<u>Study on the discrepancy between the prediction from magnetic</u> <u>measurement and the result from beam based</u> <u>measurement/spectral measurement for NSLS-II IDs</u>

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IMMW20 June 4-9 at Diamond LS



# <u>Outline</u>

- NSLS-II Storage Ring and Science Programs
- NSLS-II Insertion Devices
  - -List of IDs, Installation History, etc.
  - -NSLS-II ID-Magnetic Measurement Facility (ID-MMF)
  - -Spectrum based ID alignment
  - -1<sup>st</sup> Integral comparison between mag. meas. and beam based one
  - -Multipole Measurement / Skew quadrupole issue
- Summary

Acknowledgement:							
ID group members:	<u>C. Kitegi (now at Soleil),</u> D. Hidas, <u>M. Musardo</u> , J. Rank, <u>D.A. Harder</u> , P.						
	Cappadoro, H. Fernandes, T. Corwin, C. Rhein and B. Licciardi						
Part-time members:	Y. Hidaka, O. Chubar and C. Spataro						
Accelerator Physics:	A. Blednykh and Y. Li						
Vacuum Group:	Charles Hetzel and Charles De La Parra						
Various Beamline Group Members							





# **Evolution of LS**

Science

#### Emittance of World's SR souces



NATIONAL LABORATORY Light Source II

# NSLS-II

#### A 3<sup>rd</sup> Generation Synchrotron Light Source Min Beam size: $\sigma_x = 28 \ \mu$ m; $\sigma_y = 2.6 \ \mu$ m; bunch length = $\sim 4.5$ mm

 $\varepsilon_x = 0.9 \text{ nm-rad}$  (w. 6 DWs)  $\varepsilon_y = 8 \text{ pm-rad}$ Accelerators:

200-MeV Linac 3-GeV Booster, 1-2 Hz, C = 158.4 m

3-GeV SR: I = 500 mA, C = 792 m, 30 Achromatic DBA cells

#### **Experimental Facilities:**

19 ID+BM Beamlines as of March 2017 Capable of hosting 60+ beam lines Feb 2009 Start of Construction Mar 2012 Linac Beam Commissioning Dec 2013 Booster Beam Commissioning **April 2014 SR Beam Commissioning Started** Jan 2015 Stable Beam for Users July 2015 Designated as DOE's User Facility Oct 2015 Top-up operation started







National Synchrotron



# NSLS-II Storage Ring Current Status

- Max current of 400mA with two SRFs w/o IDs closed. Normal operation at 300mA with top-off.
- The third cavity is planned to be installed to start 500mA operation in 2019.
- $\varepsilon_v$  < 8pm with all IDs closed has been achieved. (only two out of 19 beam lines prefer low emittance mode)
- Beam stability of ~1% in horizontal and <10% in vertical beam size with FOFB on.
- Eight IVUs, Five EPUs, Six DWs, Five 3PWs One In-Air Device (refurbished ESRF) are in place.
- Refurbished EPU60 from SRC is to be installed in August17 shutdown



Tandem FPUs: 1.4m-EPU57 & 2.7m-OEPU105

Science

Canted 2.8m In-Vacuum Undulator (IVU23)

Superconducting RF



# **NSLS-II Beamline Portfolio**



Science

#### Soft X-Ray Scattering & Spectroscopy

23-ID-1: Coherent Soft X-ray Scat (2015) 23-ID-2: Coherent Soft X-ray Spectr & Pol (2015/2016) 21-ID: Photoemission-Microscopy Facility (2017) 2-ID: Soft Inelastic X-ray Scattering (2017) 22-BM: Magneto, Ellipso, High Pressure IR (2018)

#### **Complex Scattering**

10-ID: Inelastic X-ray Scattering (2015) 11-ID: Coherent Hard X-ray Scattering (2015) 11-BM: Complex Materials Scattering (2016) 12-ID: Soft Matter Interfaces (2017)

#### Diffraction & In Situ Scattering

28-ID-1: X-ray Powder Diffraction (2015) 28-ID-2: X-ray Powder Diffraction (2017) 4-ID: In-Situ & Resonant X-Ray Studies (2017) 27-ID: High Energy X-ray Diffraction (2020) 25-ID: Materials in Radiation Environments (2020?)

#### Hard X-Ray Spectroscopy

8-ID: Inner Shell Spectroscopy (2017) 7-BM: Quick X-ray Absorption and Scattering (2016) 8-BM: Tender X-ray Absorption Spectroscopy (2017) 7-ID-1: Spectroscopy Soft and Tender (2017) 7-ID-2: Spectroscopy Soft and Tender (2017) 6-BM: Beamline for Mater. Measurements (2017)

#### Imaging & Microscopy

3-ID: Hard X-ray Nanoprobe (2015) 5-ID: Sub-micron Res X-ray Spec (2015) 4-BM: X-ray Fluorescence Microscopy (2017) 18-ID: Full-field X-ray Imaging (2018)

#### Structural Biology

17-ID-1: Frontier Macromolecular Cryst (2016) 17-ID-2: Flexible Access Macromolecular Cryst (2016) 16-ID: X-ray Scattering for Biology (2016) 17-BM: X-ray Footprinting (2016) 19-ID: Microdiffraction Beamline (2017)

# NSLS-II Insertion Devices Damping Wiggler (DW) APPLE-II Type Elliptically Polarizing Undulator (EPU) In-Vacuum Undulator (IVU)

• Three Pole Wiggler (3PW) – Sometimes called Wavelength Shifter





# **NSLS-II Insertion Devices**

#### Five Apple-II EPUs (Four different types)



by Kyma SRL

Six 3.4-m hybrid 1.8T PM damping wigglers



#### Nine In-Vacuum Undulators (IVUs)



by Hitachi Metal America (Neomax)



#### **Refurbished in-house design IVU18**

National Synchrotron

BROOKHMVEN

NATIONAL LABORATORY Light Source II



# Three Pole Wiggler (3PW)



#### Hybrid 3 Pole Vertical Field







# **3PW+BM Radiation Intensity Distributions**

Observation Distance: 30 m (from 3PW Central Pole)



# NSLS-II Insertion Device List (Project IDs)

Beam Line	Туре	Design	Beam port	Location	Length [m]	Period [mm]	Peak Field [T]	K <sub>max</sub>	Canting Angle [mrad]	Vac Aper [mm]	Fund. [eV]	Total Power [kW]
							0.57 (heli)	2.6 (heli)			230 (heli)	7.3 (heli)
CSX1 /CSX2 EPU4		PPM	Low-β <sub>x</sub>	23-ID	4 (2×2)	49	0.94 (Lin)	4.3 (Lin)	0.16	8.0	180 (Lin)	9.9 (Lin)
	EPU49						0.72 (vlin)	3.2 (vlin)			285 (vlin)	5.5 (vlin)
							0.41 (45d)	1.8 (45d)			400 (45d)	1.7 (45d)
IXS	IVU22	Hybrid	High- $\beta_x$	10-ID	6 (1×3) center	22	1.52	1.52	0	7.2	1802	4.7x2
HXN	IVU20	Hybrid	Low-β <sub>x</sub>	3-ID	3	20	1.03	1.83	0	5.0	1620	8.0
СНХ	IVU20	Hybrid	Low- $\beta_x$	11-ID	3	20	1.03	1.83	0	5.0	1620	8.0
SRX /(XFN)	IVU21	Hybrid	Low-β <sub>x</sub>	5-ID	1.5 downstream	21	0.90	1.79	2.0	6.2	1570	3.6
XPD /PDF	DW100	Hybrid	High- $\beta_x$	28-ID	6.8 (2×3.4)	100	1.8	~16.5		11.5		64.5

 Total 7 Insertion Devices (IDs) installed and commissioned as part of NSLS-II Project

# NSLS-II Insertion Device List (NEXT, ABBIX, Partner)

Beam Line	Project	Туре	Design	Beamport	Location	Length [m]	Period [mm]	Peak Field [T]	K <sub>max</sub>	Canting Angle [mrad]	Vac Aper [mm]	Total Power [kW]
ESM	NEXT	EPU105/ EPU57	PPM	Low-β <sub>x</sub>	21-ID	2.7/1.4	105/49	0.74/0.57 (heli) 0.90 (vlin) 1.14/0.83 (Lin)	7.23/3.55 (heli) 7.23/3.06(vlin) 11.2/4.4 (Lin)	2.0		4.22/1.2 (heli) 4.22/0.86 (vlin) 10.1/2.0 (Lin)
SIX	NEXT	EPU57	PPM	High- $\beta_x$	2-ID	7.0 (2×3.5)	57	0.57 (heli) 0.83 (Lin)	3.55 (heli) 4.41 (Lin)	0		4.4 (heli) x2 6.8 (Lin) x2
ISR	NEXT	IVU23	Hybrid	High-β <sub>x</sub>	4-ID	2.8	23	0.95	2.05	2.0	6.0	
SMI	NEXT	IVU23	Hybrid	High-βx	12-ID	2.8	23	0.95	2.05	2.0	6.0	
ISS+XFP	NEXT	DW100	Hybrid	High- $\beta_x$	18-ID	6.8 (2×3.4)	100		~16.5		11.5	64.5
FXI	NEXT	DW100	Hybrid	High- $\beta_x$	8-ID	6.8 (2×3.4)	100		~16.5		11.5	64.5
LIX	ABBIX	IVU23	Hybrid	High- $\beta_x$	16-ID	2.8	23	1.02	2.2	0	5.5	
FMX/AMX	ABBIX	IVU21	Hybrid	Low-β <sub>x</sub>	17-ID	1.5 x 2	21	0.90	1.79	2.0	6.2	3.6
SST	Partner	U42	Hybrid	Low-β <sub>x</sub>	7-ID	1.6	42	0.82	3.27	2.0	8.0	3.2
	Partner	EPU60	PPM	Low-β <sub>x</sub>	7-ID	0.89	60	0.73 (heli)	4.1 (heli)		8.0	1.8 (heli)
								1.02 (Lin)	5.7 (Lin)	•		2.7 (Lin)
NYX	Partner	IVU18	Hybrid	Low-β <sub>x</sub>	19-ID	1.0	18	0.95	1.55	0	5.4	2.5
HEX	Partner	SCW80	EM	Low-β <sub>x</sub>	27-ID?	1.0	55	4.2	21.6	0	10	49.7

• 11 additional IDs installed so far (9 commissioned) as part of 3 different projects

- 1 more ID (SST) soon to be installed
- 2 SCWs (1.2m, 80mm period, 4.5T) planned in coming years

# NSLS-II ID-Mag. Meas. Facility Coil Measurement System Hall probe bench In Vacuum Magnetic Measurement System Our Cross Calibration Results Multipole Measurement for Small Gap ID





# ID-MMF (Coil Measurement System, Hall probe bench)

Integrated Field Measurement System by ADC USA Inc

- Reference surface flatness ±5 µm.
- Weight of each granite support: 1580 kg

3D Hall probe bench MMB-6500 by Kugler, GmbH - SENIS 3D Hall Probe (Type P for H3A)

- Flatness deviation  $< \pm 3 \,\mu m$
- Longitudinal Positioning accuracy  $< \pm 1 \mu m$ .
- 9 Motion Controlled Axes.

#### Details: M. Musardo (IMMW19)



# In-Vacuum Undualtor with a "Side Window" at ID-MMF



# Magnetic Measurement Revealed Pole Damage in an IVU

BNL's mag measurement revealed that there was a big error in the first peak field value





# In-Vacuum Magnetic Measurement System (IVMMS) Dec 2012

#### PrFeB Undulator:λu=17mm, 47CR

LN2 Cold Measurement Tes

#### Issues:Thermal load for cryogenic meas. Vacuum compatible lubricant

## Fixed Gap Calibration-Array for Cross-calibration

(1) BNL vs Danfysik Hall Probe Scan @ X=0 mm NdFeB - Fixed gap = 5.7 mm,  $L = 50 \text{ cm}, \lambda = 15 \text{ mm}$  $\Delta B_{max} = 77 G$ Residual [T 2.5 x10 sdev: 16.504 G  $\partial B_{max} = 1.1 \%$ -2.5  $\Delta B_{min} = 58 G$ By-Taper is: -85.191 G/m B max: 0.68379 T B min: 0.67583 T ∂B<sub>min</sub> =0.8 % By-Peaks [T]  $\Delta$ Taper = 40 0.682 G/m 0.680 ∆B=67.2 G 0.678 ∂B= 0.98 % 0.676-30  $\Delta \sigma = 0.2$  ° 10 2040 50 0 **#Poles** Field Integrals Measurement by 3 Labs





## Hall Probe Measurement Comparison for SIX-EPU57



# Field Integral Comparison for SIX-EPU57

#### (2) BNL vs Kyma



# **A Caveat for RMS Phase Error**

•Radiation Phase 
$$\phi = k_s z - \omega_s t$$
 then  $\frac{d\phi}{dz} = k_s - \omega_s \frac{1}{\frac{dz}{dt}} = k_s - \frac{\omega_s}{c} \frac{1}{\frac{v_{ll}}{c}} = k_s \left(1 - \frac{1}{\beta_{ll}}\right) \beta_{ll} = \sqrt{\beta^2 - \beta_{\perp}^2}$   
 $(\beta_{ll})^{-1} = \left(\beta^2 - \beta_{\perp}^2\right)^{-\frac{1}{2}} = \left(1 - \frac{1}{\gamma^2} - \beta_{\perp}^2\right)^{-\frac{1}{2}} \approx 1 + \frac{1}{2\gamma^2} + \frac{\beta_{\perp}^2}{2}$  Therefore, the phase advance over the distance S is RMS Phase Errors with N periods  
 $\phi(S) = \frac{k_s}{2} \left[\frac{S}{\gamma^2} + \int_0^S \left|\beta_{\perp}\right|^2 dS\right]$ 

→ However, the below formula is applicable only when the errors are RANDOMLY distributed.

Intensity(deg, n) 
$$\approx I_{ideal} e^{-\left(\frac{n\pi \cdot \text{deg}}{180}\right)^2}$$

Calculated spectrum shows very little degradation



# **ID Integrated Mutiplole Estimates**

 Note: Multipole expansion is a solution of Laplace equation (i.e. without source). Therefore measurement in horizontal dimension should be equal to the gap value. <u>All the vendors were making this mistake.</u>



 Beam Based Measurement on 2<sup>nd</sup> order kicks in APPLE-II EPUs
 Beam Based Field Integral Measurement
 Spectral Based ID Alignment

#### Measurements of 2<sup>nd</sup> order kick in LV Mode in Apple-II EPU57



Closed w/ CS Closed w/o CS Open Measured  $v_x$ 0.20458 0.19216 0.20307 Expected  $v_r$ N/A 0.19156 0.20422 Measured  $v_{y}$ 0.25397 0.25804 0.25610 Expected  $v_{v}$ N/A 0.25802 0.25567

#### 18 current strips per device



second order kicks (Elleaume, EPAC 1992):

$$\theta_{x/y} = -\frac{1}{(B\rho)^2} \int \left\{ \int B_x dz' \cdot \int \frac{\partial B_x}{\partial x/y} dz' + \int B_y dz' \cdot \int \frac{\partial B_y}{\partial x/y} dz' \right\} dz$$



 $x \, [mm]$ 



# Field Integrals: Beam-based vs. Flip Coil Meas.

			Gap	Coil $\Delta I_x$ [G.cm]	Coil $\Delta I_v$	e-beam $\Delta I_x$	e-beam $\Delta I_v$	RMS $\Delta x$	RMS $\Delta y$	
Device	Location	Date	[mm]		[G.cm]	[G.cm]	[G.cm]	[µm]	[µm]	***7 5mm dan
IVU20	C3	2/25/15	6.7	-15.6	3.4	-11.1	-3.4	1.152	0.501	7.5mm gap
IVU20	C11	2/25/15	6.7	-100.8	11.6	18.0	32.5	1.187	0.593	
IVU21	C5	11/15/14	6.2	-71.2	85.8	-104.454	102.777	1.417	1.084	**6.8mm gap
		2/25/15 **	6.5	-90.9*	72.5*	-81.194	88.924	1.199	2.787	01
IVU22	C10 (LS)	11/21/14	6	214	17.7	-24.237	-15.945	2.419	1.189	
		2/25/15	7.2	-109***	41.1***	-63.984	-18.226	2.534	3.014	*Realigned after
DW	C8U	12/20/14	15	-21.3	-55.4	-105.159	-99.38	8.818	4.485	vear-end shutdown
		2/25/15	15			-62.961	-79.578	5.546	4.252	in 2014
	C8D	1/23/15	15	152	159	59.702	215.524	6.066	6.634	
		2/25/15	15			42.042	199.967	10.021	5.955	
	C18U	12/17/14	15	-22.8	13.7	-144.666	-76.481	5.795	6.456	
		2/25/15	15			-96.179	-67.754	4.659	3.454	
	C18D	12/20/14	15	3.95	-13.2	-187.691	95.166	5.464	5.249	
		2/25/15	15			-213.981	79.656	5.950	9.544	
	C28U	12/8/14	15	-95.9	-24.267	141	-57.057	5.106	6.544	
		2/25/15**	15			-67.9	-53.881	4.564	3.326	
	C28D	12/8/14	15	-30.9	-237	-290	178.495	5.134	17.54	
		2/25/15 **	15			-206	160.369	7.758	6.311	

- Beam-based fitting is worse (RMS  $\Delta x \& \Delta y$ ) for DWs than for IVUs
  - -Stronger focusing effect of wigglers, sensitive to vertical orbit centering
  - –Large horizontal wiggling motion => path lengthening
- Many show large discrepancies
  - Potential causes: Earth field variation, nearby ferromagnetic structures, stray B-field, misalignment during installation
  - -Found vertical ID corrector strengths for DWs to be insufficient

# <u>Examples of Spectrum Based Alignment of IVUs</u> <u>at Hard X-ray Beamlines of NSLS-II</u>

#### **On-Axis UR Spectra Before and After Spectrum Based Alignment**

IVU21 - 1.5 m at SRX BL IVU23 - 2.8 m at SMI BL IVU23 - 2.8 m at LiX BL (harm. #5 at ~6.8 mm gap, ~8.0 keV) (harm. #7 at ~6.5 mm gap, ~8.07 keV)(harm. #9 at ~6.2 mm gap, ~9.24 keV



Spectral performance of ~Half of NSLS-II IVUs was restored / improved thanks to the Spectrum-Based Alignment procedure. The "underperforming" IVUs are identified by comparison of their measured spectra with SRW simulations (making use of magnetic measurements data).

O.Chubar

# Gap Center Search by E-Beam

- <u>https://logbook.nsls2.bnl.gov/Operations/index.html#38760\_1</u>
- yhidaka, 3/2/16, 8:57 am Show details
- Elevation scan indicates that the optimal elevation for ID12-2 is +560 um. Note that the beam orbit was vertically off by +100 um. So, the ID needs to be raised by 460 um mechanically to align around BBA.



# HXN (3-m IVU) with Beam Steering



# Effect of Vertical Translations/Angle (Calibration Array)



On-Axis: lx=5.8 G.cm, ly=21G.cm Ph.Err=1.6°

Y=+0.2mm: lx=14 G.cm, ly=27G.cm Ph.Err=1.6 °

Y=-0.2mm: lx=7.1 G.cm, ly=28G.cm Ph.Err=1.6 °

Y[Z=0]=0 Vertical Angle 0.2mrad: Ix=11 G.cm, Iy=24G.cm Ph.Err=3.2°

#### Old Beam Data before Spectral Optimization New Beam Data after Spectral Optimization SRX SRX-Ix-Beam SRX-Ix-Beam SRX-lv-Beam 100 SRX-ly-Beam SRX-Ix-Coil Fist Integral (G.cm) SRX-Ix-Coil 200 Fist Integral (G.cm) SRX-ly-Coil SRX-ly-Coil 50 100 0 0 -50 -100 -100 7 9 10 8 7 8 9 10 Gap (mm) Gap (mm) LIX 20 0 -20 0 -40 -20 LIX-Ix-beam LIX-Ix-beam -60 LIX-ly-beam LIX-ly-beam LIX-Ix-Coil LIXC-Ix-Coil -40 LIX-ly-Coil LIXC-ly-Coil -80 15 20 25 30 35 10 40 10 15 20 25 Gap (mm) Gap (mm)

#### SRX (1.5-m IVU) & LIX (2.8-m IVU) Mag. Meas. vs Beam

# SMI (2.8-m IVU) Mag. Meas. Vs Beam



Old Beam Data Before Spectral Optimization (beam with +100 mm vertical offset)

New Beam Data After Spectral Optimization



# SIX (3.5m EPU) Mag. Meas. Vs Beam



Integrated Field Integral variations with beam are larger than those by magnetic field measurement

 $\rightarrow$  Spectral optimization may be still needed



33

# In-Situ Direct Gap Measurement Used in IVU18 (2005)

(Was not used for NSLS-II IVUs Due to their Larger Vacuum Chamber Size) Measurement accuracy of  $\pm 2\mu m$  and repeatability of  $\pm 0.15\mu m$ .







# ID Coupling Correction

- SQ error estimates by DTBLOC (Driving-Terms-based Linear Optics Calibration) algorithm [Y. Hidaka et al. NAPAC 2016
  - Based on RDTs formalism used by ESRF coupling correction [A. Franchi et al., PRSTAB 14, 034002 (2011)]
  - Also estimates normal guad errors as well as BPM gains/rolls/deformations (very important for coupling!)
  - Very fast (~2 min. data acq. [TbT + Dispersion], ~3 min. data proc. & fitting, for 1 iteration)

$$\begin{split} f_{1001}(s) &\cong \frac{\sum_{w} (\Delta a_{2}L)_{w} \sqrt{\beta_{x}^{w} \beta_{y}^{w}} e^{i(\Delta \phi_{x}^{w,s} \mp \Delta \phi_{y}^{w,s})}}{4\left(1 - e^{2\pi i \left(\nu_{x} \mp \nu_{y}\right)}\right)} \quad \left| f_{x1} \right| = \sqrt{2I_{x} \beta_{x0}} \quad \left| f_{y1} \right| = \sqrt{2I} \\ f_{x2} &= \sqrt{2I_{y} \beta_{x0}} \sqrt{\left(2\Im\{f_{1001}\} + 2\Im\{f_{1010}\}\right)^{2} + \left(2\Re\{f_{1001}\} - 2\Re\{f_{1010}\}\right)^{2}}}{f_{y2}} \\ f_{y2} &= \sqrt{2I_{x} \beta_{y0}} \sqrt{\left(2\Im\{f_{0110}\} + 2\Im\{f_{1010}\}\right)^{2} + \left(2\Re\{f_{0110}\} - 2\Re\{f_{1010}\}\right)^{2}} \\ \end{split}$$

35

- With feedforward turned on under a nominal user operation condition (i.e., high current, moderate emittance):

  - $\Delta \sigma_y$  of 60% (260% in  $\varepsilon_y$ ) => 4% (8%) Beam-current-lifetime-product change of 53% reduced to 11%.
- Table generated at low current (2 mA) (.207, .285) was equally effective at high current (250 mA).



# <u>Summary</u>

- Magnetic measurement system at the NSLS-II has been cross-calibrated with other facilities' similar equipment.
- Some devices' characteristics had changed after transportation (may be due to mechanical shocks, extra baking process, variation in earth field?)
- EPU's 2<sup>nd</sup> order effect (dynamic integral effect) has been successfully compensated with current strips.
- Multipole measurement for small gap ID poses new challenge in terms of accuracy of measurement.
- Discrepancy between magnetic measurement and beam based one was larger with high field wiggler maybe due to:
  - Stronger focusing effect of wigglers, sensitive to vertical orbit centering
  - Large horizontal wiggling motion contributes increased path length.
- Beam-based measurement of horizontal field integral is more sensitive to beam orbit than that of vertical field.
- Beam-based kick measurement assumes straight trajectory inside an ID. However, magnetic measurements of some IDs show that some devices have somewhat curved trajectory in the ID.

#### More to do:

- o More spectral optimizations for other IDs and repeat the same experiment
- Use long coils to straighten the trajectories in some IDs and repeat the same experiment
- o Identify the sources of extra field in the tunnel

# •Back up slides

# **Dynamic Aperture Considerations**

•J.Benstsson 2007 ID review

The impact of Insertion Devices (IDs) is given by

$$\langle H \rangle_{\lambda_{u}} = \frac{p_{\chi}^{2} + p_{y}^{2}}{2(1+\delta)} - \frac{k_{\chi}^{2} x^{2} - k_{y}^{2} y^{2}}{4k_{z}^{2} \rho_{u}^{2}(1+\delta)} - \frac{k_{\chi}^{4} x^{4} + 3(k_{\chi}^{2} - k_{y}^{2})k_{\chi}^{2} x^{2} y^{2} + k_{y}^{4} y^{4}}{12k_{z}^{2} \rho_{u}^{2}(1+\delta)} - \delta + O(p_{\chi,y})^{4}$$
(EQ 1)

which drive beta and phase advance beat, tune shift, nonlinear resonances, and amplitude dependent tune shift. In particular

$$\Delta v_{y} = \frac{\beta_{y} L_{u}}{8\pi \rho_{u}^{2}}, \qquad \mathcal{M} = e^{:h} \mathcal{M}_{\text{linear}}, \qquad \frac{\partial v_{y}}{\partial J_{y}} = \frac{\pi \beta_{y}^{2} L_{u}}{4\lambda_{u}^{2} \rho_{u}^{2}}$$
(EQ 2)

The beta and phase advance beat, and tune shift can be corrected locally.

- Top-up injection: stay-clear and efficiency.
- Touschek life time: momentum aperture, vertical physical apertures, and nonlinear dynamics.
- Impact on emittance: canting and Three-Pole Wigglers (~10% for 15 TPWs).

$$Min < \beta^{2}(s) > --- > \beta_{0} = L/2\sqrt[4]{5} \sim L/3$$



#### Impact of Radom Multipole Errors in the Long Straight

13 devices were used in the simulation

(J. Bengtsson)



$$T/m = 100G/cm$$

$$T/m^2 = G/cm^2$$

# A Typical "Canted" Short Straight

