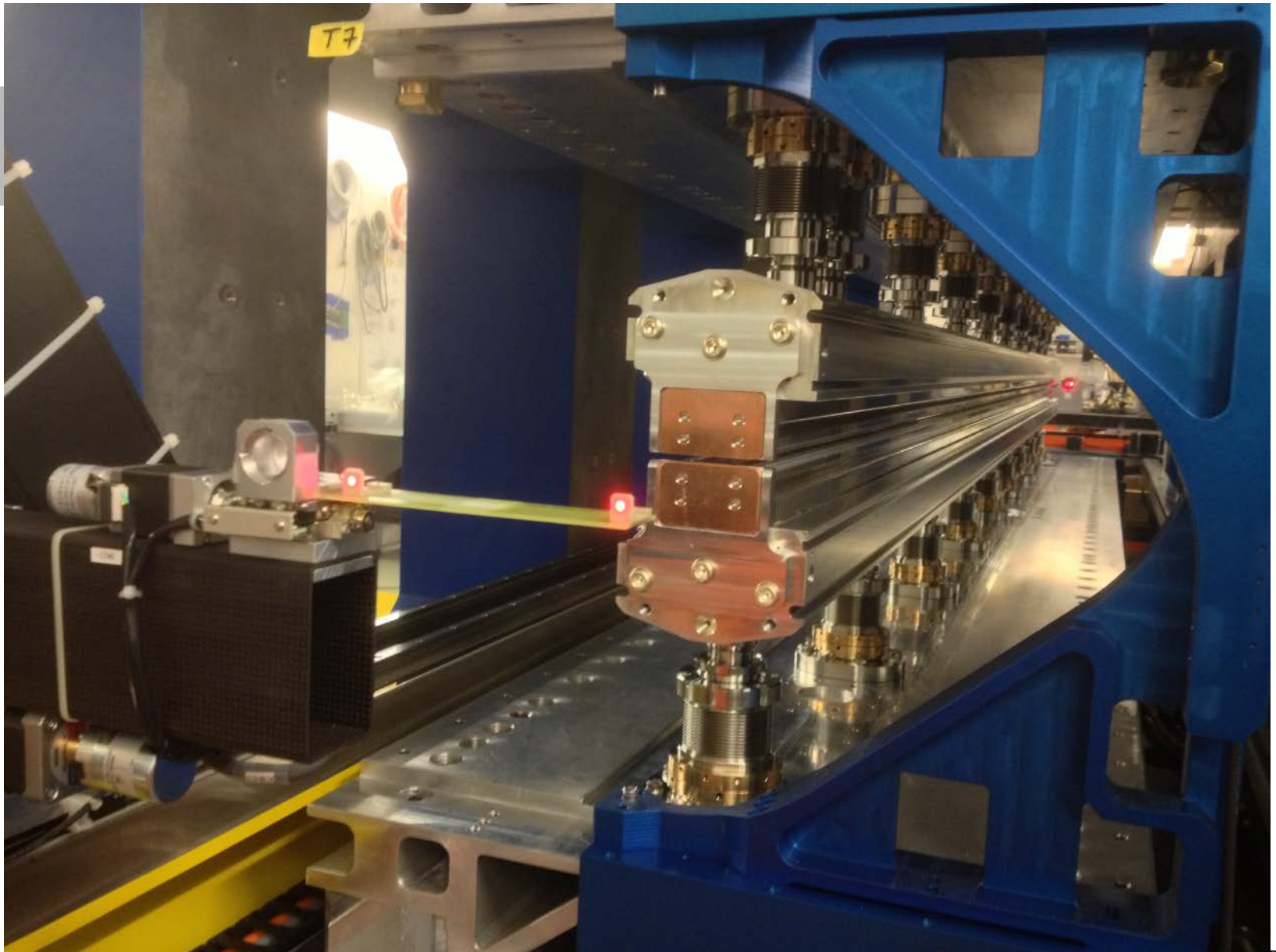
Columns optimisation



ng the inner l-beam (m)

- Introduction to Light Sources: PSI examples
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Ex-Vacuum Bench



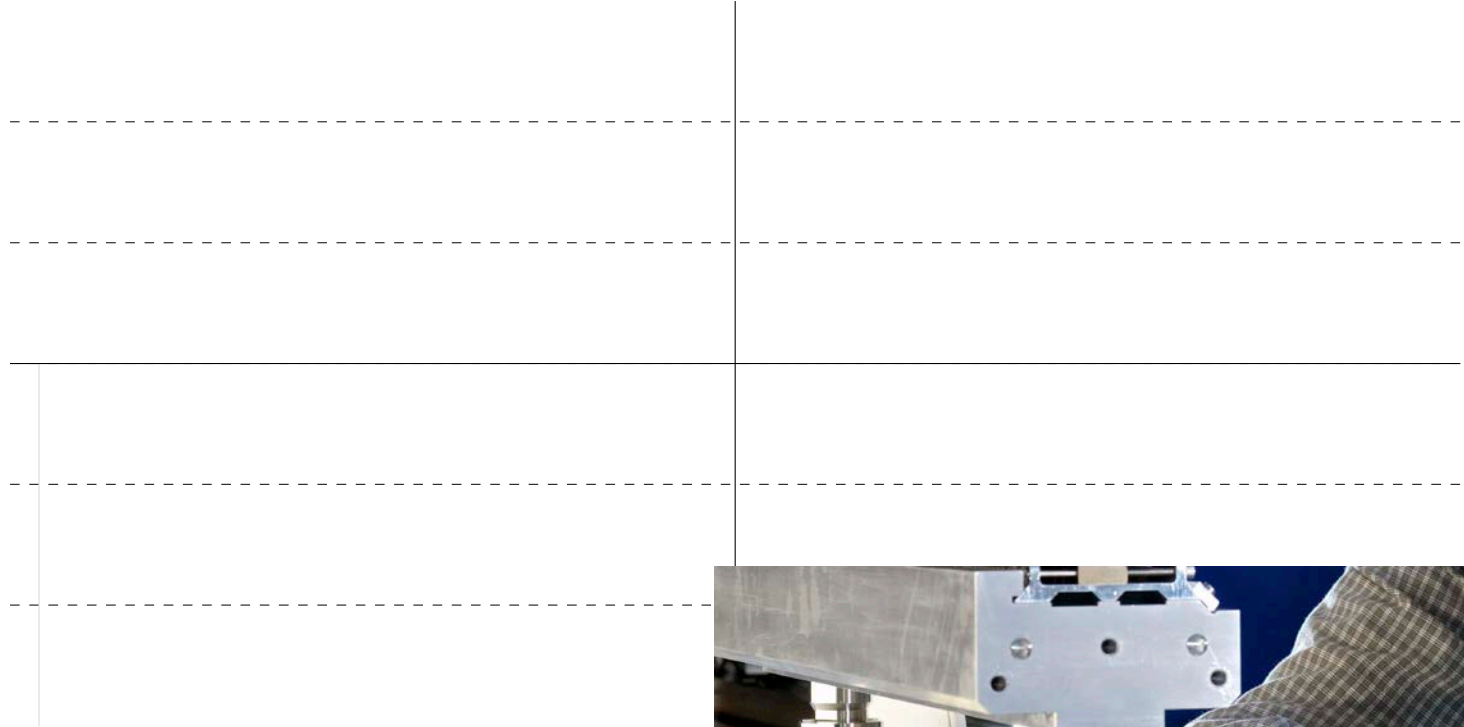
UpStr

localK optimization

$\phi_{\text{error}} : 63.8^\circ$

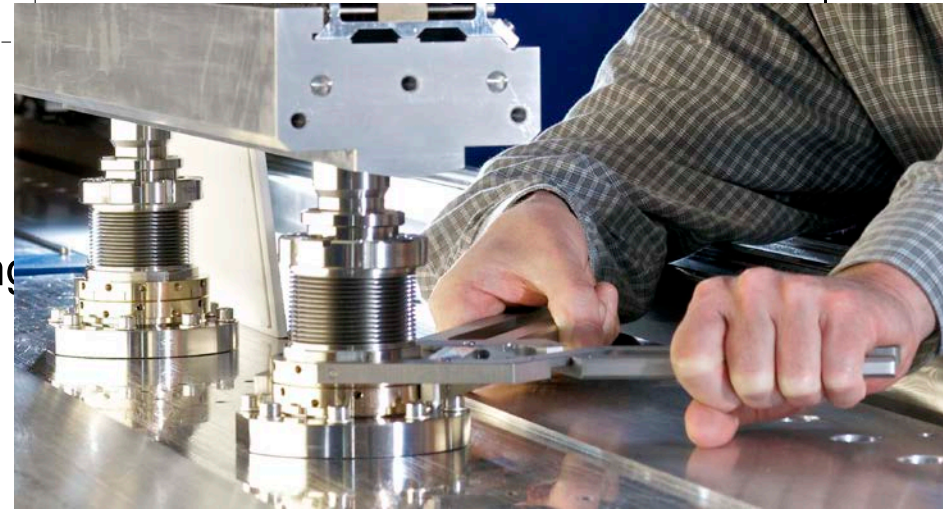
DownStr

Pole height adj (μm)



_2015-12-11-09_47_36

one



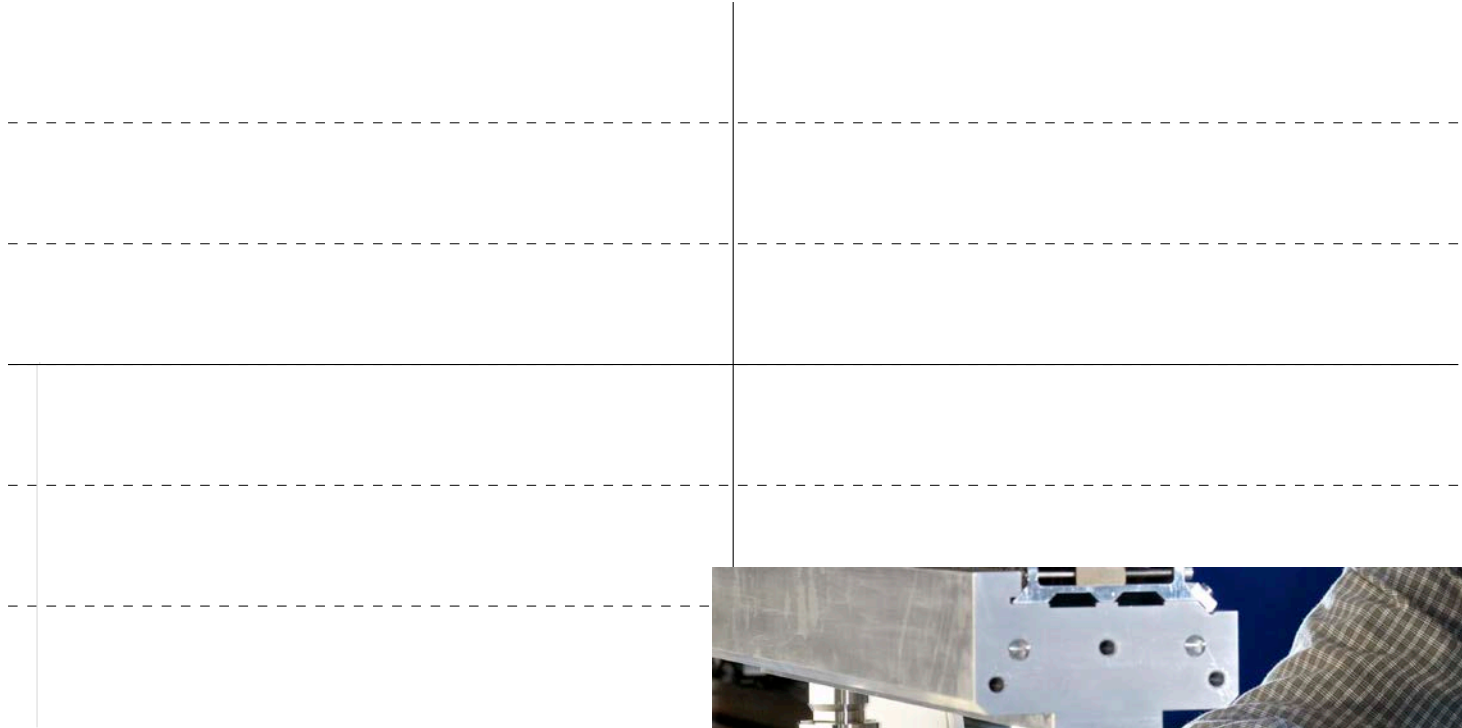
UpStr

localK optimization

$\phi_{\text{error}} : 23.0^\circ$

DownStr

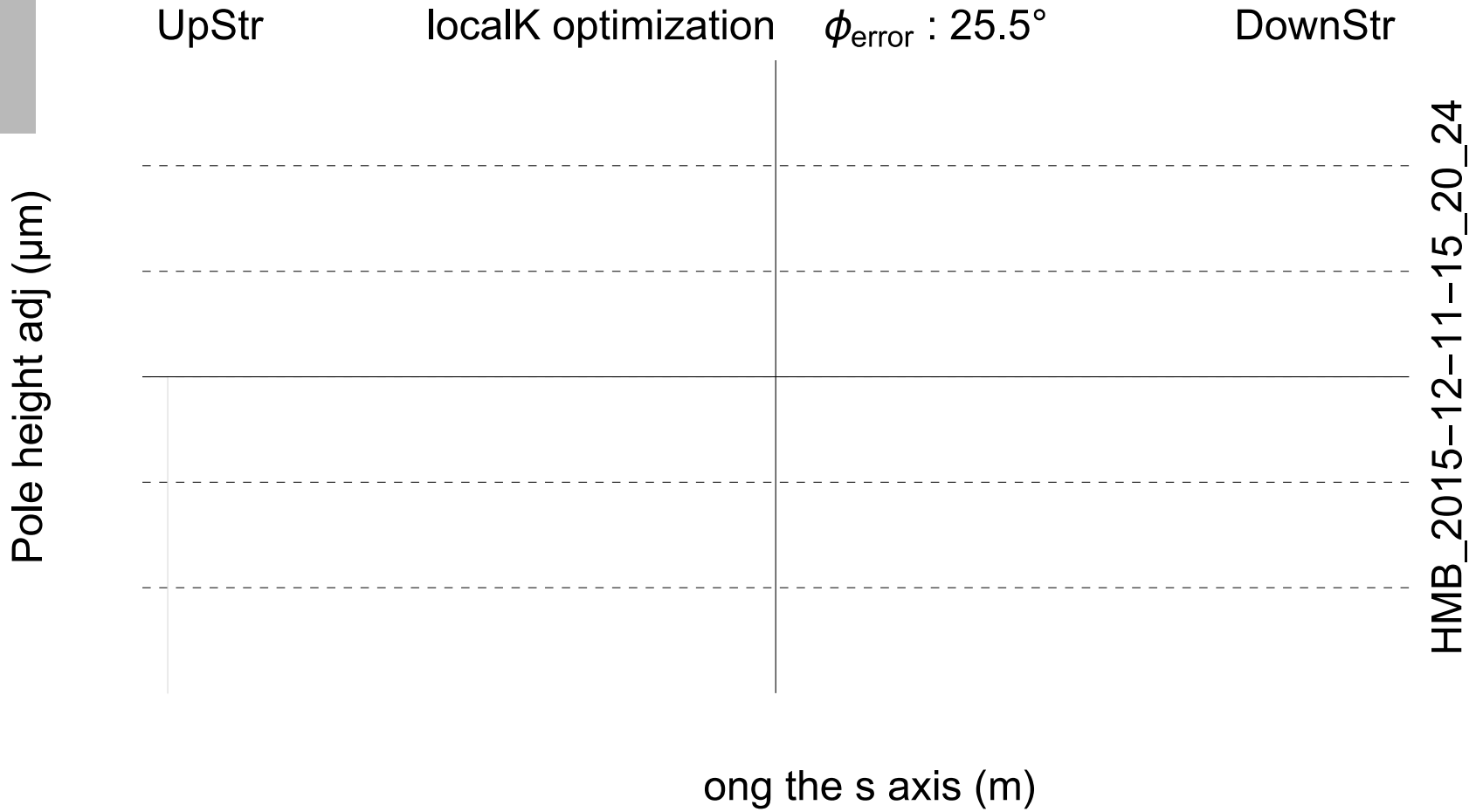
Pole height adj (μm)

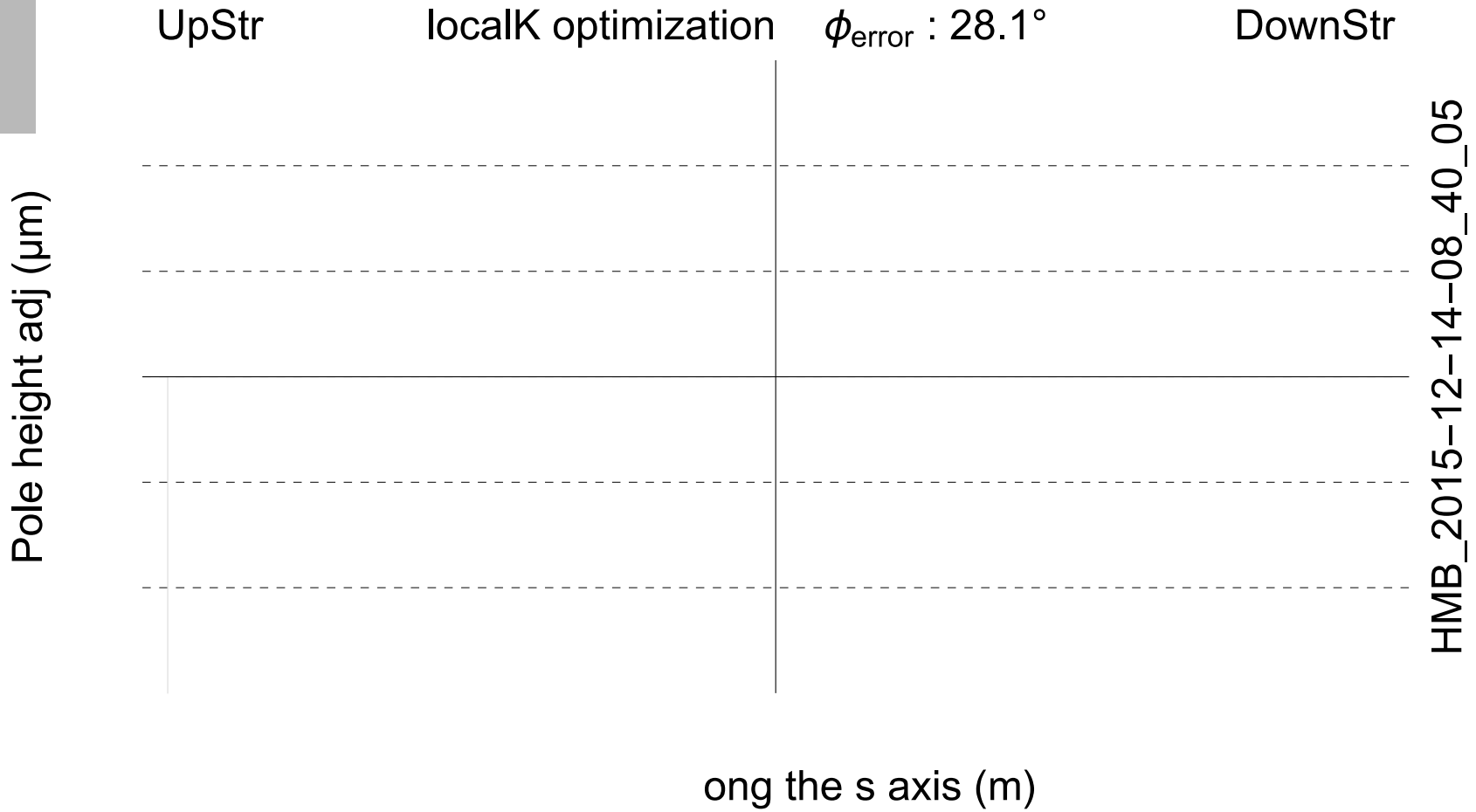


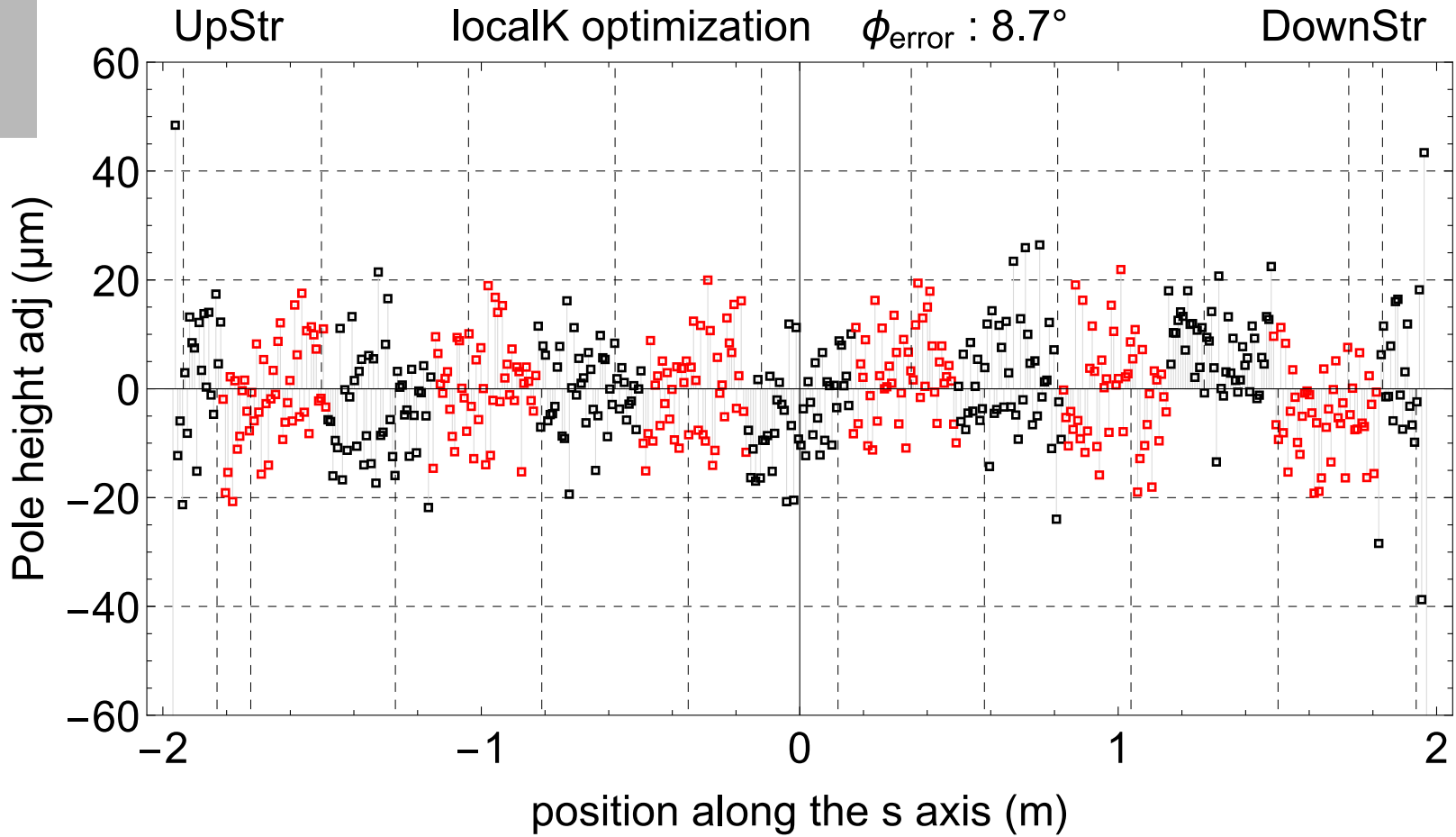
_2015-12-11-13_57_32

along

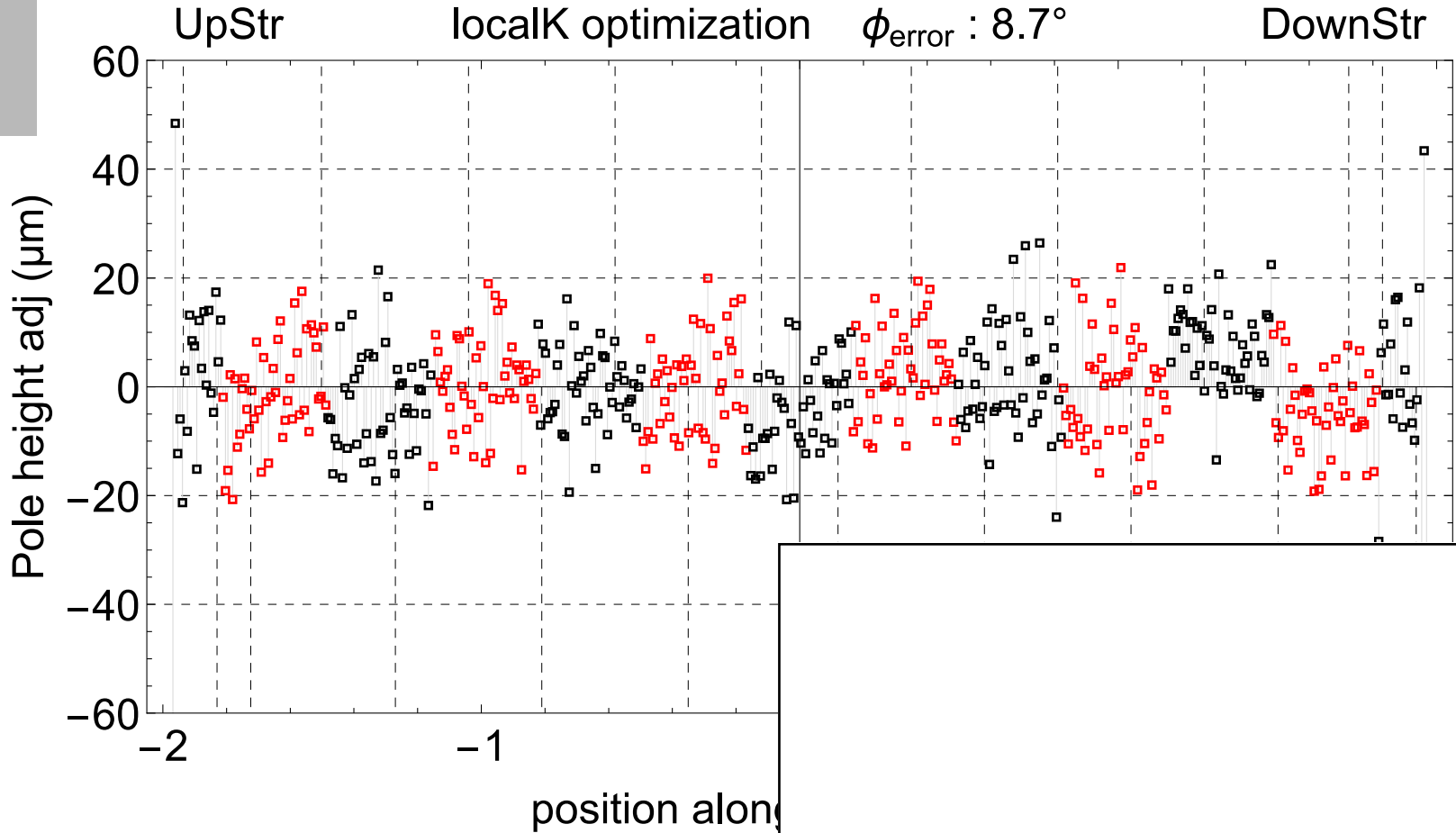






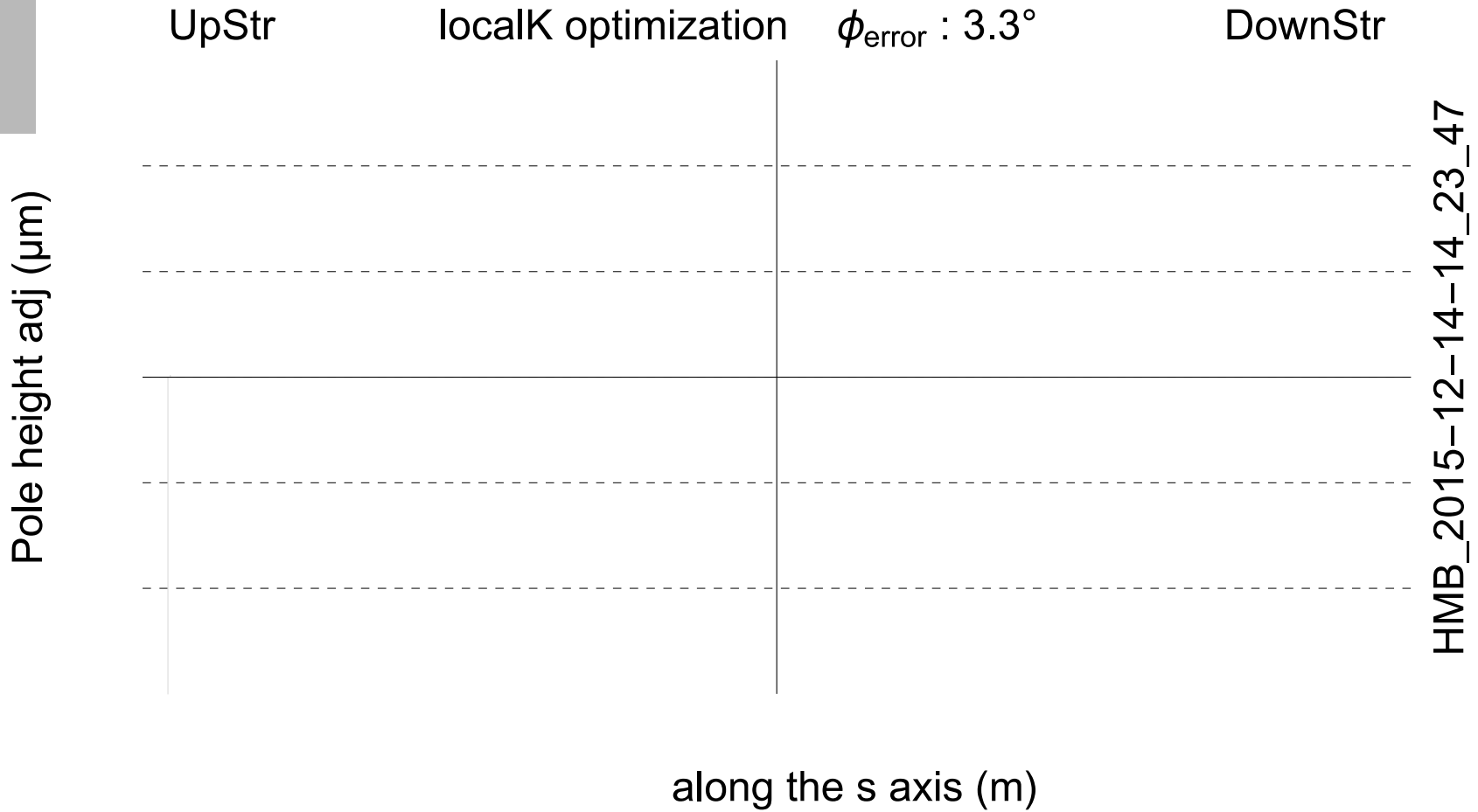


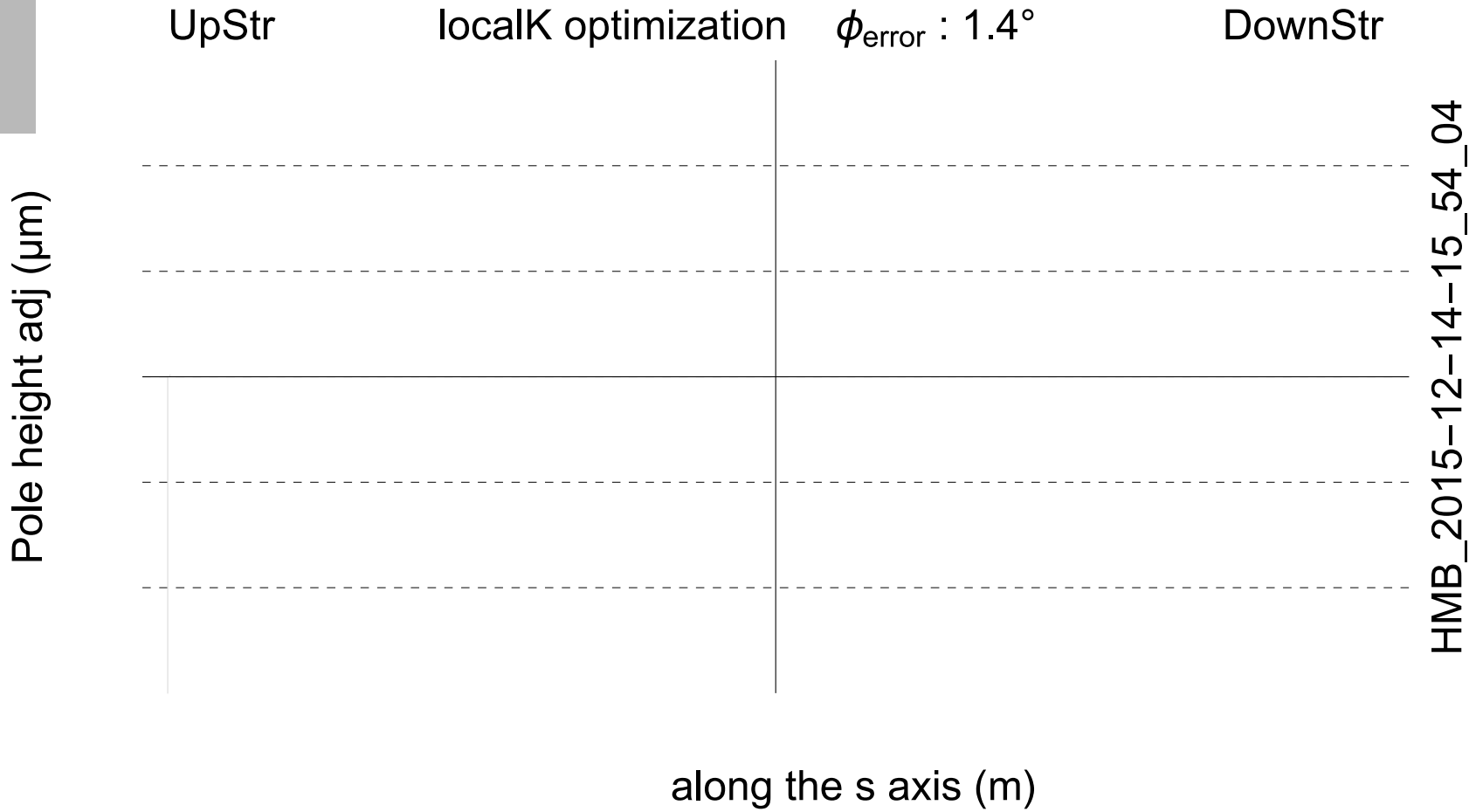
HMB_2015-12-14-10_18_13

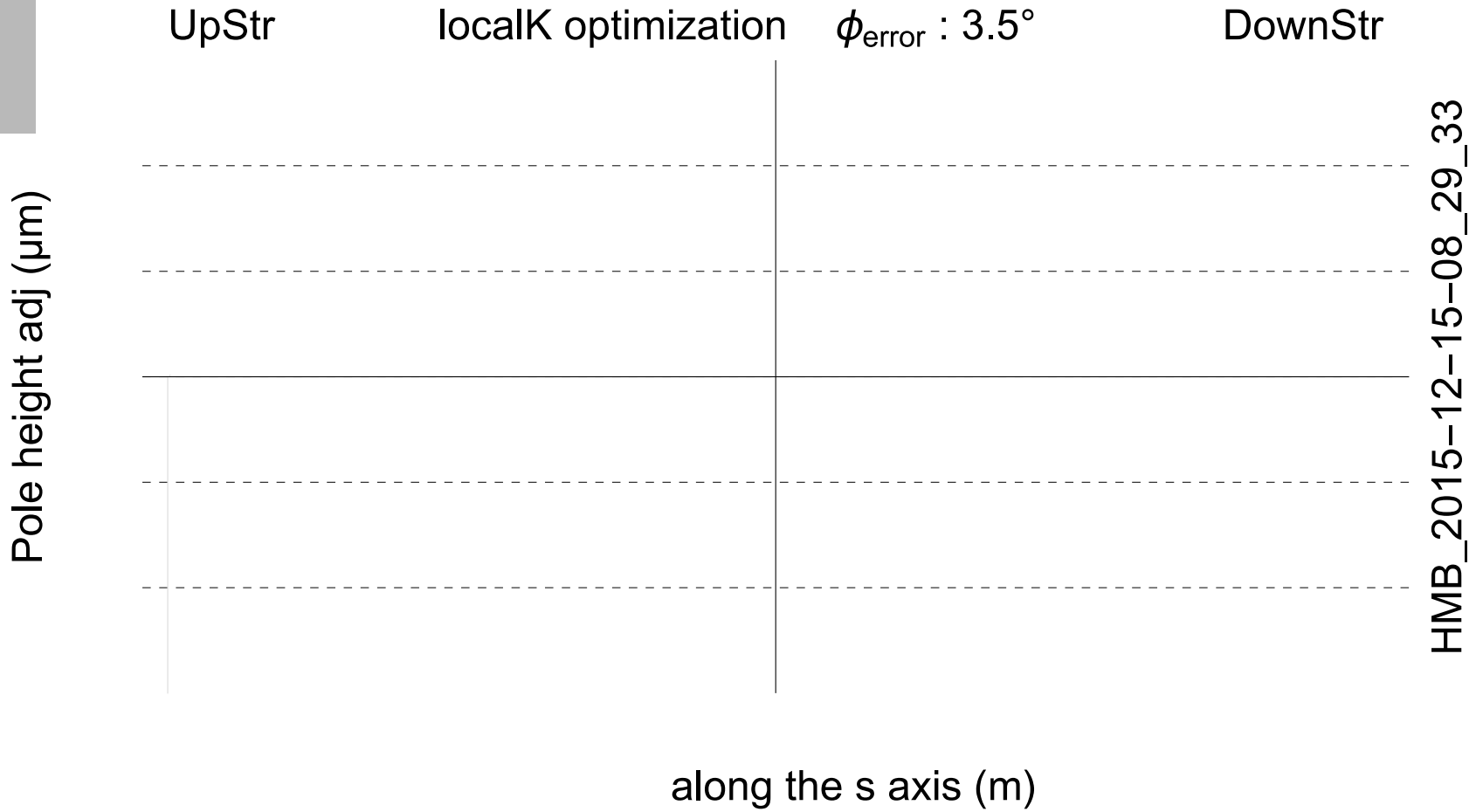


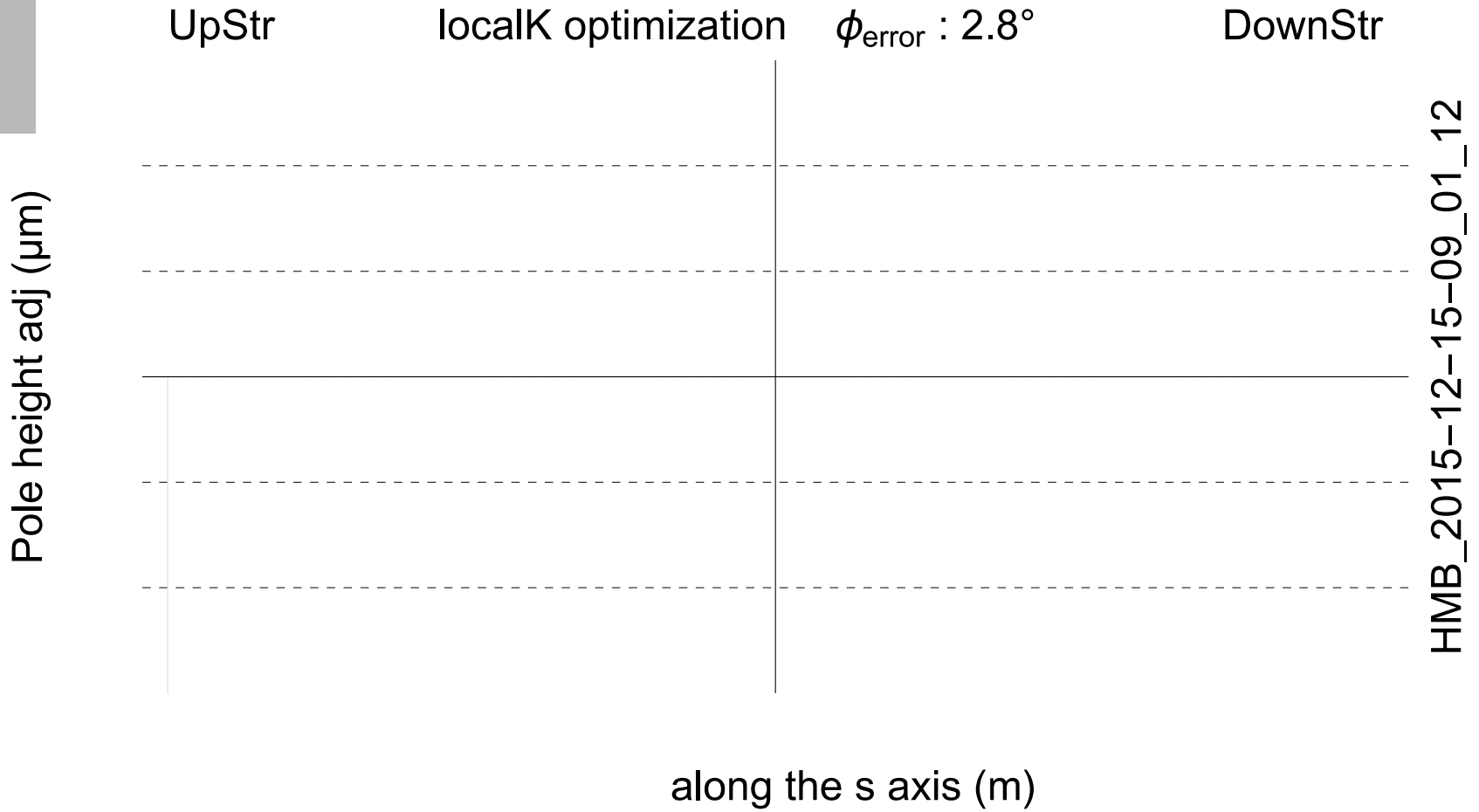
2015-12-14-10_18_13

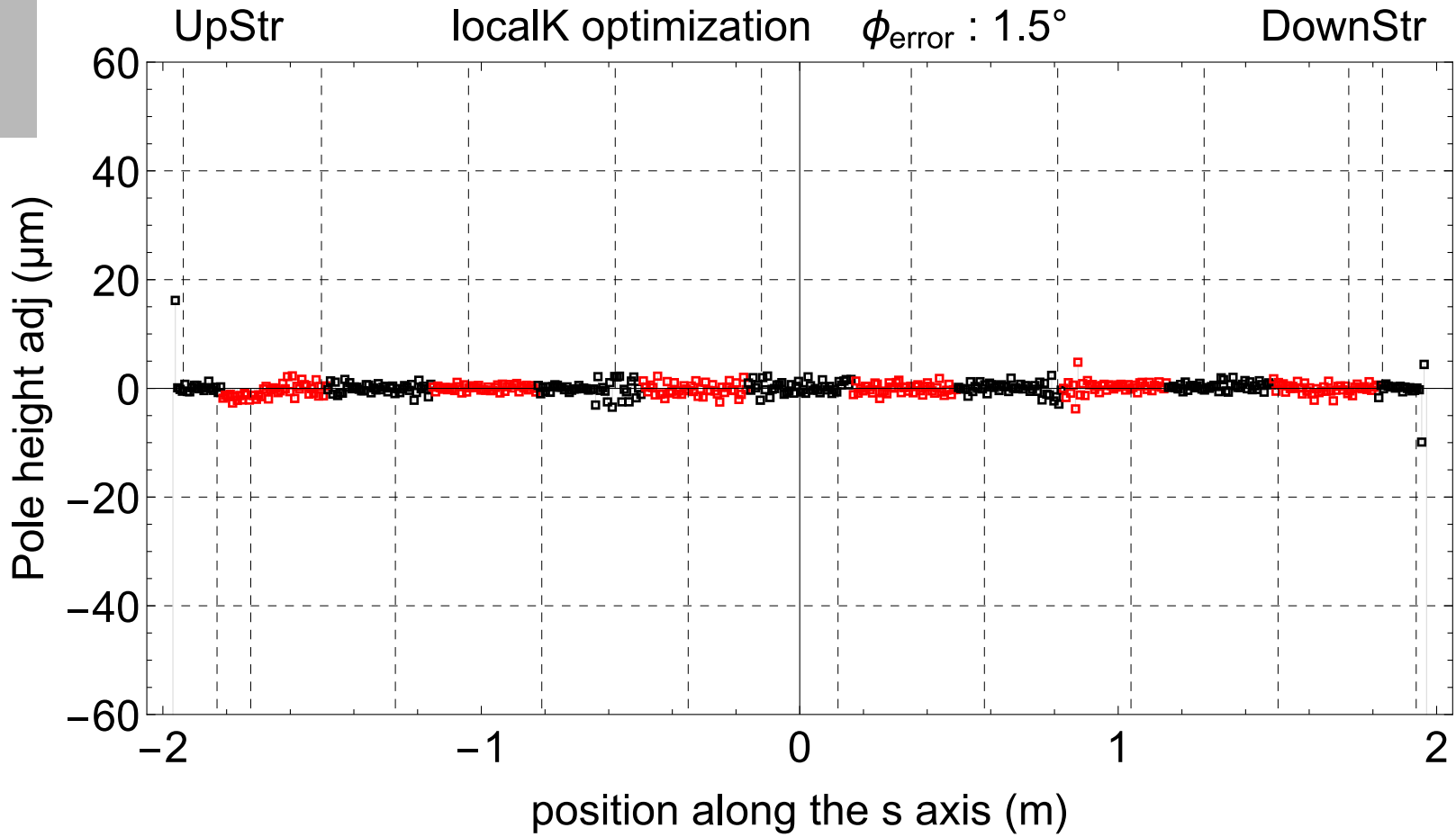




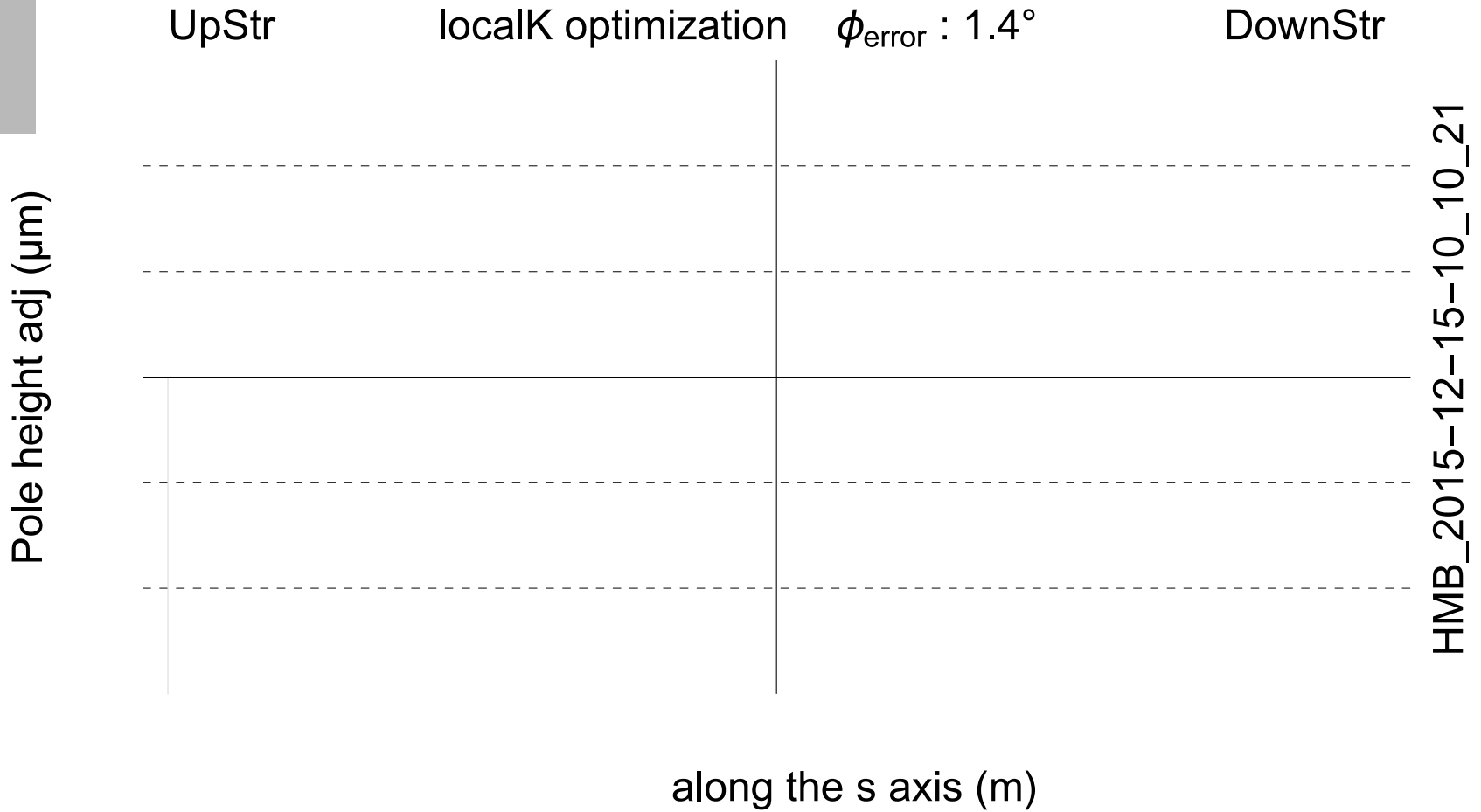


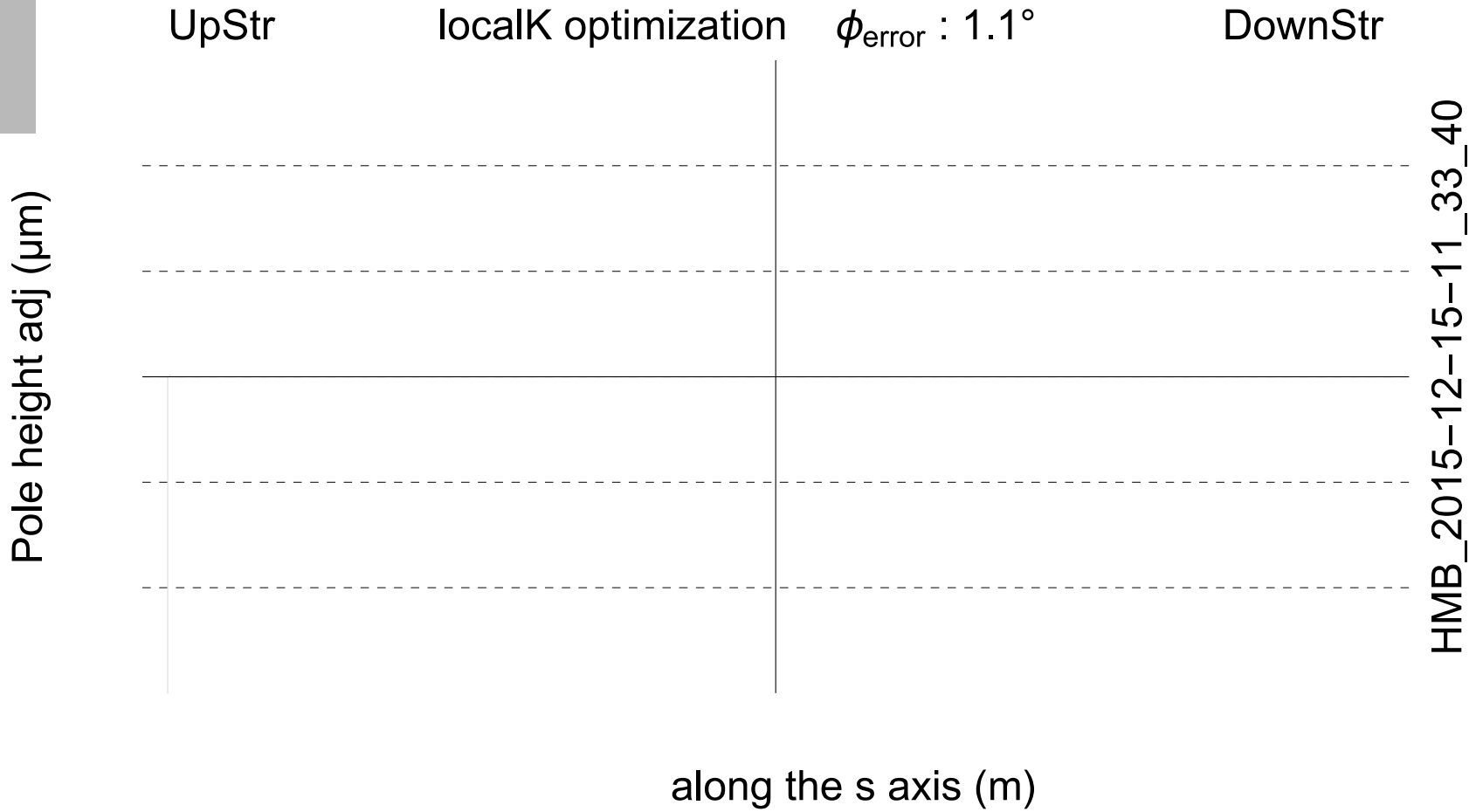






HMB_2015-12-15-09_53_27

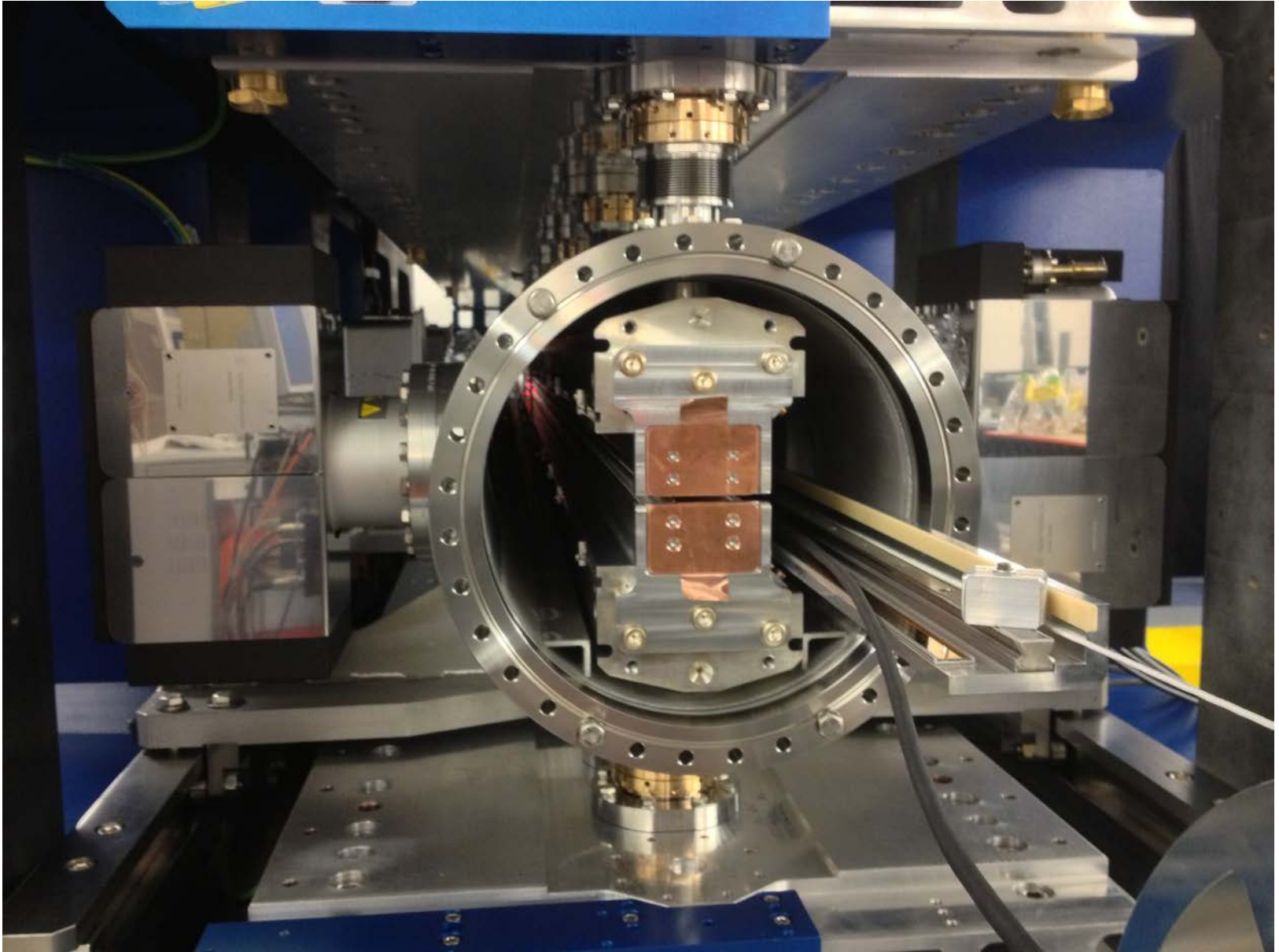


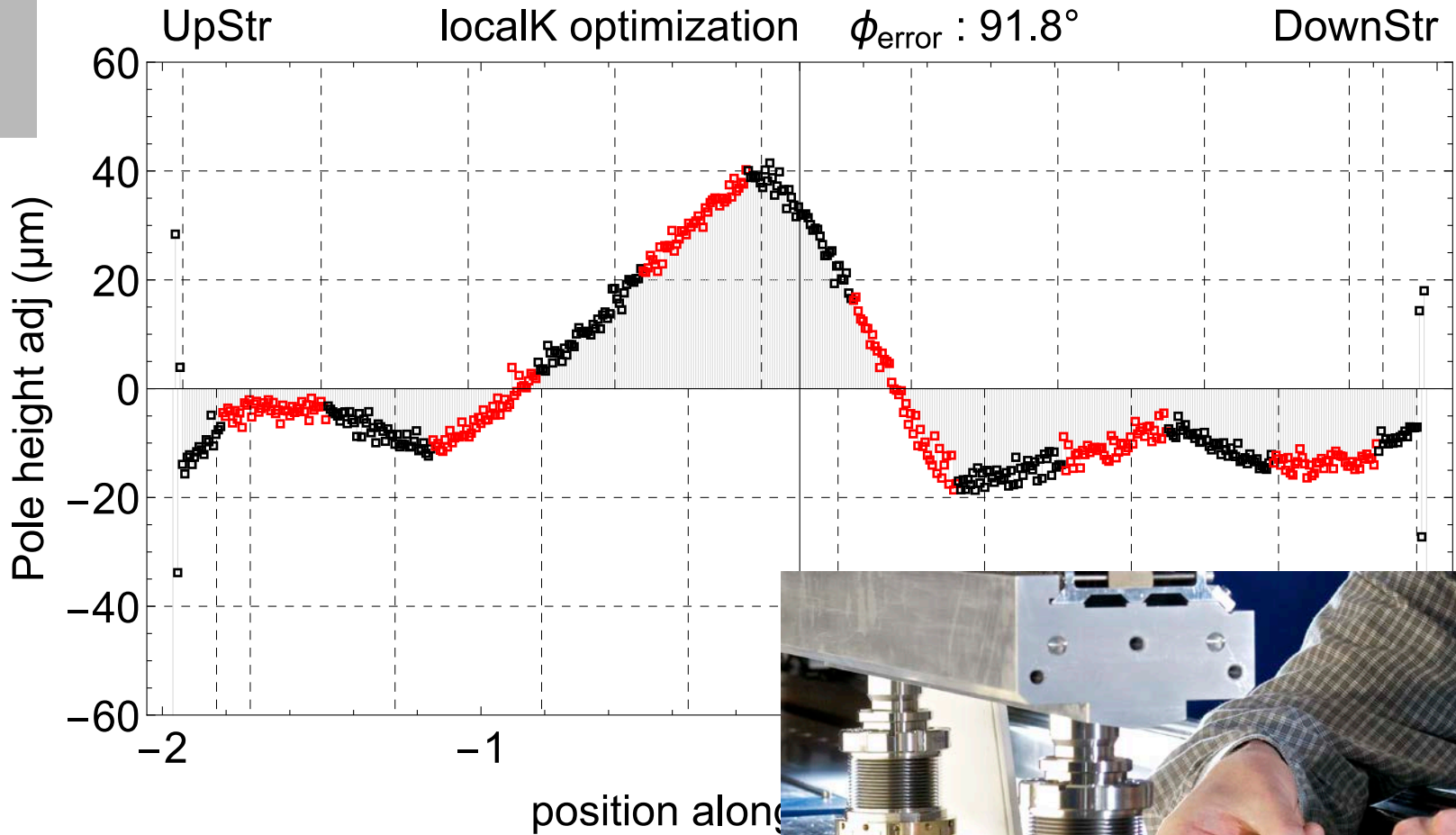


Moving to Bench B



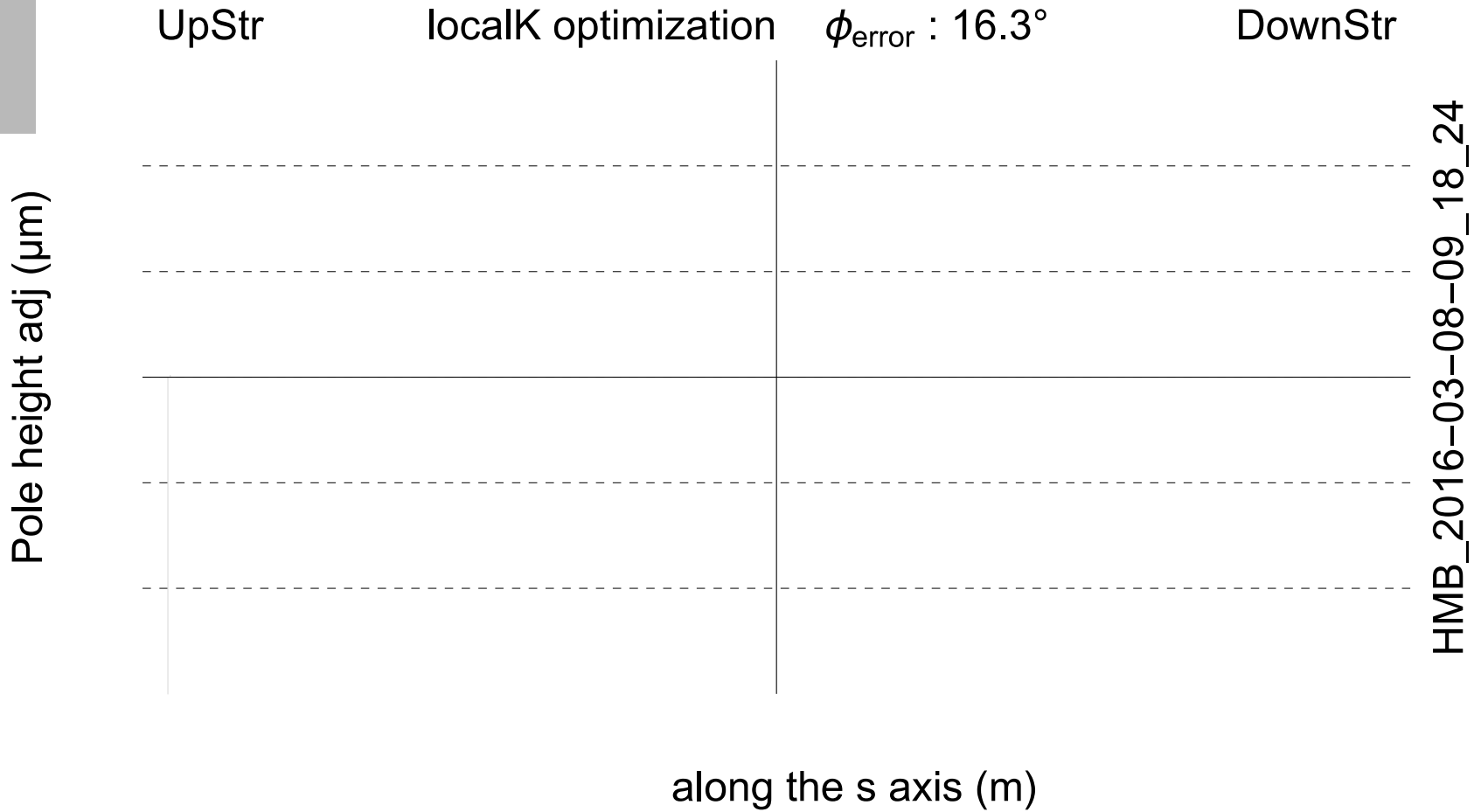
In-vacuum bench

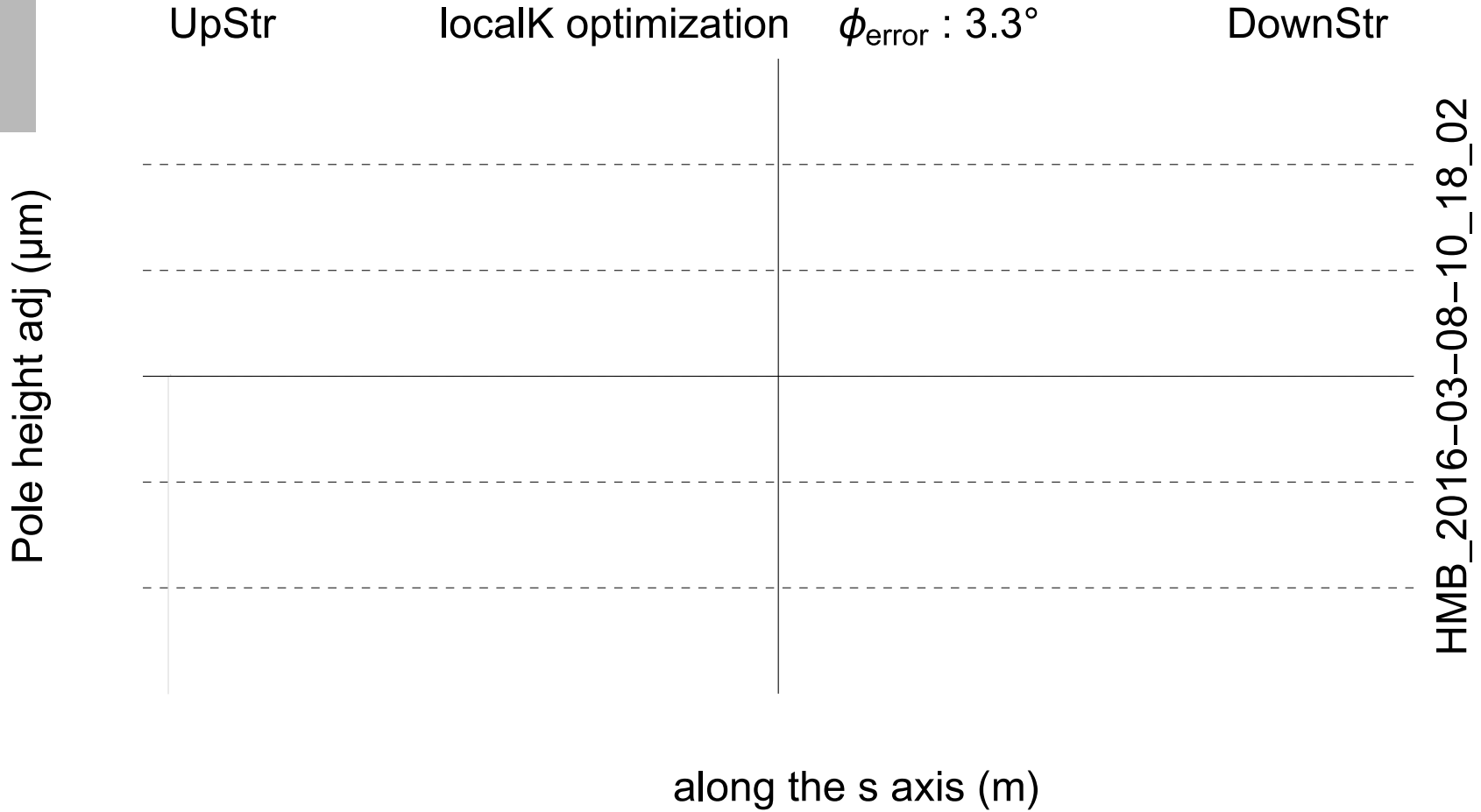


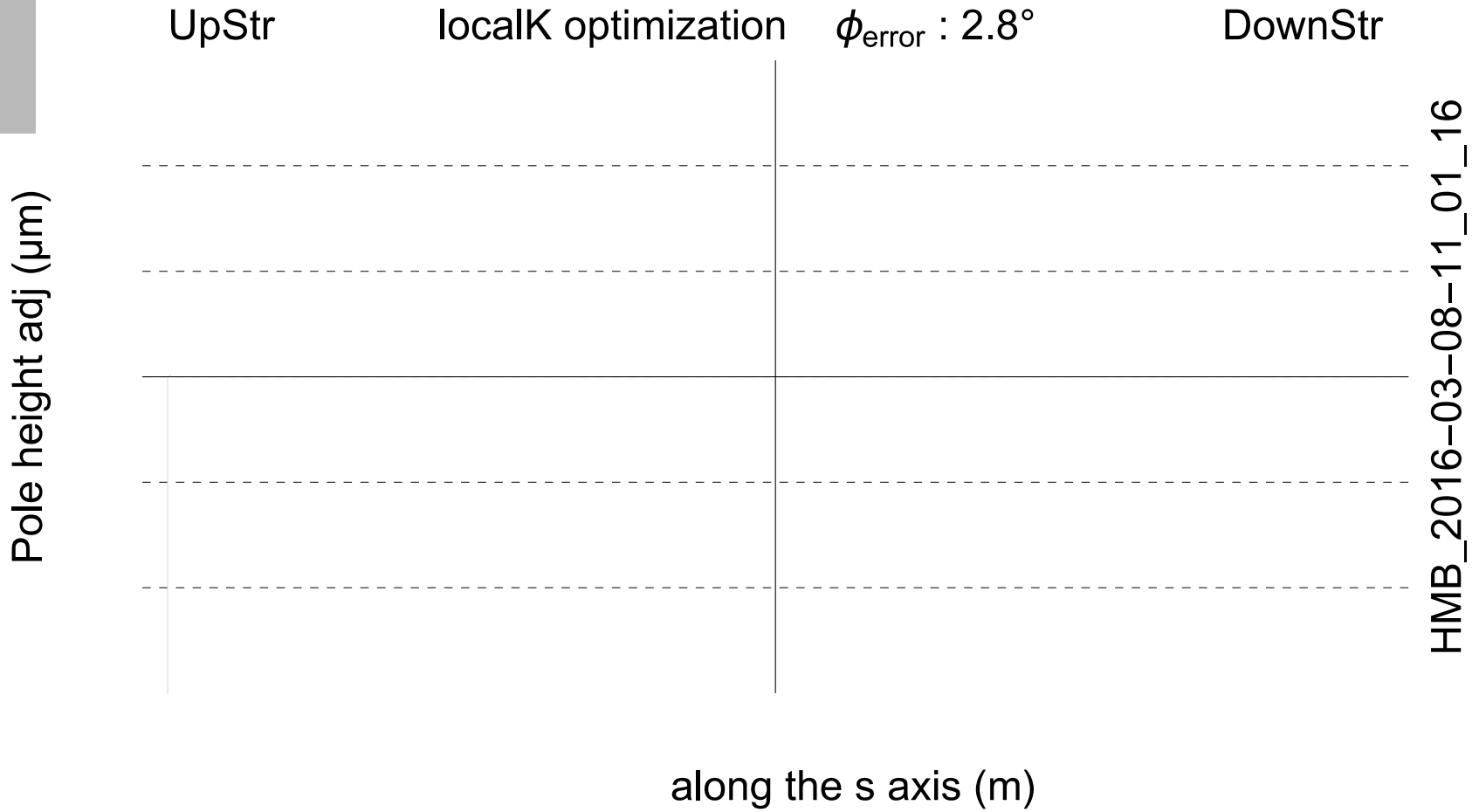


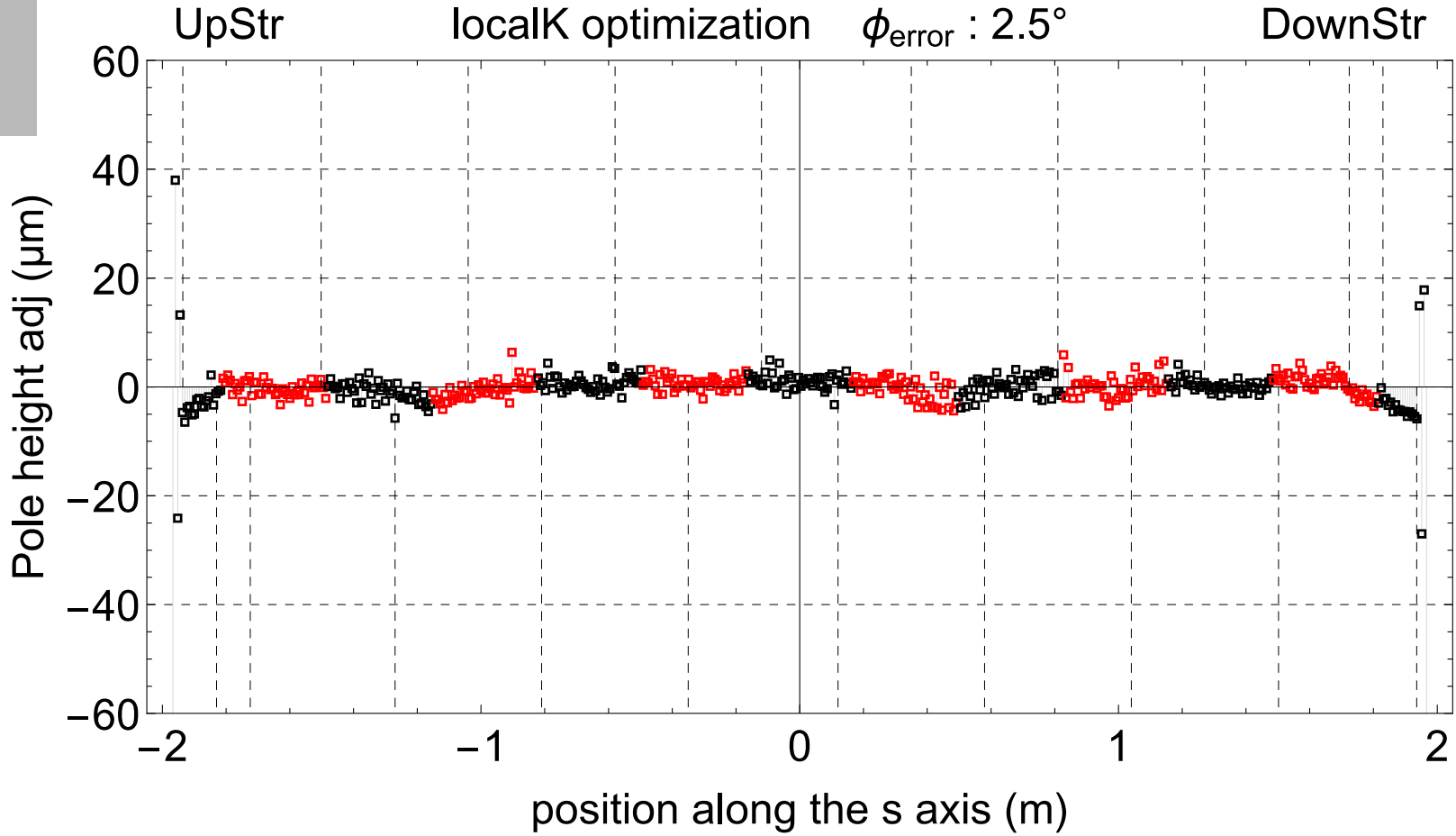
2016-03-07-14_40_41



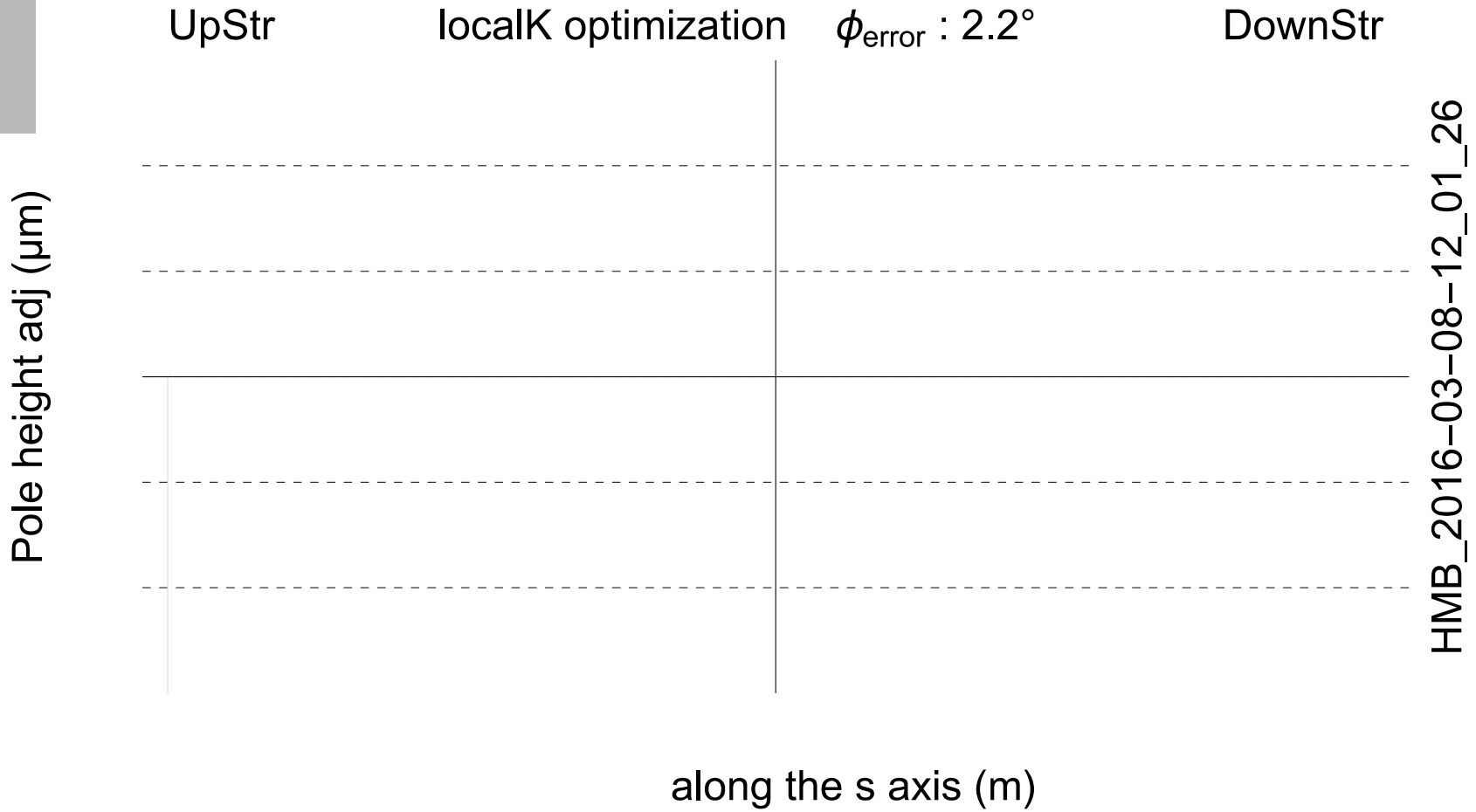




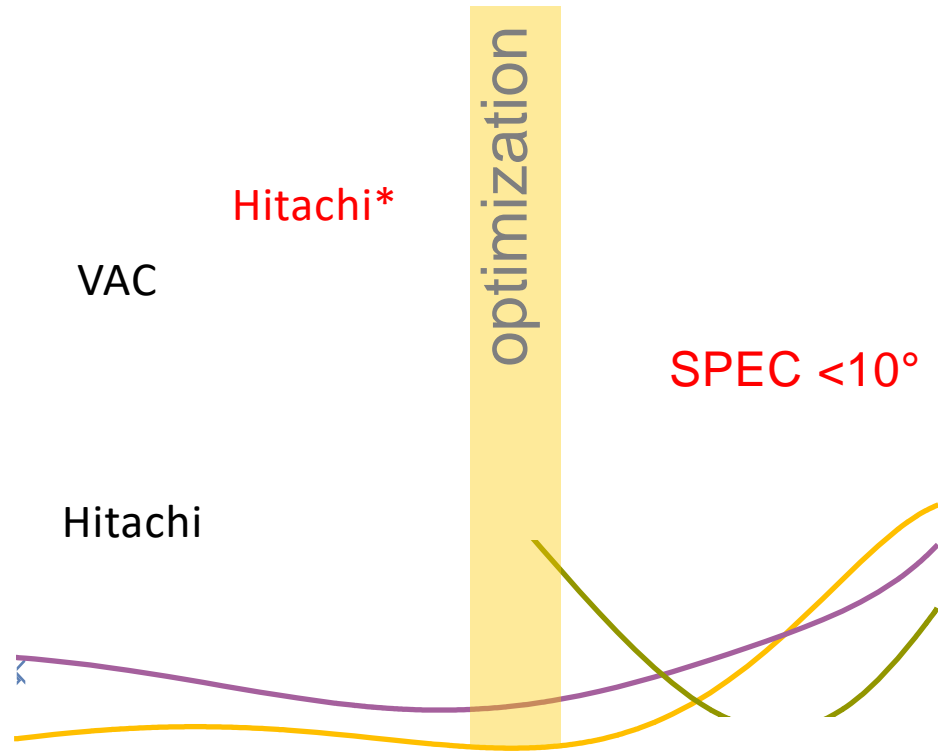




HMB_2016-03-08-11_32_05

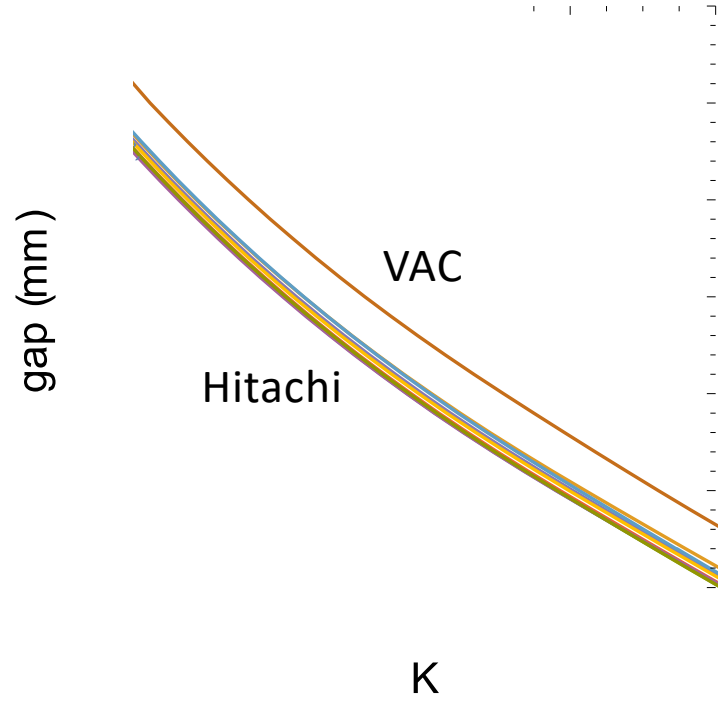
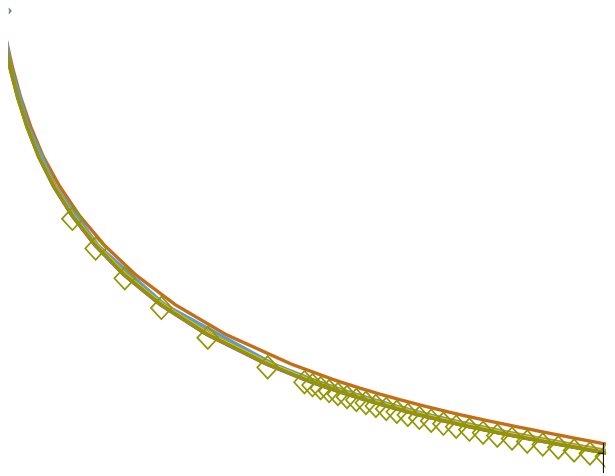


Summary of the 13 undulator of Aramis line

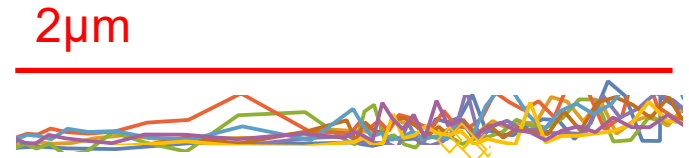
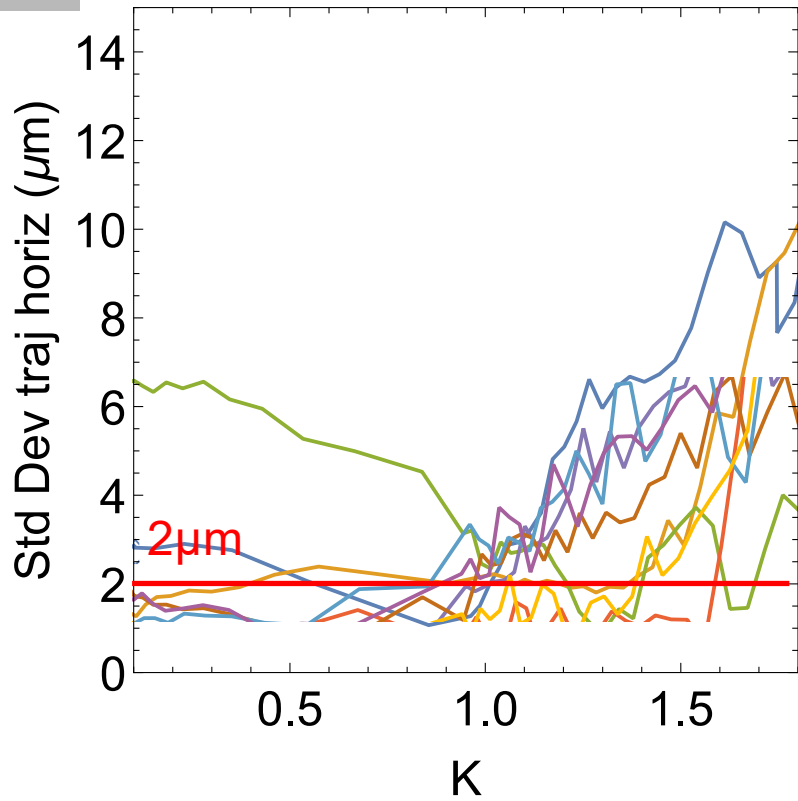


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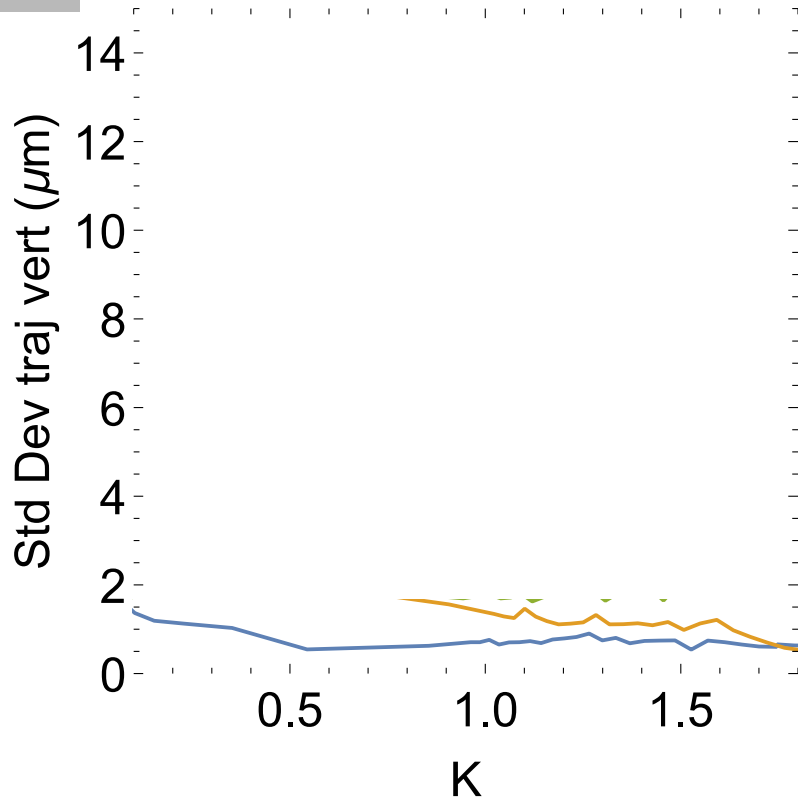
Setting the gap



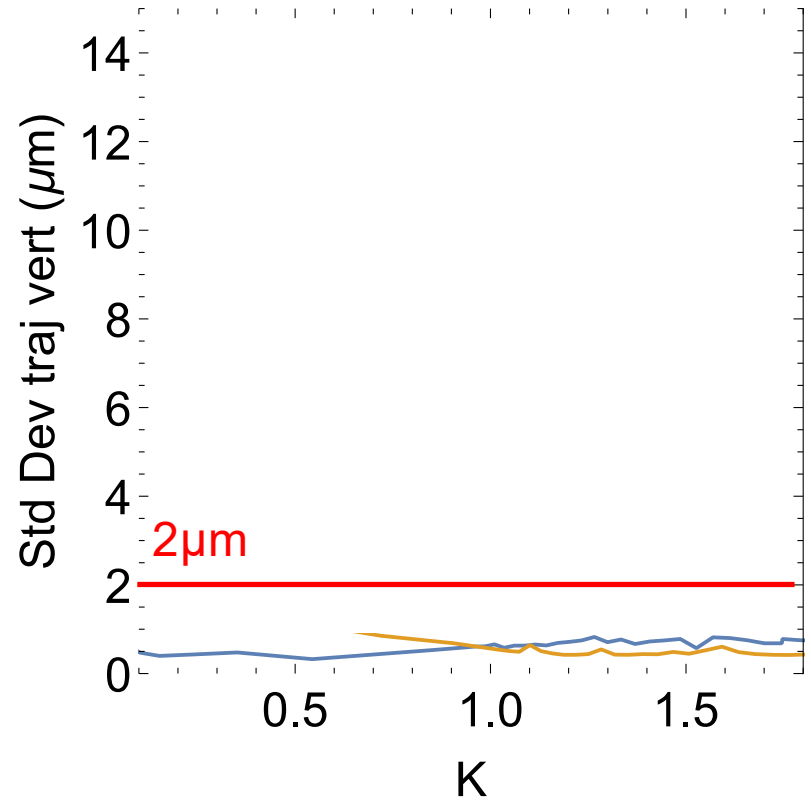
before correction

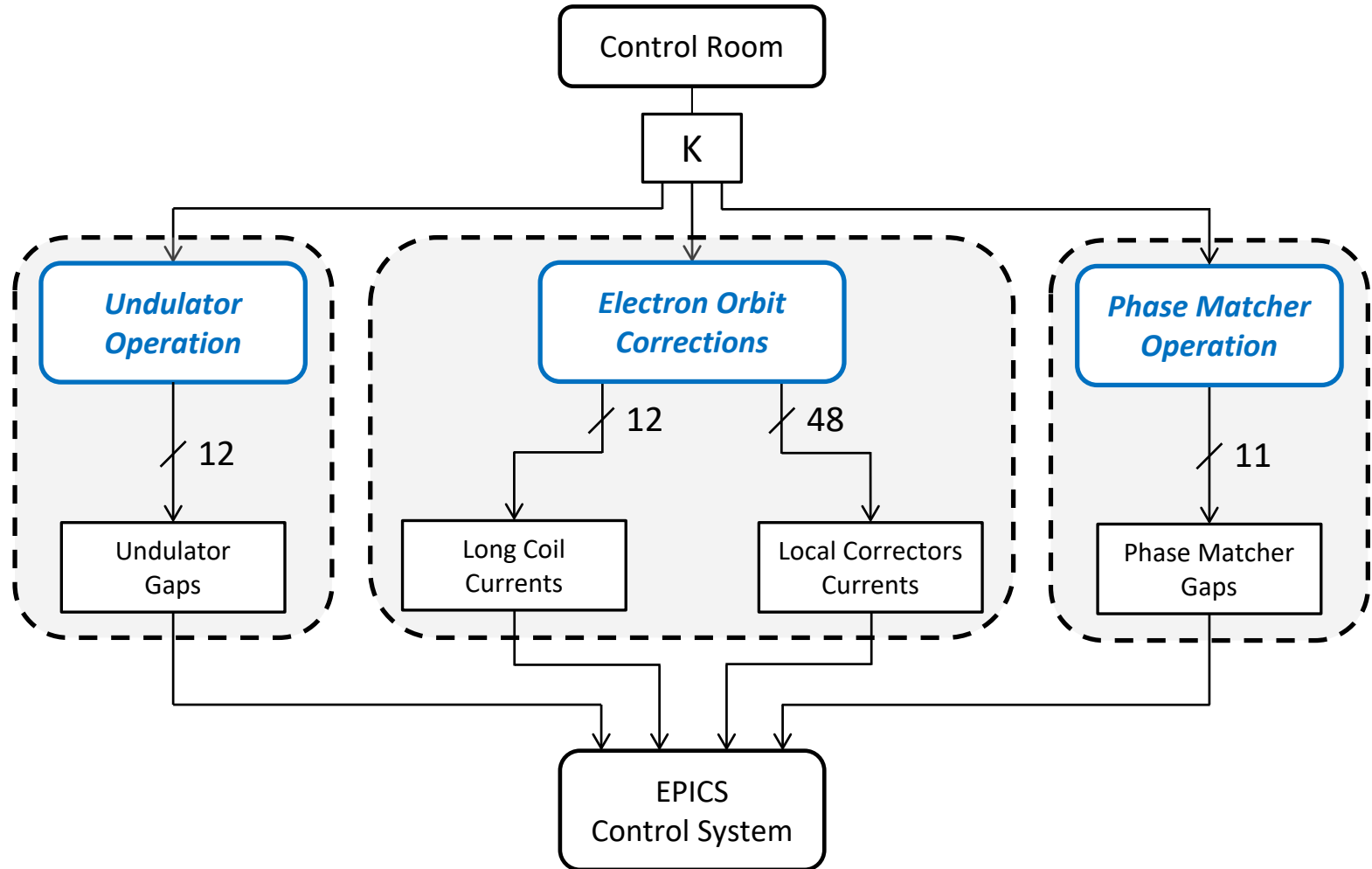


before correction



after correction

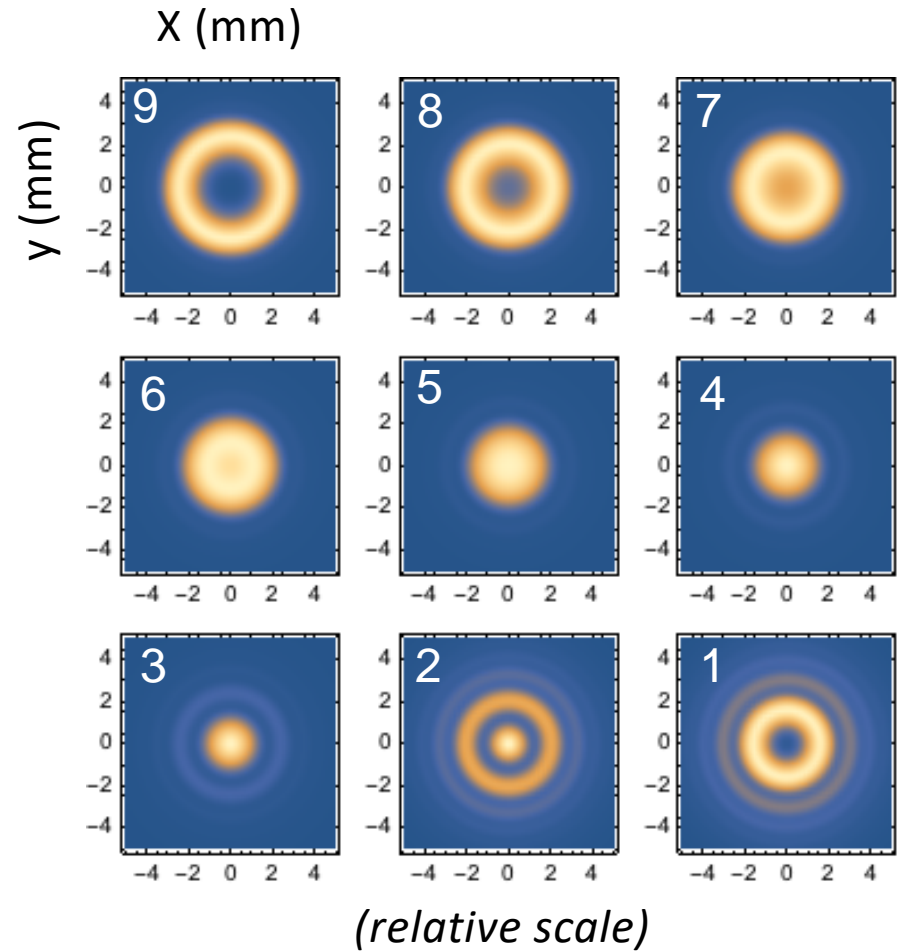
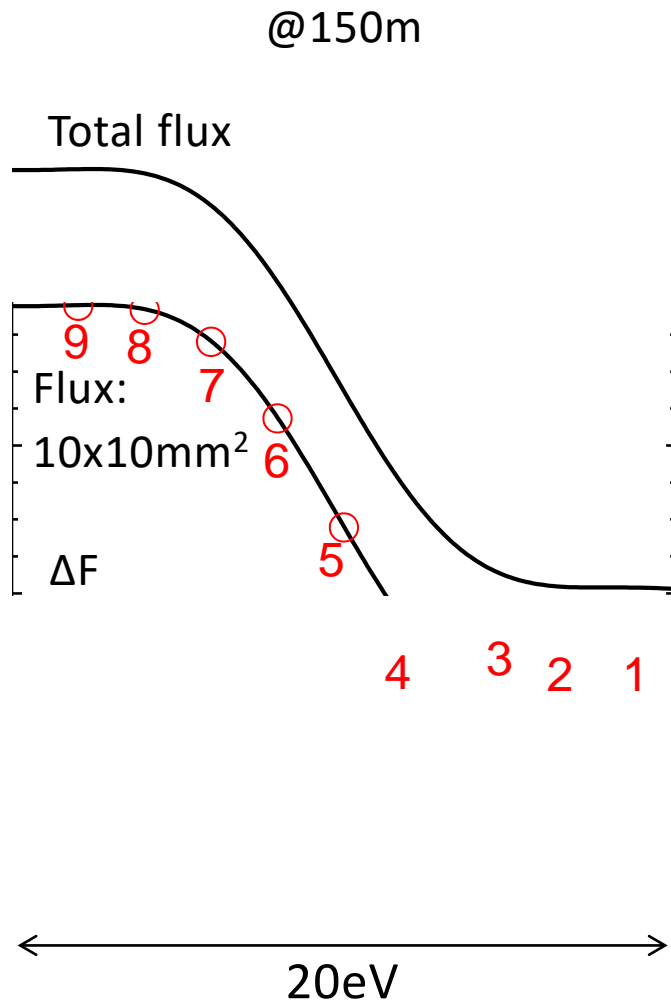




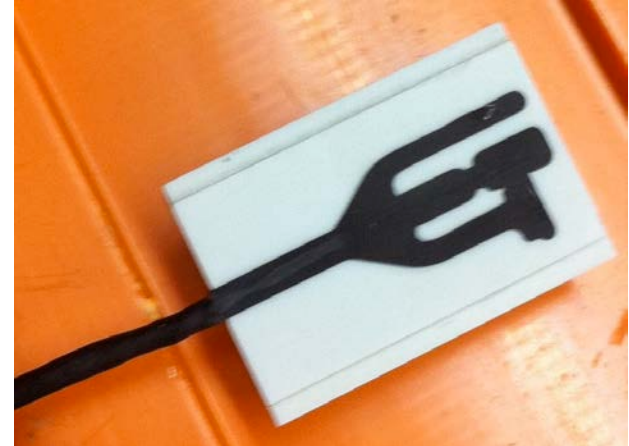
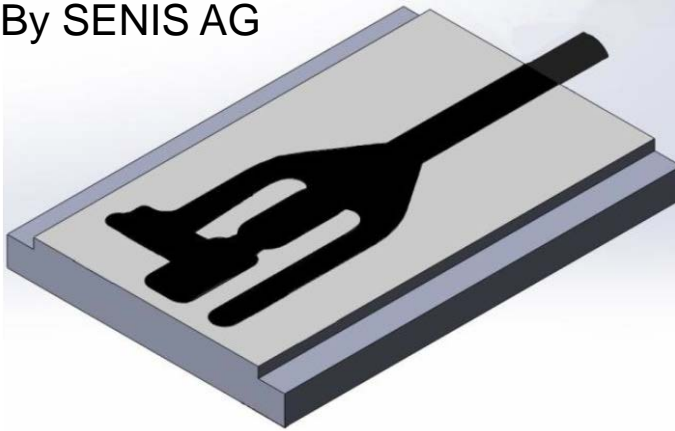
**OPEN FOR
QUESTIONS**



E=3.0GeV & K=1.8 – 1st harmonic



By SENIS AG

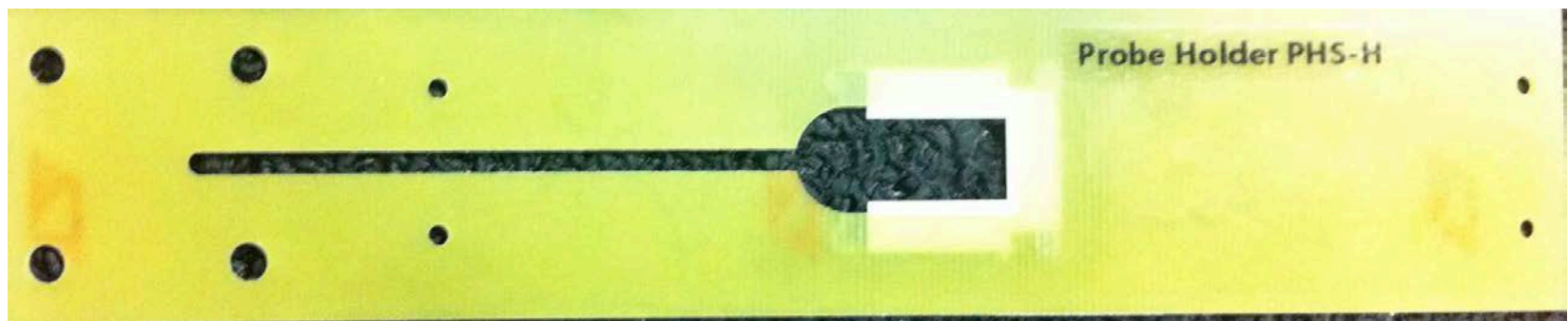


Dimensions: 1.5x10.5x15.0mm³

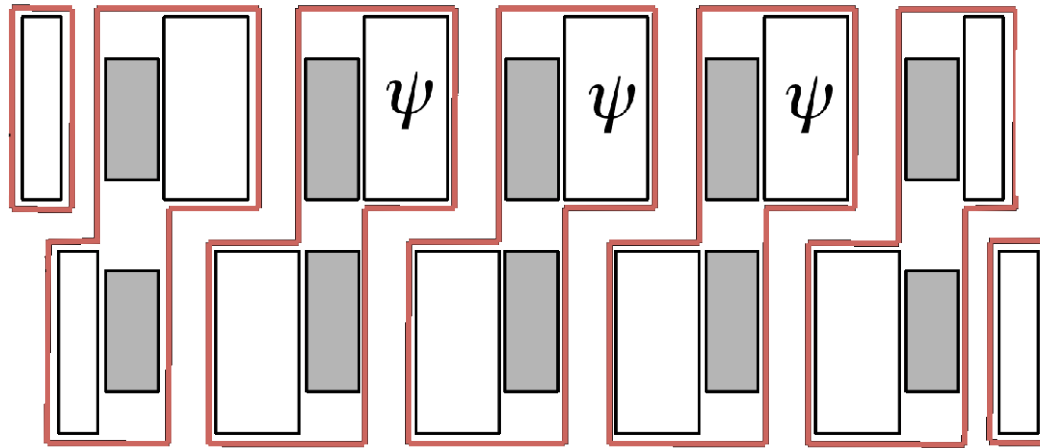
Mutual orthogonality: $<2^\circ$

Angular accuracy with respect to the reference surface: $\pm 2^\circ$

The three probes are all at the same height of 0.75 (middle of the probe) and horizontal position, while they are spaced longitudinally by 2mm



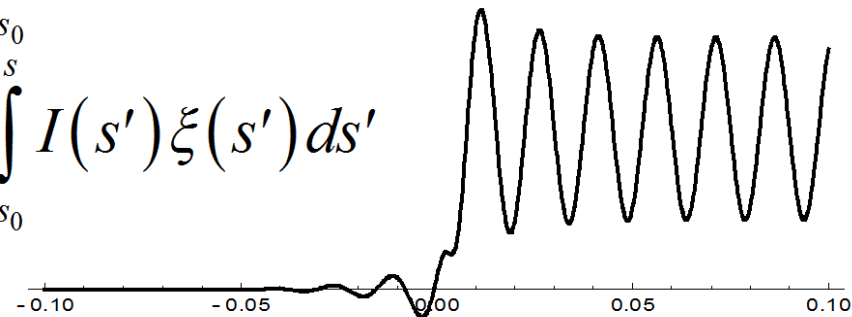
Optimization: Phase



Phase

$$\xi(s) = \int_{s_0}^s \psi(s') ds'$$

$$\chi(s) = \int_{s_0}^s I(s') \xi(s') ds'$$



$$\Delta\varphi(s) = 2\alpha \sum_n b_n \chi(s - s_n)$$

